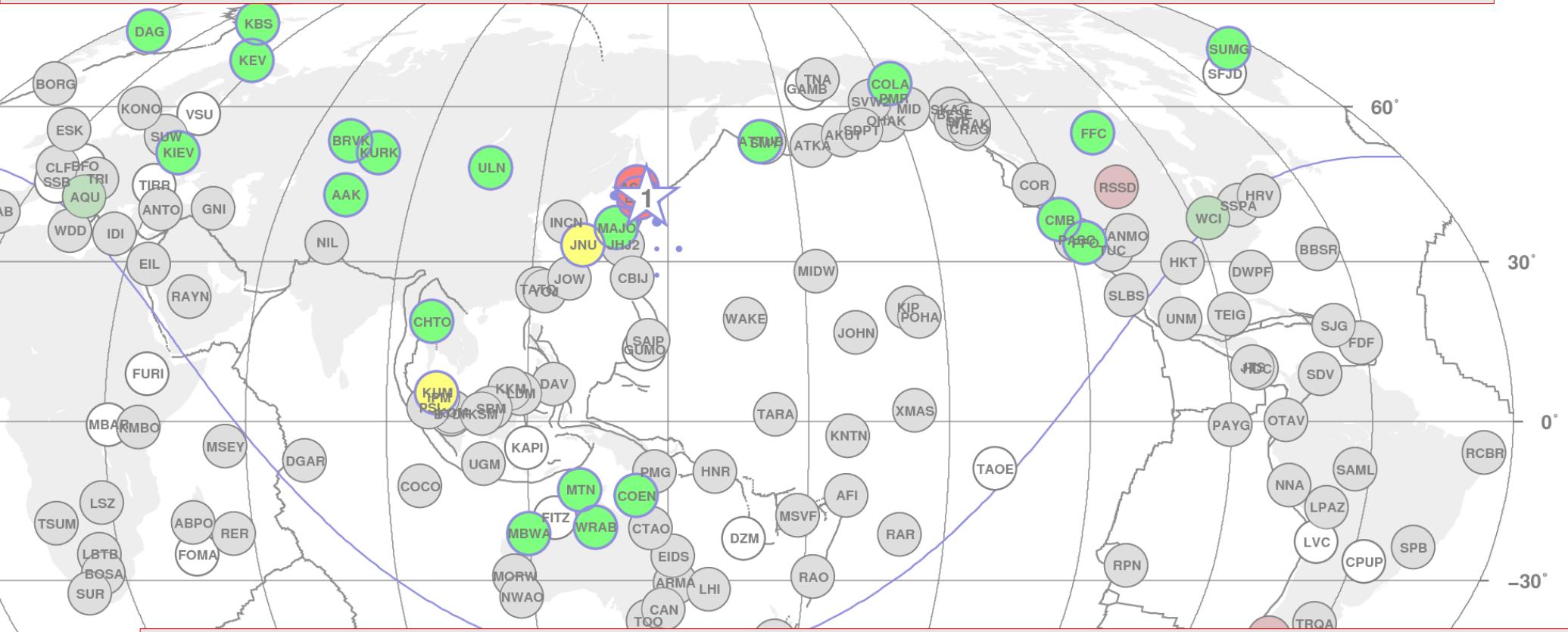


Real-Time Earthquake Location



Anthony Lomax
ALomax Scientific, Mouans-Sartoux, France

Alberto Michelini
Istituto Nazionale di Geofisica e Vulcanologia, Roma, Italy

Andrew Curtis
ECOSSE, Grant Institute of GeoSciences, University of Edinburgh, Edinburgh, United Kingdom

Outline:

Introduction

- 1. Phase picking, phase association and event detection**
- 2. Earthquake location at local, regional and teleseismic distances: Probabilistic, global-search earthquake location**
- 3. New perspectives in observatory analysis: Illustrative examples of global-search earthquake location**

More information: <http://alomax.net/science.html>

Anthony Lomax - ALomax Scientific, Mouans-Sartoux, France - anthony@alomax.net, www.alomax.net

