

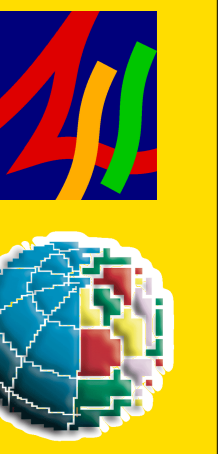
# S21A-0131 An energy-duration method for rapid and accurate determination of earthquake magnitude and tsunamigenic potential

Anthony Lomax

A Lomax Scientific, Mouans-Sartoux, France; anthony@alomax.net, www.alomax.net

Alberto Michelini and Alessio Piatanesi

Istituto Nazionale di Geofisica e Vulcanologia (INGV), Roma, Italy; www.ingv.it



## 1. Introduction

The 26 December 2004, M9 Sumatra-Andaman earthquake caused a tsunami that devastated Indian Ocean coasts within 3 hours; the 17 July 2006,  $M_w=7.7$  Java earthquake caused an unexpectedly large and destructive tsunami. For both events the magnitude and other information available within the first hour after the origin time (OT) severely underestimated the event size and tsunamigenic potential. Improved tsunami warning and energy response for future large earthquakes requires that accurate knowledge of the earthquake size and tsunamigenic potential is available rapidly, within 30 minutes or less after OT. There are a number of procedures for rapid analysis of large earthquakes in use at earthquake and tsunami monitoring centers. For example, the Pacific Tsunami Warning Center (PTWC) uses the  $M_{\text{obs}}$  moment magnitude and the  $M_s$  mantle magnitude. Currently, however, the earliest accurate estimates of the size of large earthquakes are moment tensor determinations, including the Harvard Centroid-Moment Tensor (CMT) (e.g., Dziewonski et al., 1981), based on long-period, S and surface-wave recordings, typically not available until an hour or more after OT.

Seismic P waves are the earliest signal to arrive at seismic recording stations. At teleseismic distances the arrival times of the initial P-wave are used routinely to locate the earthquake hypocentre within about 15 minutes after OT. The P-waves also contain comprehensive information about the event size and source character. Here we introduce a rapid and robust, energy-duration procedure to obtain an earthquake moment and a moment magnitude,  $M_{ED}$ , from P-wave recordings from global seismic stations at 30° to 90° distance from an event. At many earthquake and tsunami monitoring centers, these recordings are available within 20 to 30 minutes after OT. The energy-duration procedure combines a radiated seismic energy measured within the P to S interval on broadband records, and a source duration measured on high-frequency, P-wave records. The measured values also provide the energy-to-moment ratio  $\Theta$  (e.g., Newman, and Okal, 1998) for identification of tsunami earthquakes.

## 2. Theory

Haskell (1964) proposed a kinematic, double-couple, extended-fault model with scalar moment  $M_0$  and a trapezoidal, far-field, source-time function of duration  $T_0$  and rise / fall time  $xT_0$ . With this model, Vassiliou and Kanamori (1982) show that the radiated seismic energy,  $E$ , can be expressed as,

$$E = \frac{1}{15\pi\rho\alpha^3} + \frac{1}{10\pi\rho\beta^3} \left[ \frac{2}{x(1-x)^2} T_0^2 \right] M_0^2 \quad (1)$$

where  $\rho$ ,  $\alpha$  and  $\beta$  are the density, and P and S wave speeds, respectively, at the source. Solving Eq. (1) for  $M_0$  we find, for a given rise-time factor,  $x$ , a moment estimate,

$$M_0 = K x^{1/2} (1-x) E^{1/2} T_0^{3/2} \quad (2)$$

where  $K$  depends on  $\rho$ ,  $\alpha$  and  $\beta$  at the source. This compact expression (Eq. 2) shows that the scalar moment,  $M_0$ , for an earthquake can be obtained from estimates of the radiated energy,  $E$ , and the source duration,  $T_0$ .