Real-Time Earthquake Location

Introduction – Earthquake location

Anthony Lomax

ALomax Scientific, Mouans-Sartoux, France

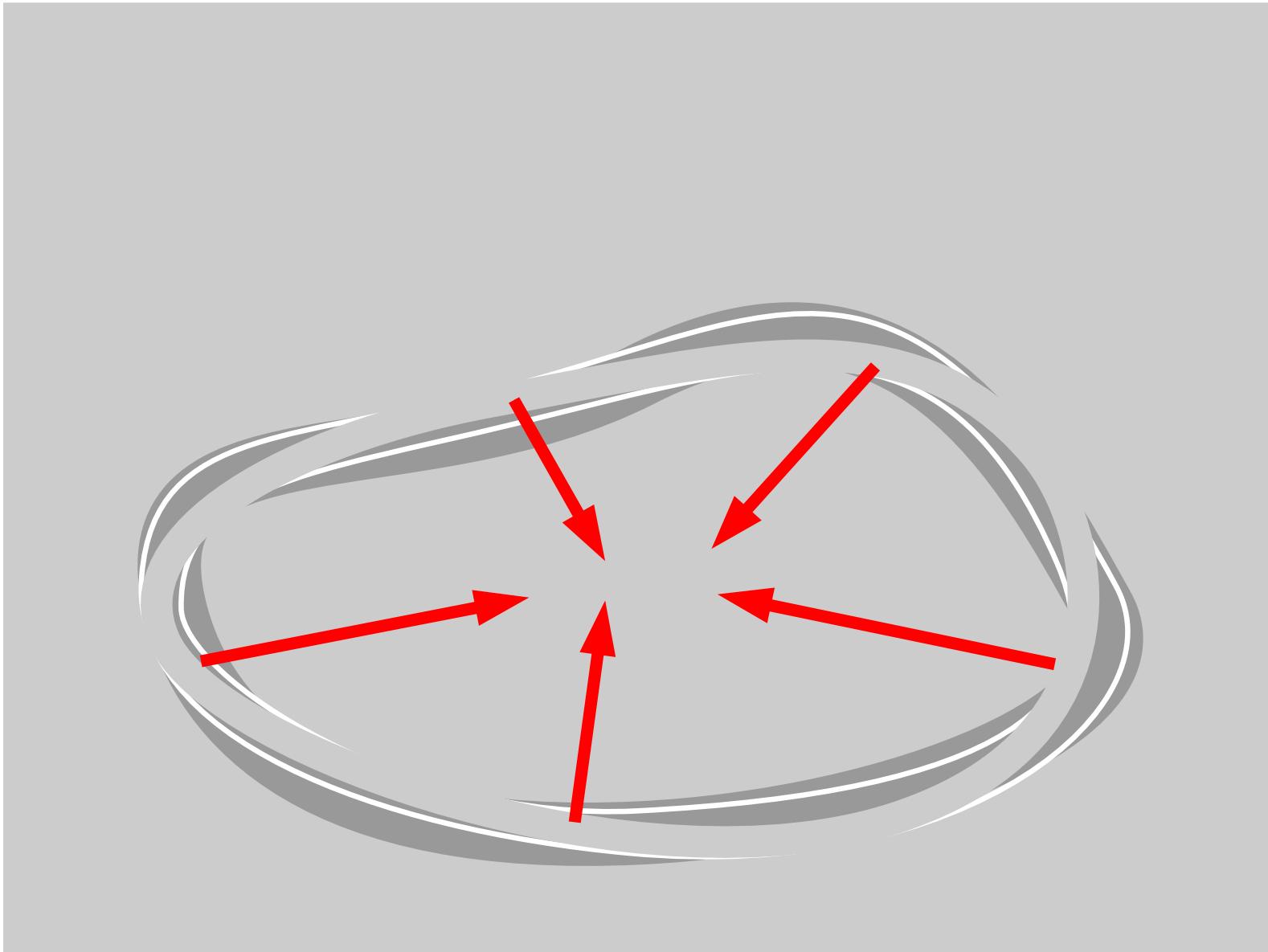
Alberto Michelini

Istituto Nazionale di Geofisica e Vulcanologia, Roma, Italy

Andrew Curtis

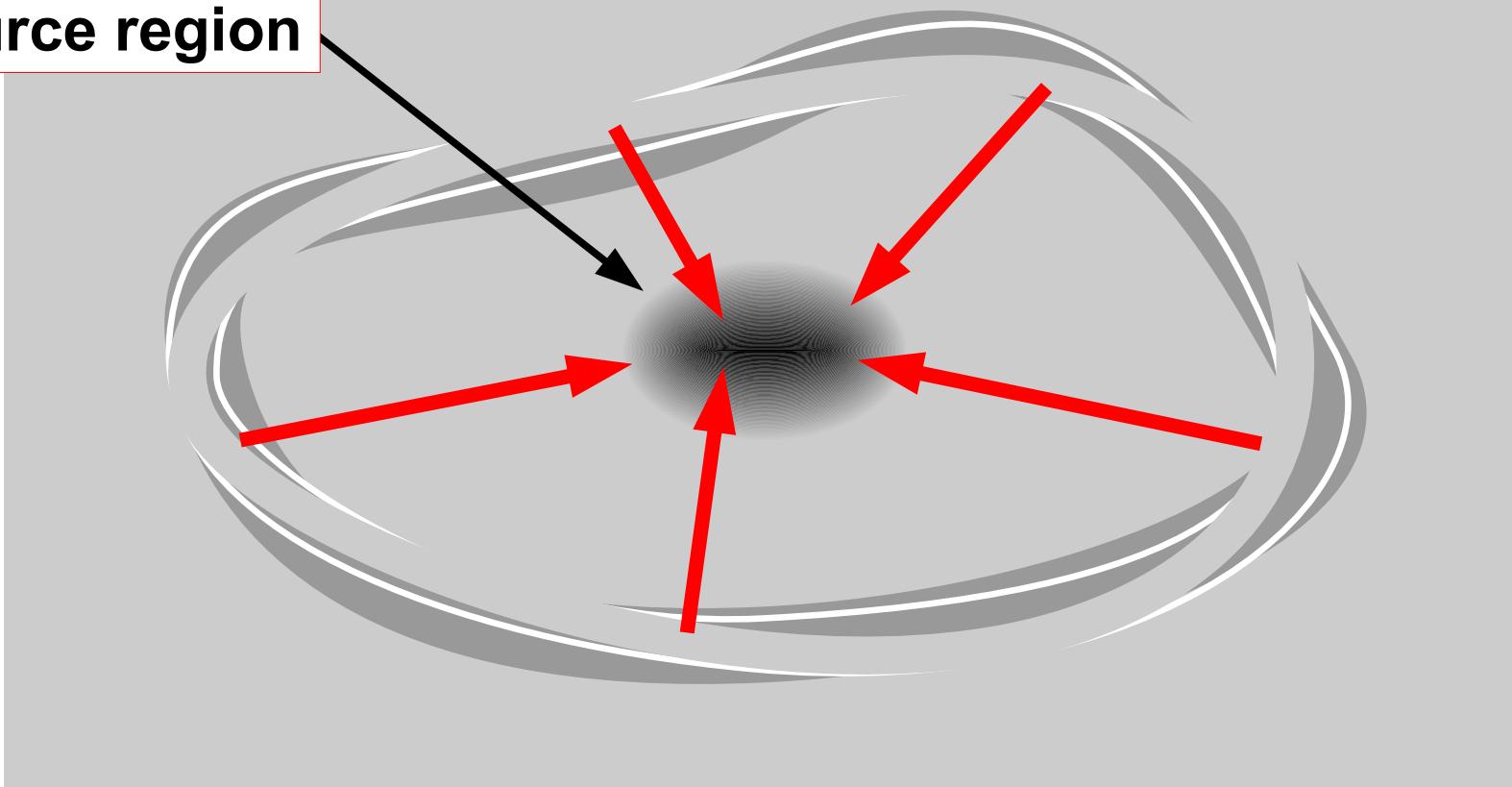
ECOSSE, Grant Institute of GeoSciences, University of Edinburgh, Edinburgh, United Kingdom

Earthquake Location



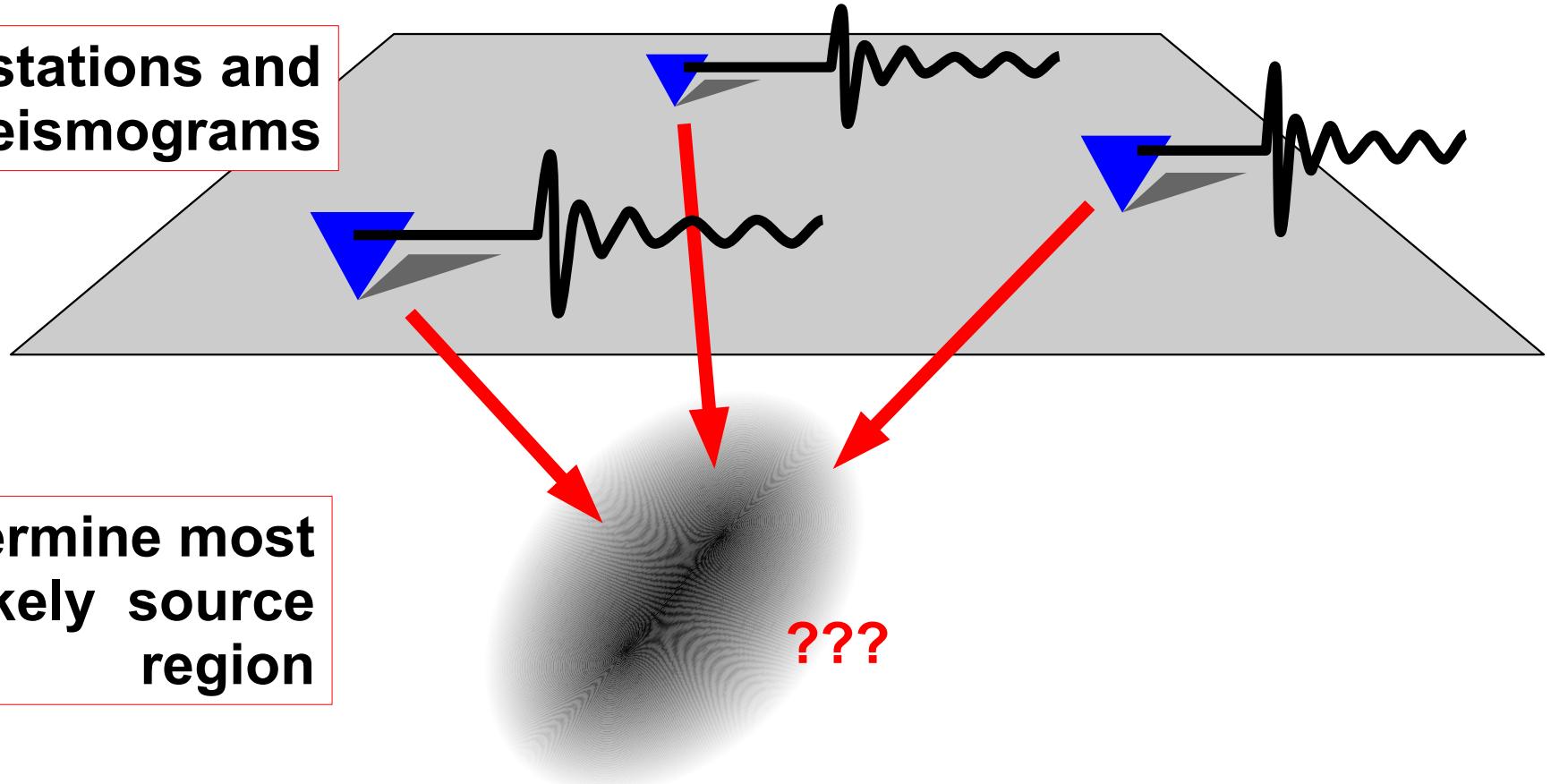
Earthquake Location

most likely
source region



Earthquake Location

stations and seismograms



determine most likely source region

Real-Time Earthquake Location

1. Phase picking, phase association and event detection

Anthony Lomax

ALomax Scientific, Mouans-Sartoux, France

Alberto Michelini

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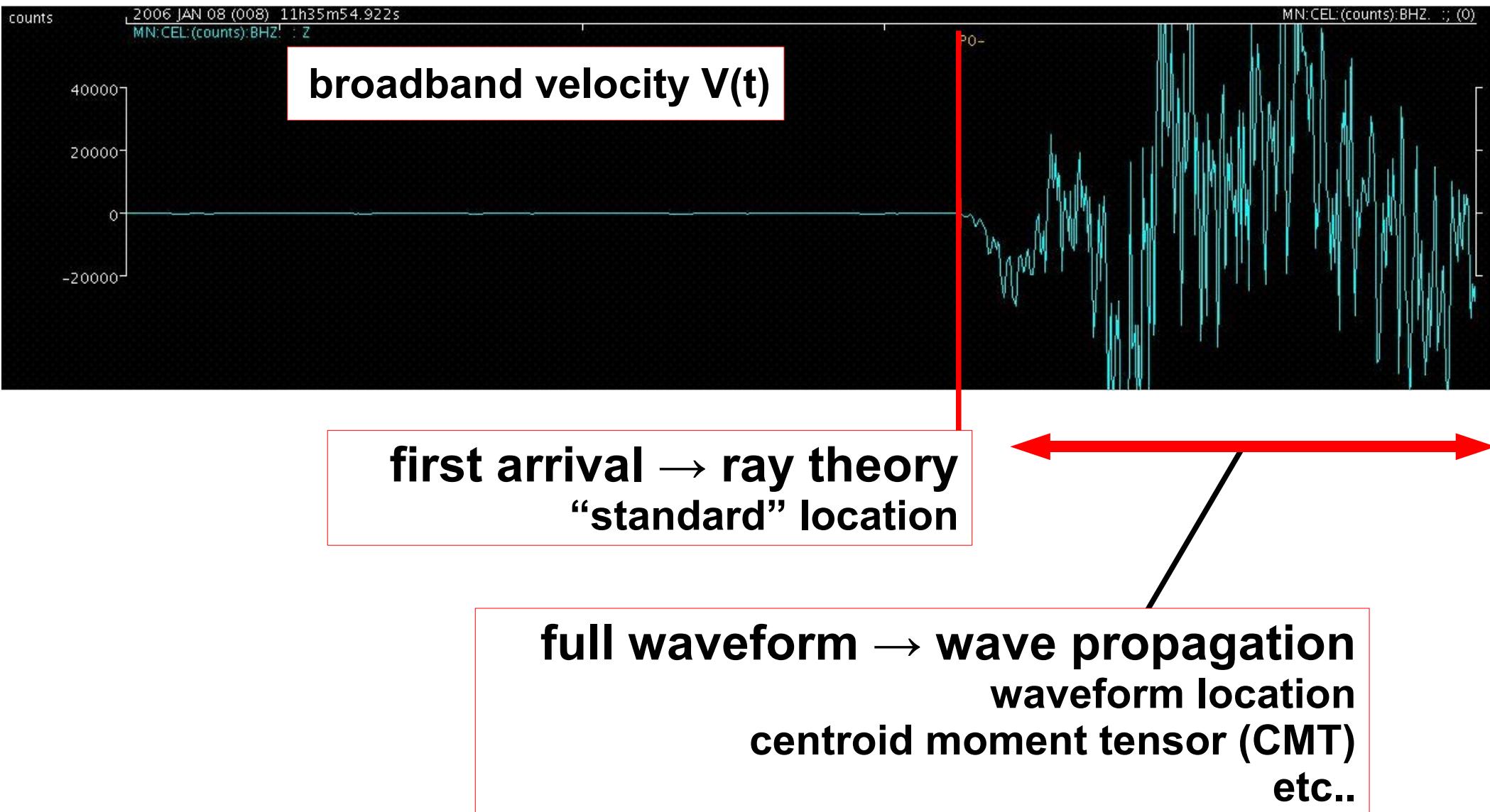
ECOSSE, Grant Institute of GeoSciences, University of Edinburgh, Edinburgh, United Kingdom