## 3. Methodology

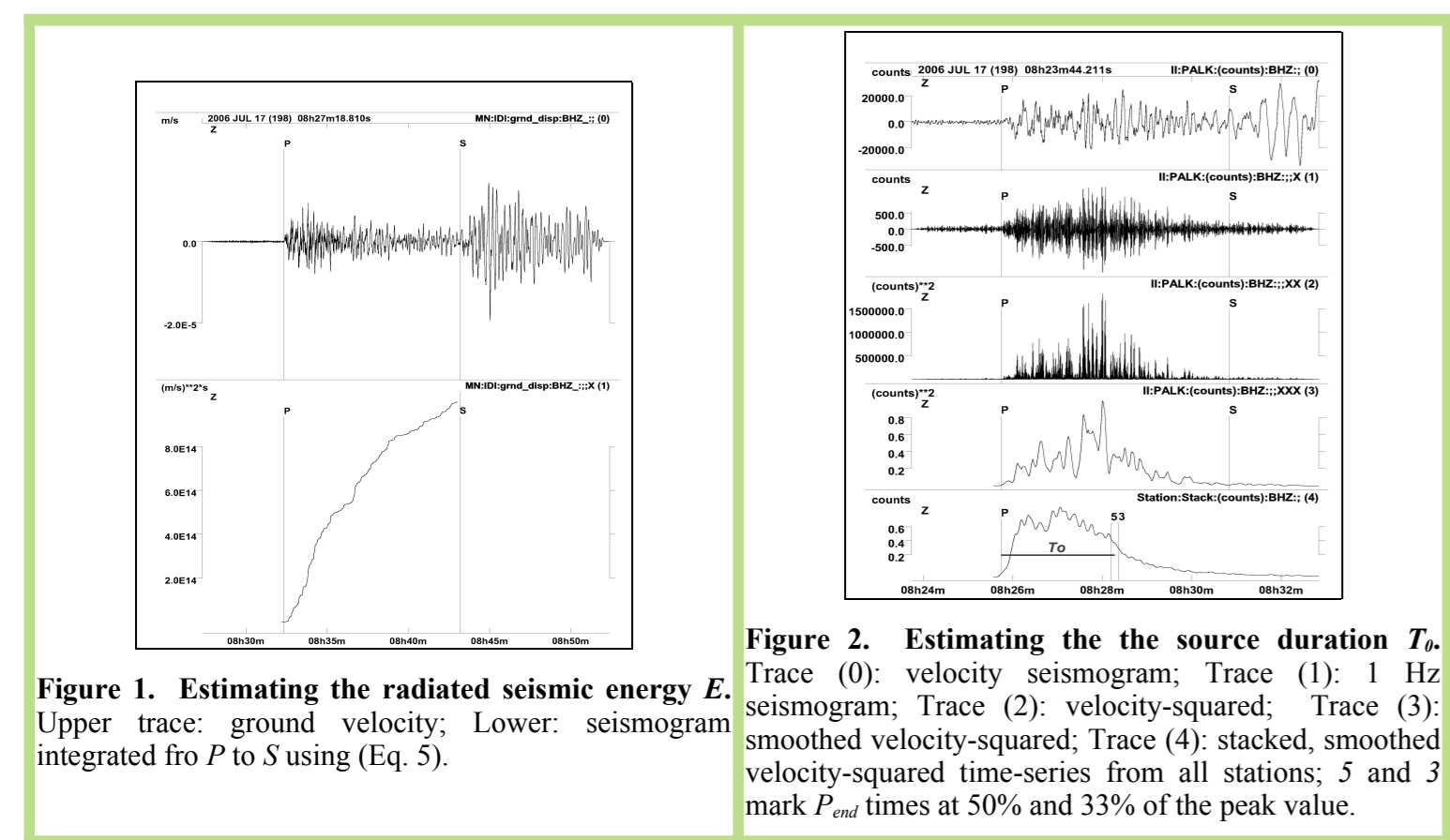
For each earthquake we require a hypocentre location and P and S travel times from the hypocentre to each station; currently, monitoring agencies have this information within about 10 minutes of OT for teleseismic events (great-circle distance (GCD) to recording stations > 30°). We use vertical-component, broadband, digital seismograms for about 10 or more stations at 30°-90° GCD from the source, moderately well distributed in distance and azimuth.