Real-Time Earthquake Location

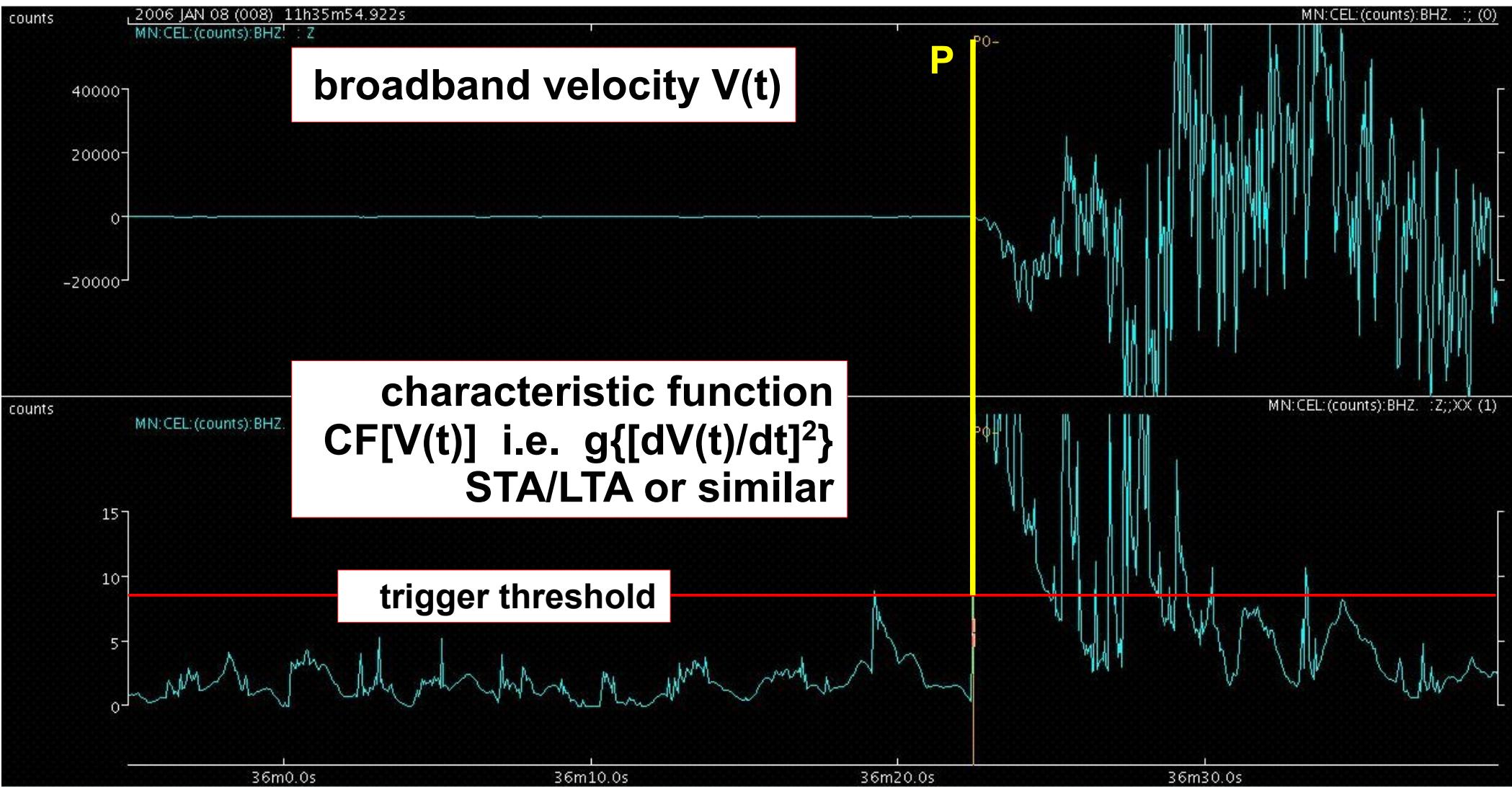
1. Phase picking, phase association and event detection