### Estimating the radiated seismic energy

An estimate of the radiated seismic energy,  $E$ , for a point, double-couple source using a P-wave seismogram is given by (e.g., Boatwright and Choy, 1986),

$$E = 53\pi r^2 \rho \alpha \int v^2 |r| dt \quad (3)$$

where  $v(t)$  is a ground-velocity seismogram,  $r$  is the source-station distance, and  $\rho$  and  $\alpha$  are the density and P wave speed, respectively, at the station; the constant terms include corrections for the P wave radiation pattern, free-surface amplification and attenuation. We estimate  $E$  for each event using the following procedure (Fig. 1): 1) Convert each seismogram to ground-velocity in m/sec. 2) Cut the seismogram from 10 seconds before the P arrival to 10 seconds before the S arrival to obtain P-wave seismograms. 3) Apply Eq. (3) to each P wave seismograms to obtain station energy values. 4) Multiply the station energy value by a factor  $T_0 / t_{s,p}$  if  $T_0 > t_{s,p}$ . 5) Calculate an average  $E$  and associated standard deviation for each event from the station energy values.



### Estimating the source duration $T_0$

To estimate the source duration,  $T_0$ , we make three assumptions: 1) the radiated P-waves contain higher frequencies than other wave types; 2) this signal can be isolated on the seismograms; 3) a meaningful time for the end of this signal can be determined. We estimate  $T_0$  for each event using the following procedure (Fig. 2), based on that of Lomax (2005) and Lomax and Michelini (2005): 1) Convert the seismograms from each station to high-frequency records using a narrow-band, Gaussian filter of the form  $e^{-\alpha|f-f_{\text{cut}}|/\beta}$ , where  $f$  is frequency,  $f_{\text{cut}}$  the filter center frequency, and  $\alpha$  sets the filter width (here we use  $f_{\text{cut}}=1.0$  Hz and  $\alpha=10.0$ ). 2) Convert each high-frequency record to kinetic-energy density by squaring the velocity values. 3) Smooth each velocity-squared time-series with a 10 sec wide, triangle function and normalize to form an envelope function. 4) Stack the station envelope functions aligned on their P arrival times to form a summary, event envelope function. 5) Measure a source end time,  $T_{\text{end}}$ , defined as the mean of the times where the event envelope function last drops below 50% and below 33% of its peak value. 6) Calculate the source duration  $T_0$  from the difference between  $T_{\text{end}}$  and the stack alignment P time.

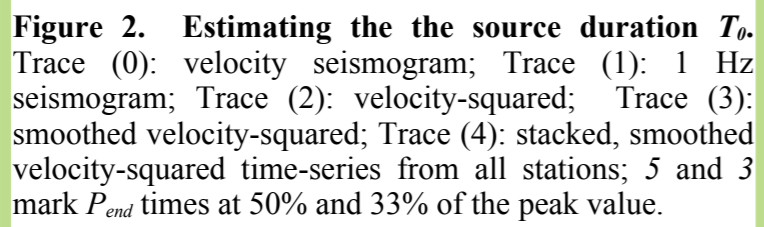


Figure 2. Estimating the source duration  $T_0$ . Trace (0): velocity seismogram; Trace (1): 1 Hz seismogram; Trace (2): velocity-squared; Trace (3): smoothed velocity-squared; Trace (4): stacked, smoothed velocity-squared time-series from all stations; 5 and 3 mark  $T_{\text{end}}$  times at 50% and 33% of the peak value.

### Estimating the radiated seismic energy $E_s$

For all the studied strike-slip earthquakes, however, we obtain  $E$  values that are less than those of NEIC by a factor of about 10, on average (Table 1, Fig. 5). All of these events have steeply dipping nodal axes close to which teleseismic P rays depart from the source; to allow meaningful comparison of our results with CMT values, we increase our radiated seismic energy values,  $E$ , by a factor of 10 for strike slip events to approximately account for this energy underestimate (Table 1,  $E$  corrected).

### Energy-duration moment and magnitude calculation

From the obtained values of the radiated seismic energy,  $E$ , and the source duration,  $T_0$ , we calculate an energy-duration estimate of the seismic moment,  $M_{ED}$ , using Eq. (2). We evaluate the unknown rise-time,  $x$ , through regression of our  $M_{ED}$  values for each event against the corresponding CMT moment values,  $M_{CMT}$ , so that the mean of  $\log_{10}(M_{ED}/M_{CMT}) \rightarrow 0$ . Finally we calculate an energy-duration magnitude,  $M_{ED}$ , through application of the standard moment to moment magnitude relation,

$$M_{ED} = (\log_{10} M_{ED} - 9.1) / 1.5 \quad (4)$$

where  $M_{ED}$  has units of N-m.

### Energy-to-moment ratio

From the obtained values of the radiated seismic energy,  $E$ , and our calculated seismic moment estimate,  $M_{ED}$ , we can determine the energy-to-moment ratio parameter,  $\Theta$ , (e.g., Newman, and Okal, 1998) for identification of tsunami earthquakes,

$$\Theta = \log_{10} \left( \frac{E}{M_{ED}^2} \right) \quad (5)$$

## 4. Application to recent large earthquakes

We apply our energy-duration methodology to 35 recent earthquakes with  $M_{CMT} \geq 6.9$  (Table 1). For each event, we obtain from the IRIS Data Center broadband vertical (BHZ) recordings at stations from 30° to 90° GCD. Equivalent data sets would be available within 30 minutes after a large earthquake. Applying the methodology outlined above, excluding poor quality data, we determine  $E$ ,  $T_0$ ,  $M_{ED}$ ,  $M_{ED}$  and  $\Theta$  for each event (Table 1).

Origin time	Event	Type*	NEIC			CMT			this study, energy-duration results									
			latitude (°)	longitude (°)	depth (km)	depth (km)	$M_{CMT}$ (N-m)	$M_{ED}$ (N-m)	$T_0$ (sec)	$T_0$ (sec)	$E$ (J)	$E$ corrected (J)	$M_{ED}$ (N-m)	$M_{ED}$ (N-m)	$\Theta$	$M_{ED}$ (N-m)		
1992.09.02 00:15	Nicaragua	I	11.74	-87.34	44	2.6E+14	15	3.4E+20	7.6	37	175	1.9E+14	1.9E+14	4.4E+20	7.7	-6.4	7.3	
1992.12.10 02:59	Flores Indonesia	I	-8.48	121.9	49	6.0E+15	20	5.1E+20	7.8	36	91	7.8E+15	7.8E+15	1.1E+21	8.0	-5.1	7.7	
1993.07.12 13:17	Hokkaido	I	42.85	139.2	18	8.7E+15	17	4.7E+20	7.7	33	78	1.0E+16	1.0E+16	9.8E+20	7.9	-5.0	7.6	
1994.01.17 12:30	S California	R	34.21	-118.54	21	1.1E+14	17	1.2E+19	6.7	11	17	1.2E+14	1.2E+14	8.9E+18	6.6	-4.9	6.9	
1994.06.02 18:17	Java	I	-10.48	112.84	6	1.2E+14	15	5.3E+20	7.7	23	97	3.8E+14	2.8E+14	2.6E+20	7.5	-5.8	7.5	
1994.09.00 03:33	Bolivia	D	-13.84	-67.55	631	3.2E+16	647	2.6E+21	8.2	40	42	4.8E+16	4.8E+16	3.0E+21	8.2	-4.8	7.8	
1994.10.04 13:23	Kuril	P	43.77	147.32	61	1.1E+17	68	3.0E+21	8.3	50	67	6.4E+16	6.4E+16	3.3E+21	8.3	-4.7	7.8	
1995.12.05 18:01	Kuril	I	44.66	149.3	23	2.4E+15	26	8.2E+20	7.9	28	71	2.9E+15	2.9E+15	7.5E+20	7.9	-5.4	7.6	
1996.02.10 05:59	Irian Jaya	I	4.89	136.95	11	8.5E+15	15	2.4E+21	8.2	59	114	8.9E+15	8.9E+15	1.0E+21	8.1	-5.3	-	
1996.02.21 12:51	Peru	I	-9.59	-79.59	4	-	15	2.2E+20	7.5	21	75	2.2E+14	2.2E+14	1.4E+20	7.4	-5.8	7.3	
1998.07.17 08:49	Papua New Guinea	I	-2.96	141.93	7	2.4E+14	15	3.7E+19	7.1	15	49	1.2E+14	1.2E+14	5.2E+19	7.1	-5.6	6.9	
1999.04.08 13:10	Russia-China	D	43.61	139.35	576	9.0E+14	575	5.1E+19	7.1	17	11	7.3E+14	7.3E+14	4.4E+19	7.0	-4.8	7.0	