Phase picking

Phase picking – theory

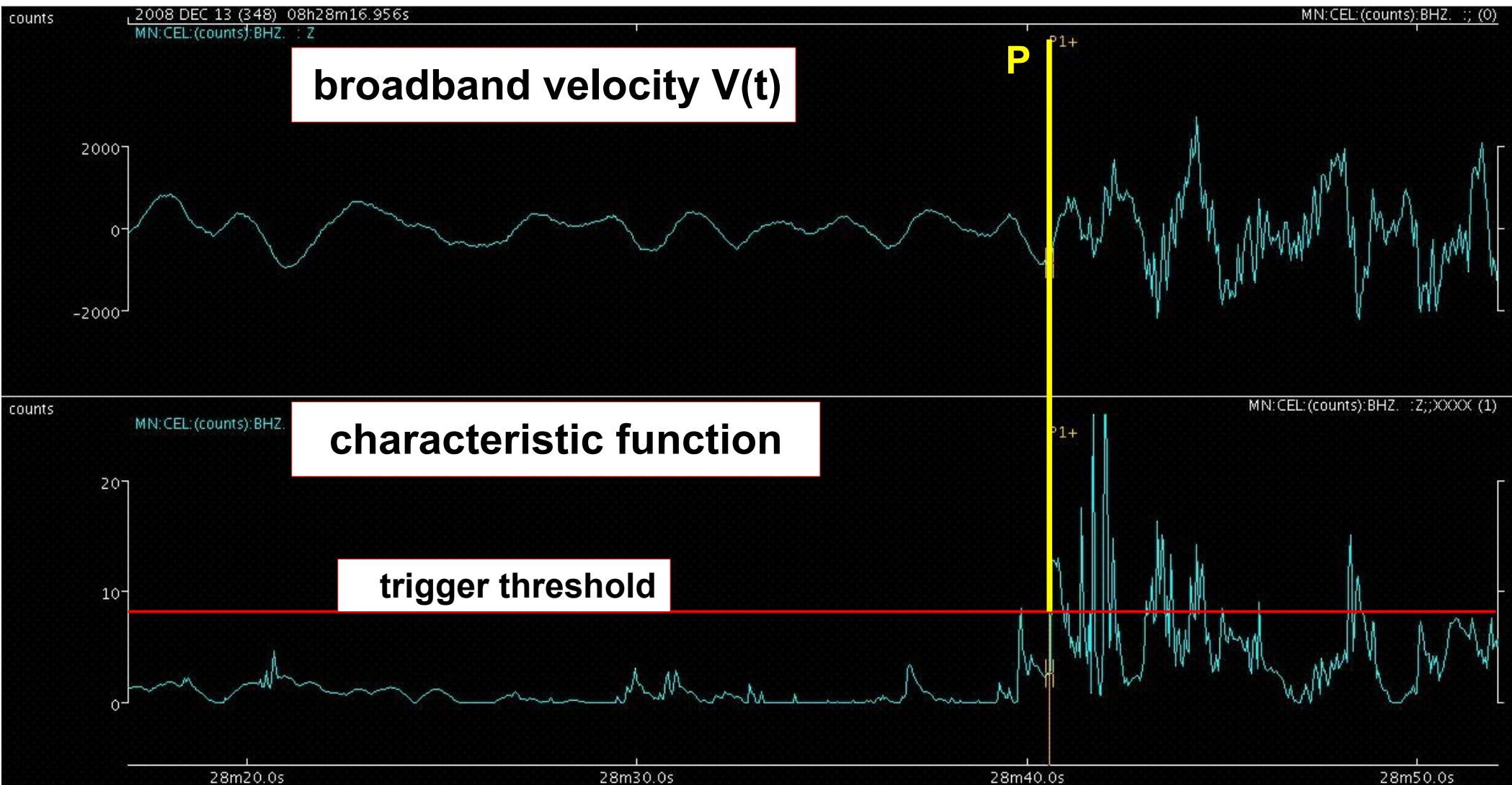


Phase picking – Automatic pickers - algorithm

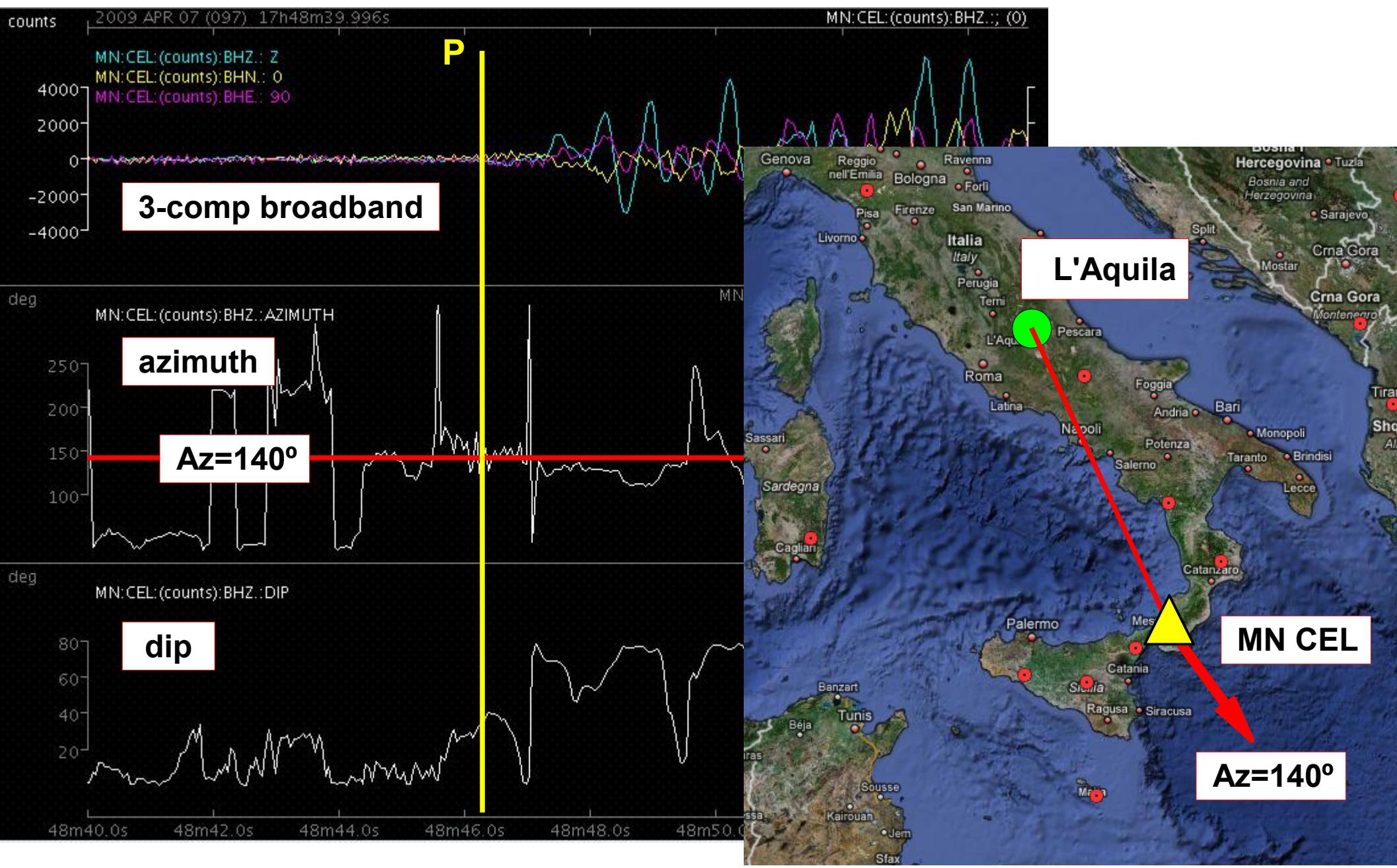


e.g. Allen, R.V. (1982) - Baer, M., and U. Kradolfer (1987) - Sleeman, R., and T. van Eck (1999) - etc...