1999.08.17 00:01	Turkey	S	40.75	29.86	13	8.1E+15	17	2.9E+20	7.6	41	51	1.2E+16	1.2E+16	4.4E+20	7.7	-4.6	7.6	
1999.09.20 17:47	Taiwan	R	23.77	120.98	8	1.5E+15	21	3.4E+20	7.6	40	58	2.7E+15	2.7E+15	2.4E+20	7.5	-5.0	7.6	
1999.10.10 09:46	S California	S	34.59	-116.27	20	1.9E+15	15	6.0E+19	7.1	20	42	1.5E+14	1.5E+14	1.2E+20	7.1	-4.9	7.4	
2000.10.06 04:30	W Honshu	S	35.46	133.13	10	2.9E+15	15	1.2E+19	6.7	12	54	4.8E+13	4.8E+13	9.9E+19	7.3	-5.3	6.8	
2001.01.26 03:16	S India	R	23.42	70.23	10	4.6E+15	20	3.4E+20	7.6	48	33	7.6E+15	7.6E+15	1.9E+20	7.5	-4.4	7.8	
2001.02.28 18:54	Washington	P	47.15	-122.72	-	1.1E+14	51	1.9E+19	6.8	12	15	1.1E+14	1.1E+14	1.4E+19	6.7	-5.1	6.6	
2001.03.24 06:27	W Honshu	P	34.08	132.53	-	5.5E+13	47	1.9E+19	6.8	12	34	7.4E+13	7.4E+13	4.1E+19	7.0	-5.7	7.0	
2001.06.23 20:33	Peru	I	-16.27	-73.64	8	2.9E+16	30	4.7E+21	8.4	86	135	1.5E+16	1.5E+16	4.5E+21	8.4	-5.5	7.5	
2002.11.01 22:12	Alaska	R	63.52	-147.44	4	3.3E+16	15	7.5E+20	7.1	17	39	2.8E+15	2.8E+15	4.4E+20	7.7	-4.2	7.4	
2003.05.21 18:44	N Algeria	R	36.96	3.63	9	3.4E+14	15	2.0E+19	6.8	12	28	2.2E+14	2.2E+14	2.5E+19	6.9	-5.1	7.0	
2003.09.25 19:50	Hokkaido	I	41.82	143.91	13	2.2E+16	28	3.1E+21	8.3	67	74	1.4E+16	1.4E+16	1.8E+21	8.1	-5.1	7.9	
2003.09.27 11:33	Siberia	S	50.04	87.93	1	5.1E+15	15	9.4E+19	7.2	12	68	5.7E+14	5.7E+14	4.8E+20	7.7	-4.9	7.4	
2003.12.26 01:56	S Iran	S	29	58.31	10	6.1E+14	15	9.3E+18	6.6	10	31	3.2E+13	3.2E+14	3.5E+19	7.0	-5.0	6.7	
2004.12.23 14:59	Macquarie	S	-50.15	160.37	-	5.2E+16	28	1.6E+21	8.1	53	59	8.3E+15	8.3E+16	3.1E+21	8.3	-4.6	7.8	
2004.12.26 00:58	Sumatra-Andaman	I	-3.3	95.98	39	1.4E+17	29	4.0E+22	9.0	190	420	1.4E+17	1.4E+17	7.7E+22	9.2	-5.7	8.1	
2005.03.28 16:09	N Sumatra	I	2.09	97.11	-	6.7E+16	30	1.1E+22	8.6	99	94	5.0E+16	5.0E+16	4.8E+21	8.4	-5.0	8.2	
2005.06.13 22:44	Chile	W	-19.99	-69.12	115	5.4E+15	95	5.1E+20	7.7	36	53	1.6E+16	1.6E+16	1.1E+21	8.0	-4.8	7.6	
2005.07.24 15:42	Nicobar	S	7.92	92.19	16	1.2E+16	12	8.8E+19	7.2	25	39	8.4E+14	8.4E+15	2.5E+20	7.5	-4.5	7.2	
2005.08.16 02:46	Honshu	I	38.28	142.98	36	3.8E+14	37	7.4E+19	7.2	20	53	3.2E+14	3.2E+14	1.4E+20	7.4	-5.7	7.4	
2005.10.08 01:30	Pakistan	R	34.54	73.59	26	3.1E+15	12	2.9E+20	7.6	18	54	2.8E+15	2.8E+15	2.4E+20	7.5	-4.9	7.6	
2006.02.22 22:19	Moanbaque	N	-21.32	33.58	11	4.4E+14	12	4.5E+19	7.0	16	26	6.4E+14	6.4E+14	3.7E+19	7.0	-4.8	7.3	
2006.05.16 10:39	Kermadec	D	31.78	179.31	151	-	155	1.7E+20	7.4	25	25	5.6E+15	5.6E+15	2.2E+20	7.5	-4.6	7.5	
2006.07.17 08:19	Java	I	-9.25	107.41	34	2.2E+14	20	4.9E+20	7.7	100	157	6.6E+14	6.6E+14	7.1E+20	7.8	-4.0	7.2	