Phase picking – Automatic pickers – noisy signal

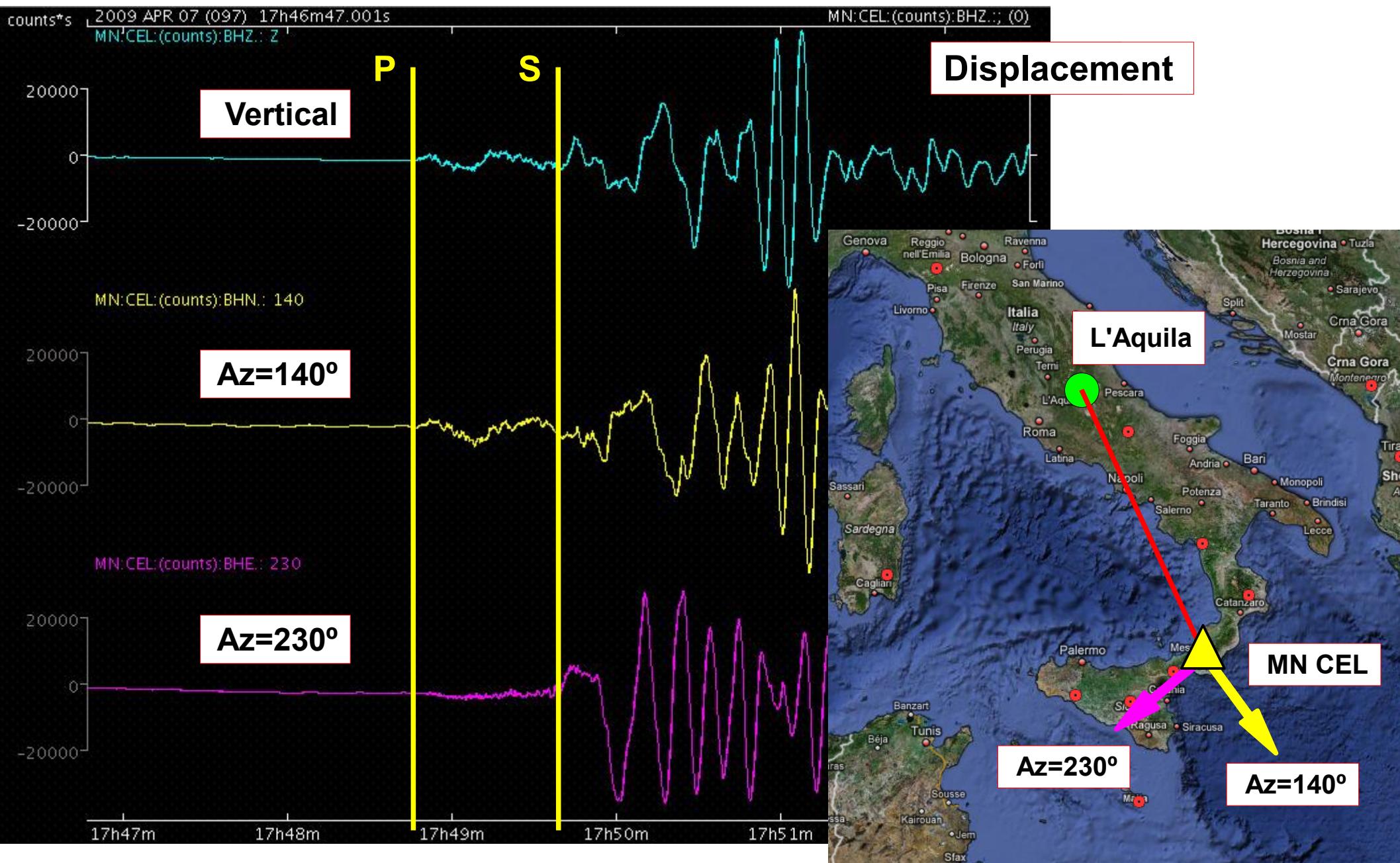


Phase picking – 3-component broadband – polarisation



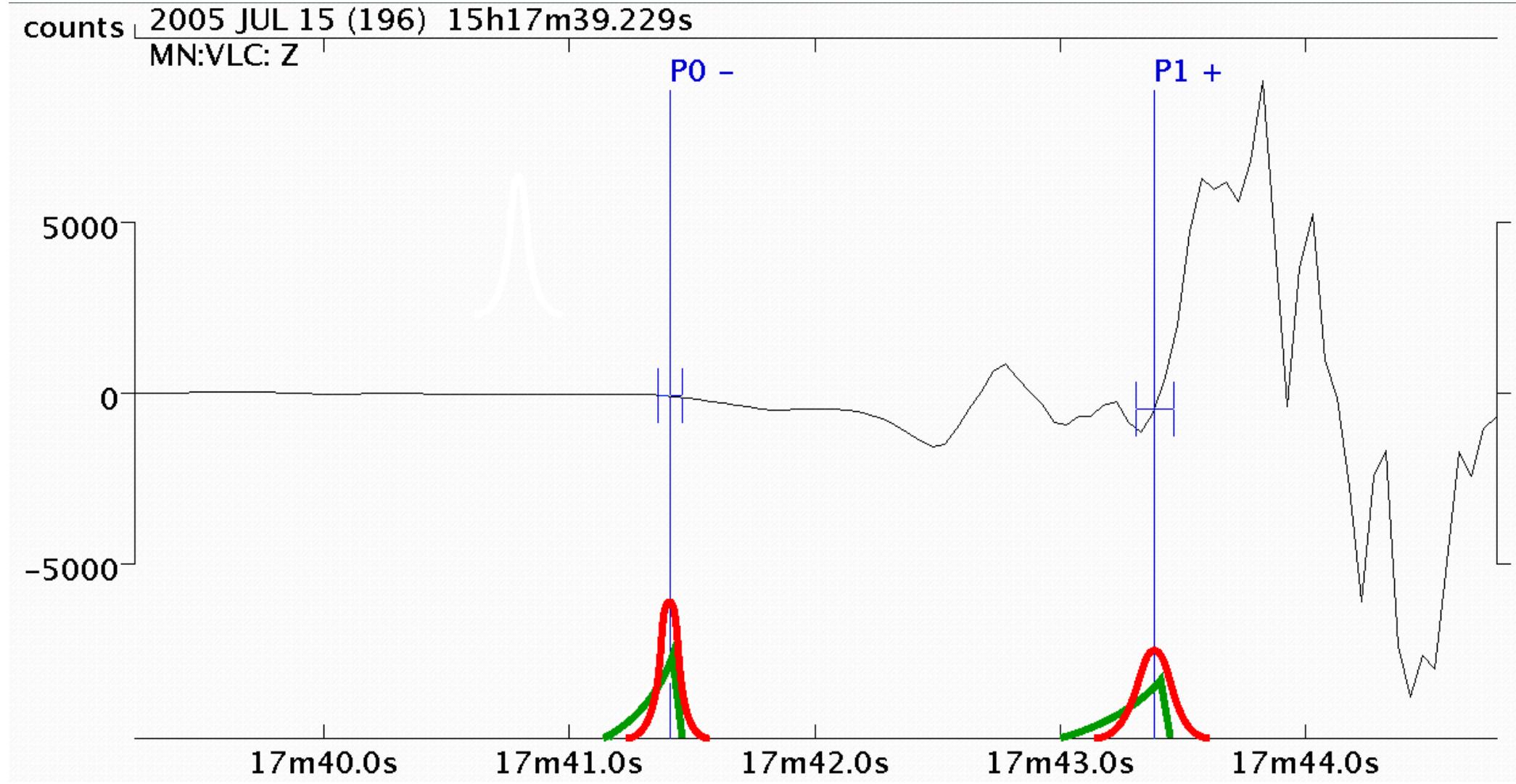
e.g. Magotra, N., N.Ahmed, and E.Chael (1987) - Cichowicz, A. (1993) - Oye, V. and W.L. Ellsworth (2005) - etc...

Phase picking – 3-component broadband



e.g. Magotra, N., N.Ahmed, and E.Chael (1987) - Cichowicz, A. (1993) - Oye, V. and W.L. Ellsworth (2005) - etc...