\* Earthquake type: I - interpolate thrust; T - tsunami earthquake; W - downward; P - intraplate; D - deep; S - strike-slip crustal; R - reverse-faulting crustal; N - normal-faulting crustal. 2 x CMT half-duration.

### Table 1. Events used in this study.

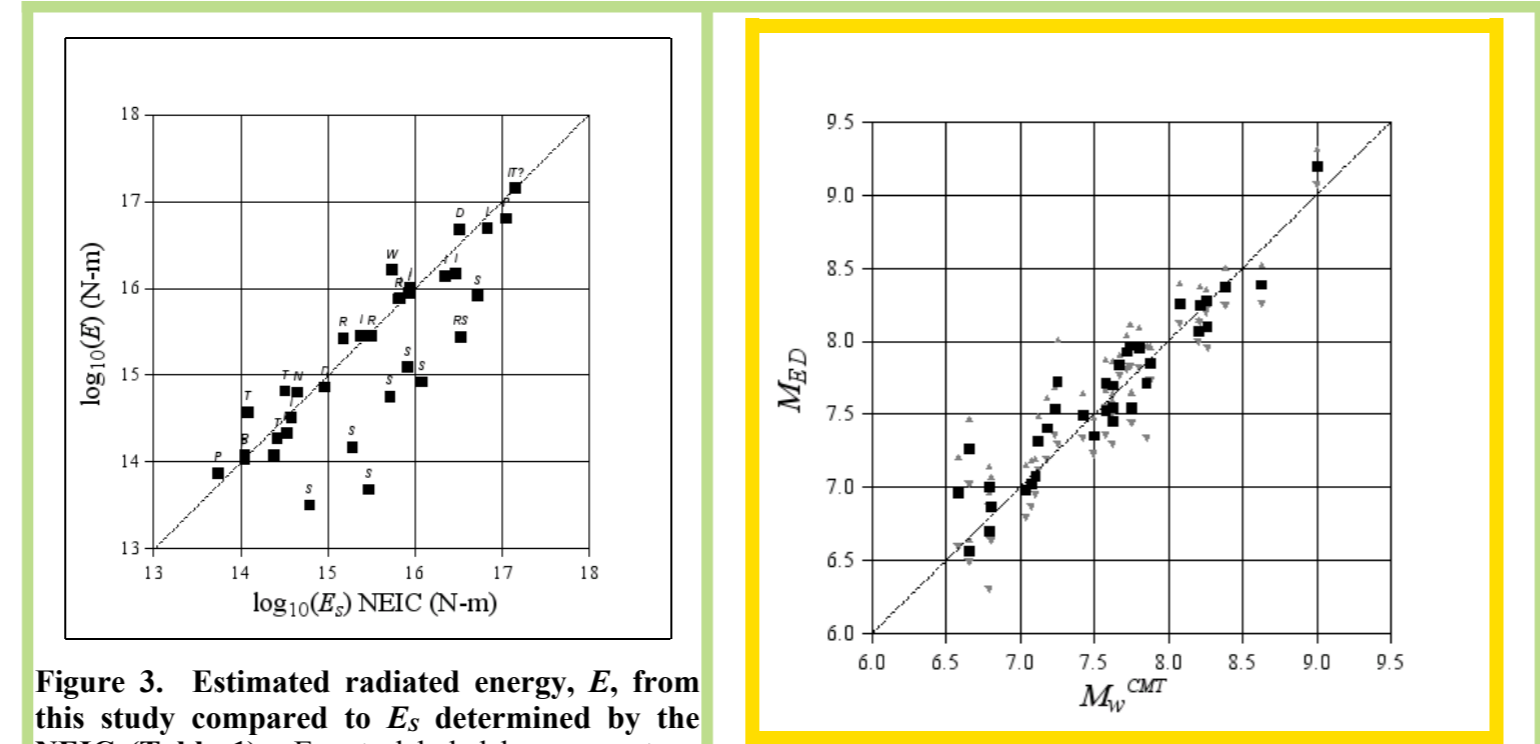


Figure 3. Estimated radiated energy,  $E$ , from this study compared to  $E_s$  determined by the NEIC (Table 1). Events labeled by source type (see Table 1).

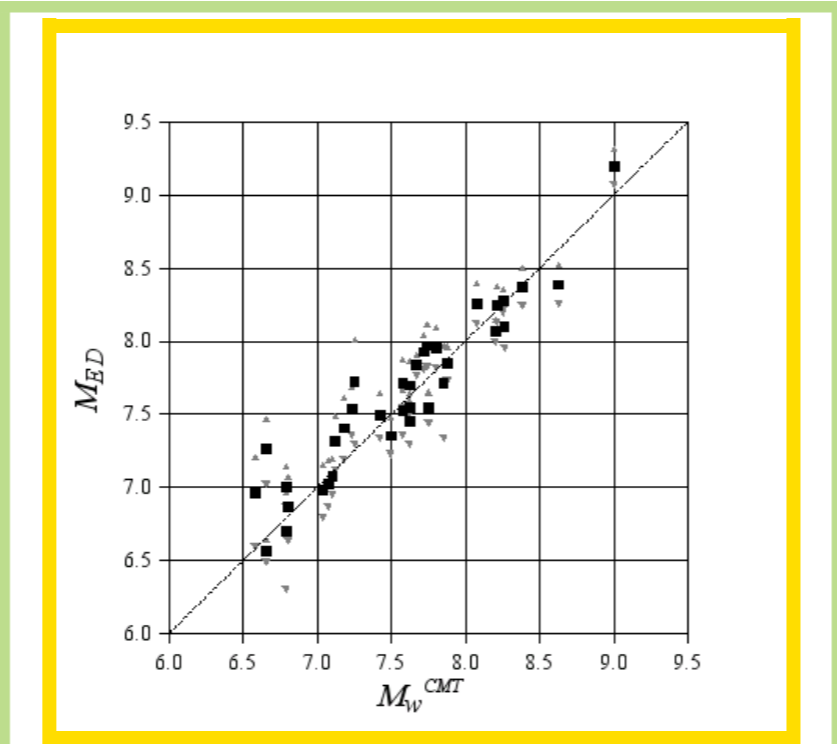


Figure 4. Energy-duration magnitude  $M_{ED}$  from this study compared to CMT magnitude  $M_{CMT}$ . Bounds on  $M_{ED}$  are indicated by grey triangles.

### Energy estimations

Table 1 and Fig. 3 show that our values,  $E$ , for radiated energy, excluding strike-slip events, agree well with the radiated energy values,  $E_s$ , determined by the NEIC using the procedure of Boatwright and Choy (1986). For all the studied strike-slip earthquakes, however, we obtain  $E$  values that are less than those of NEIC by a factor of about 10, on average (Table 1, Fig. 5). All of these events have steeply dipping nodal axes close to which teleseismic P rays depart from the source; to allow meaningful comparison of our results with CMT values, we increase our radiated seismic energy values,  $E$ , by a factor of 10 for strike slip events to approximately account for this energy underestimate (Table 1,  $E$  corrected).

### Duration estimations

A comparison between our estimates of source duration  $T_0$  and the CMT duration (i.e., 2 x the CMT half-duration; Table 1) shows that our  $T_0$  values are on average about twice the CMT duration. Our mean value of  $T_0=420$ s and 33% energy peak value of  $T_0=473$ s for 2004.12.26 Sumatra-Andaman are closer than the CMT duration of 190s to the inferred value for the full, co-seismic rupture of about 450-600s for this event (e.g., Lomax, 2005; Ammon, et al., 2