Phase picking - Arrival times and pick uncertainty

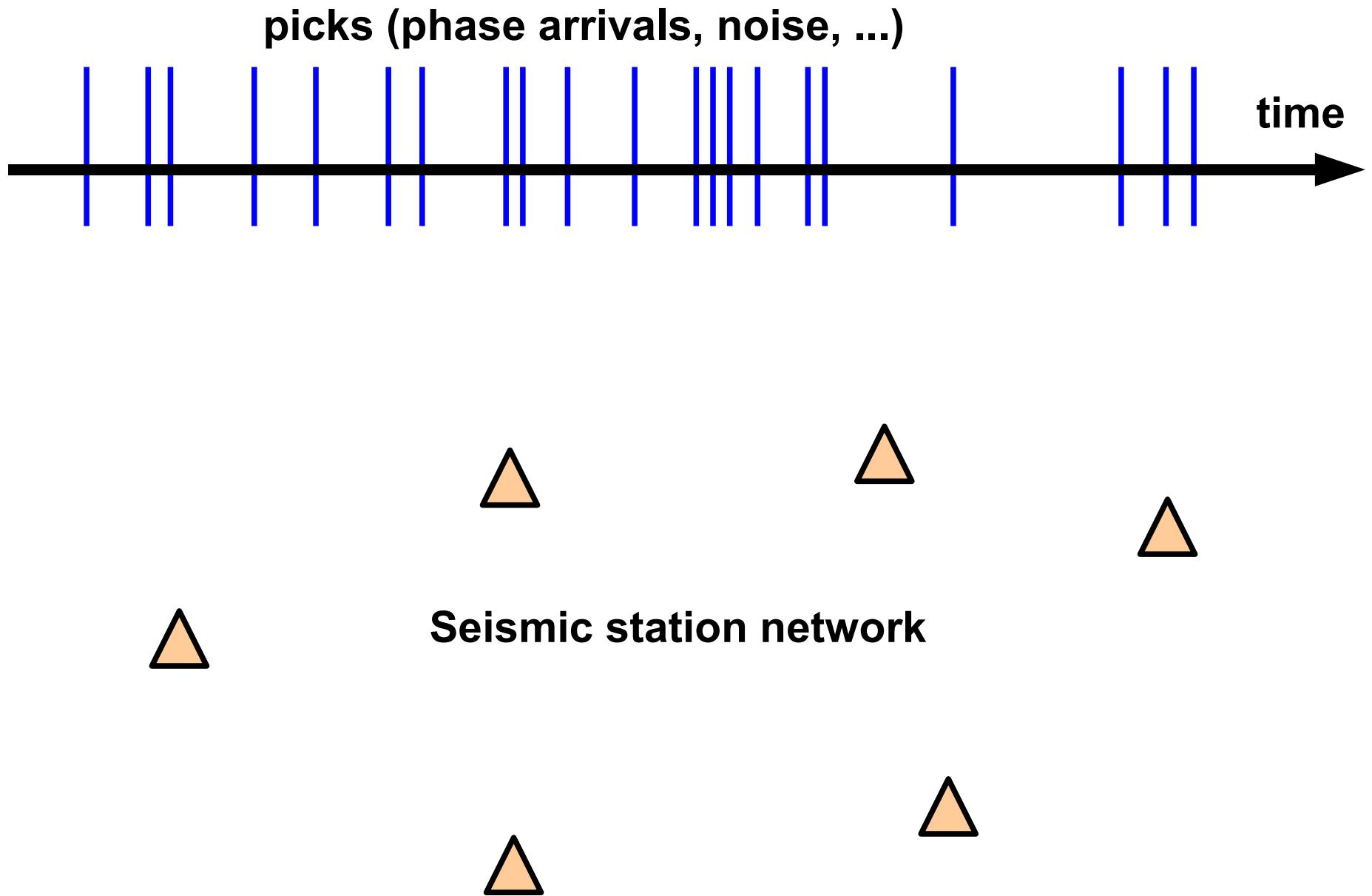


e.g. Tarantola, A. (1987) - refs in Lomax, A., A. Michelini, A. Curtis (2009) - etc...

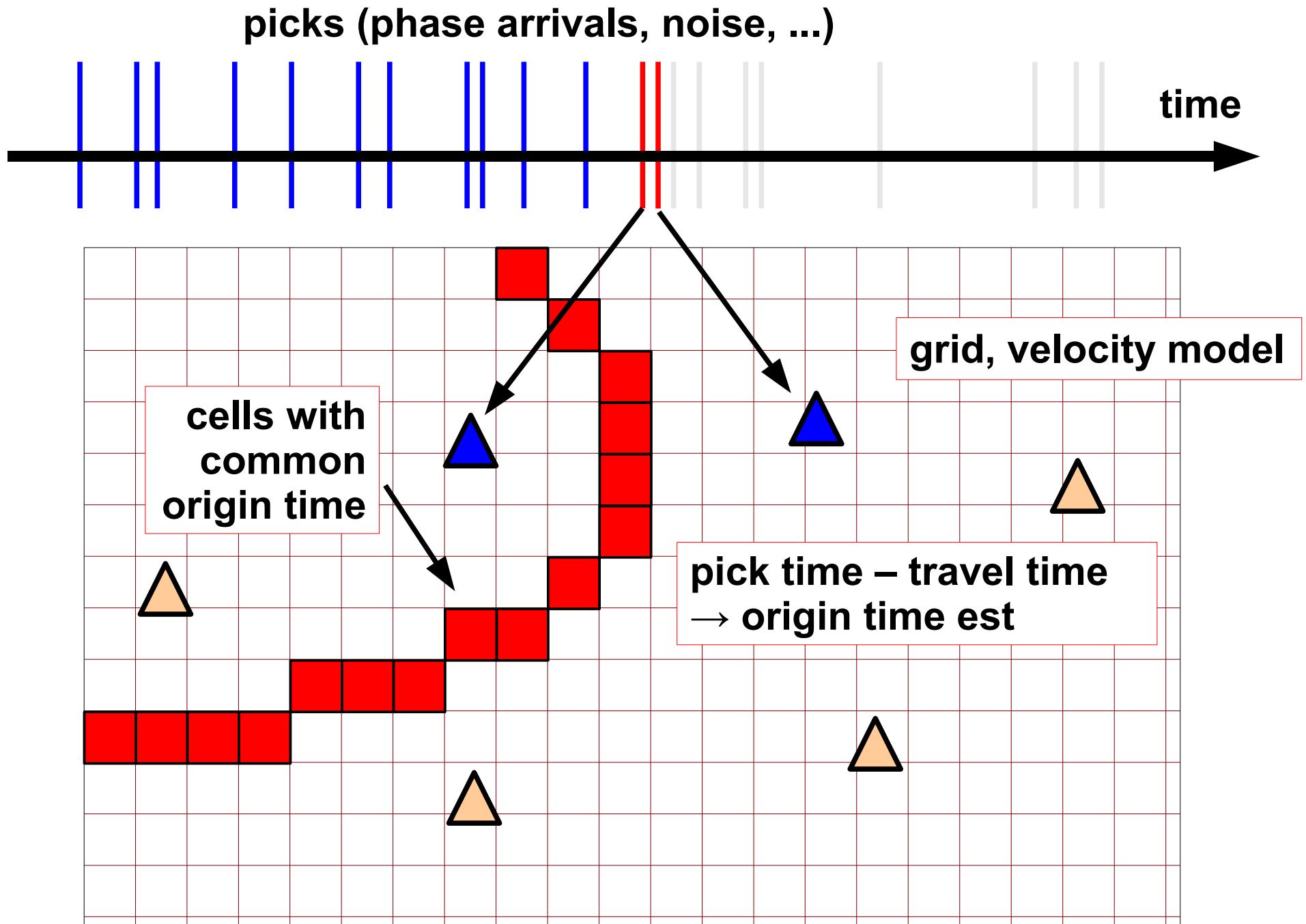
1. Phase picking, phase association and event detection

Phase association and event detection

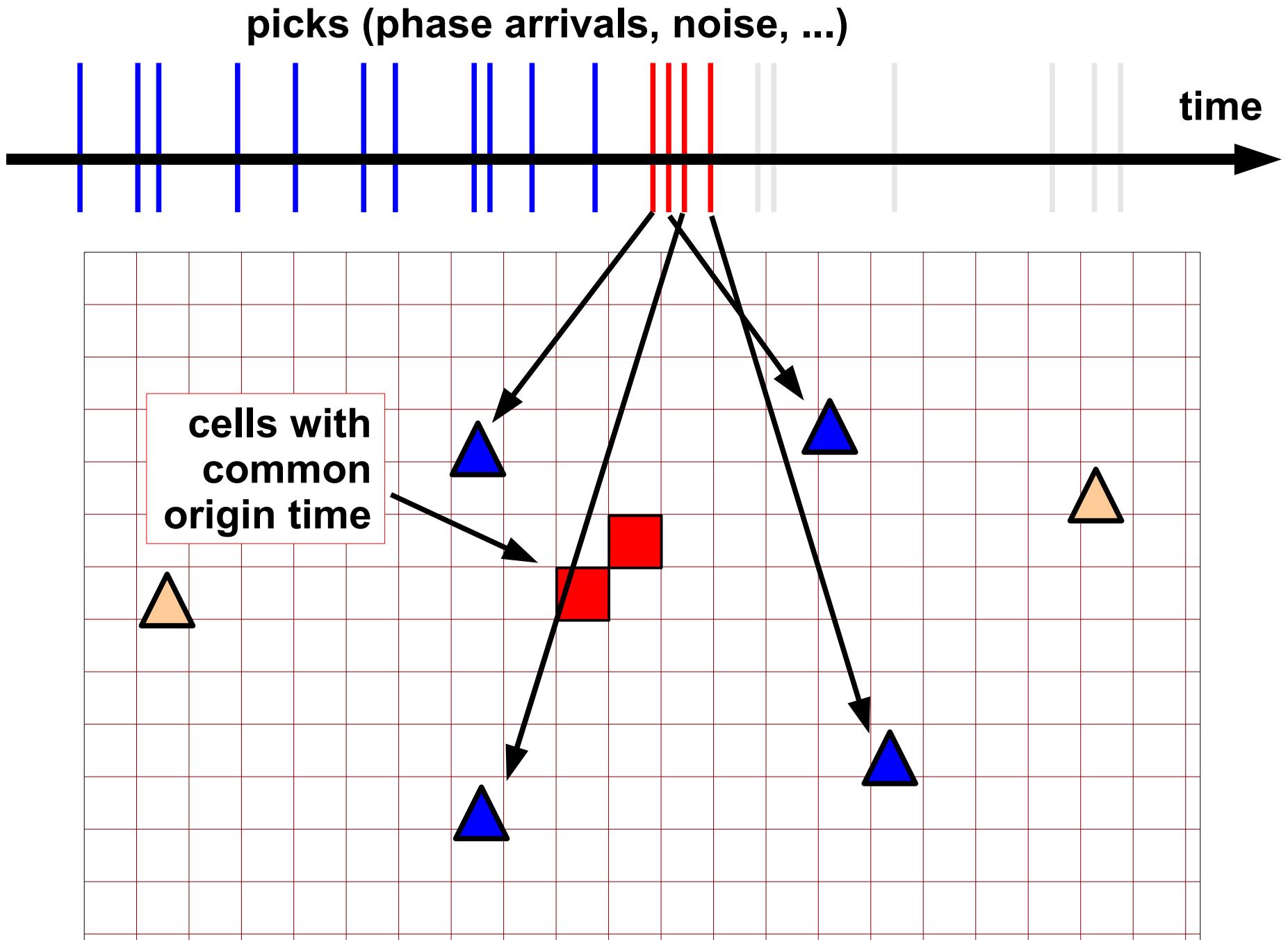
Phase association and event detection



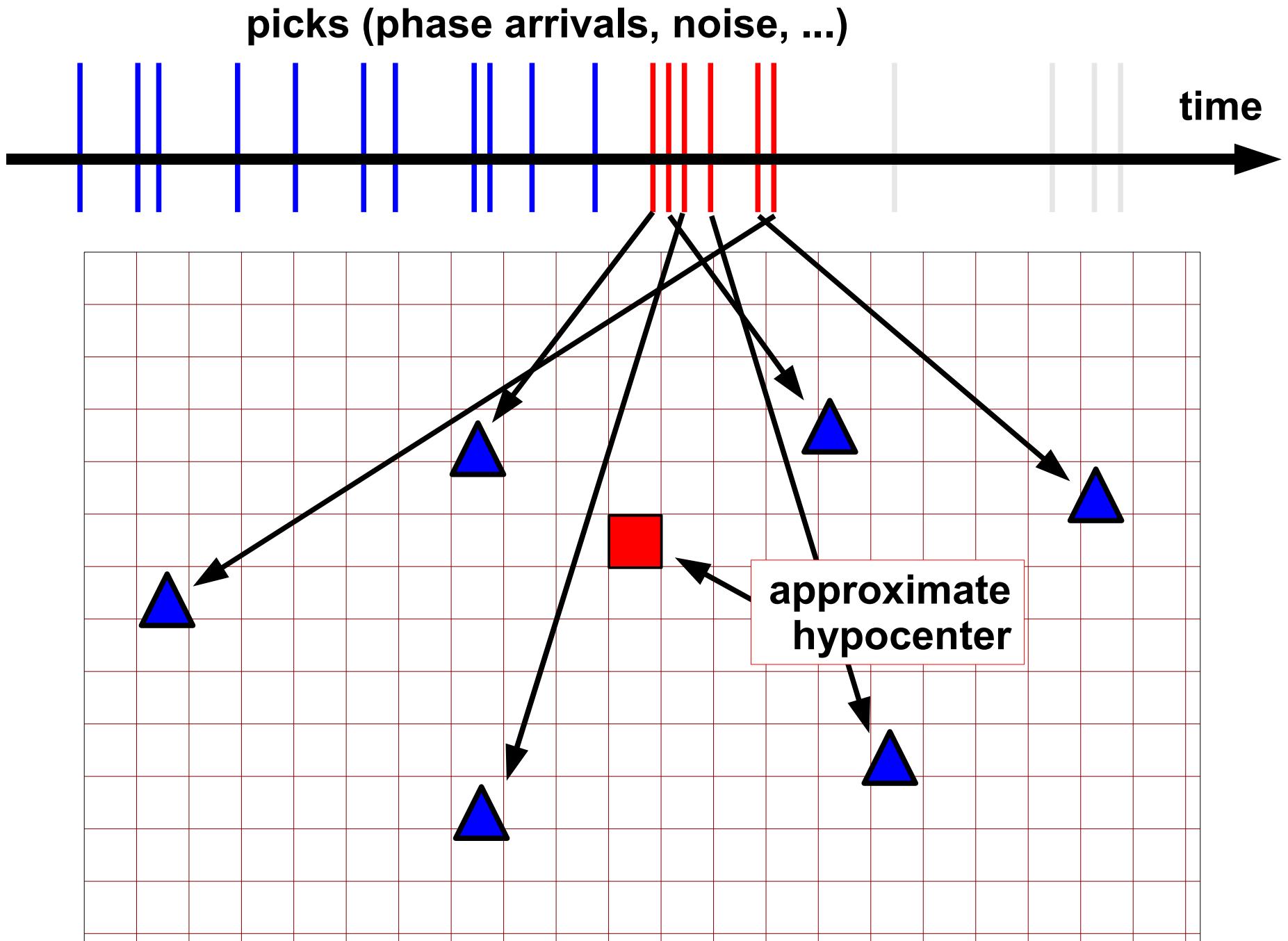
Phase association and event detection



Phase association and event detection



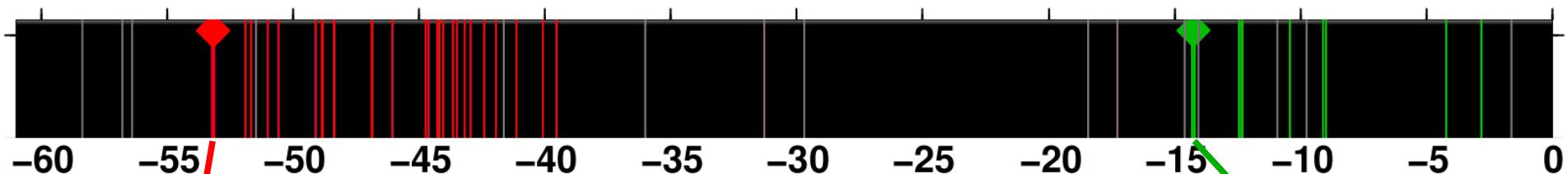
Phase association and event detection



Phase association and event detection

2009.04.15–17:39:39 UTC

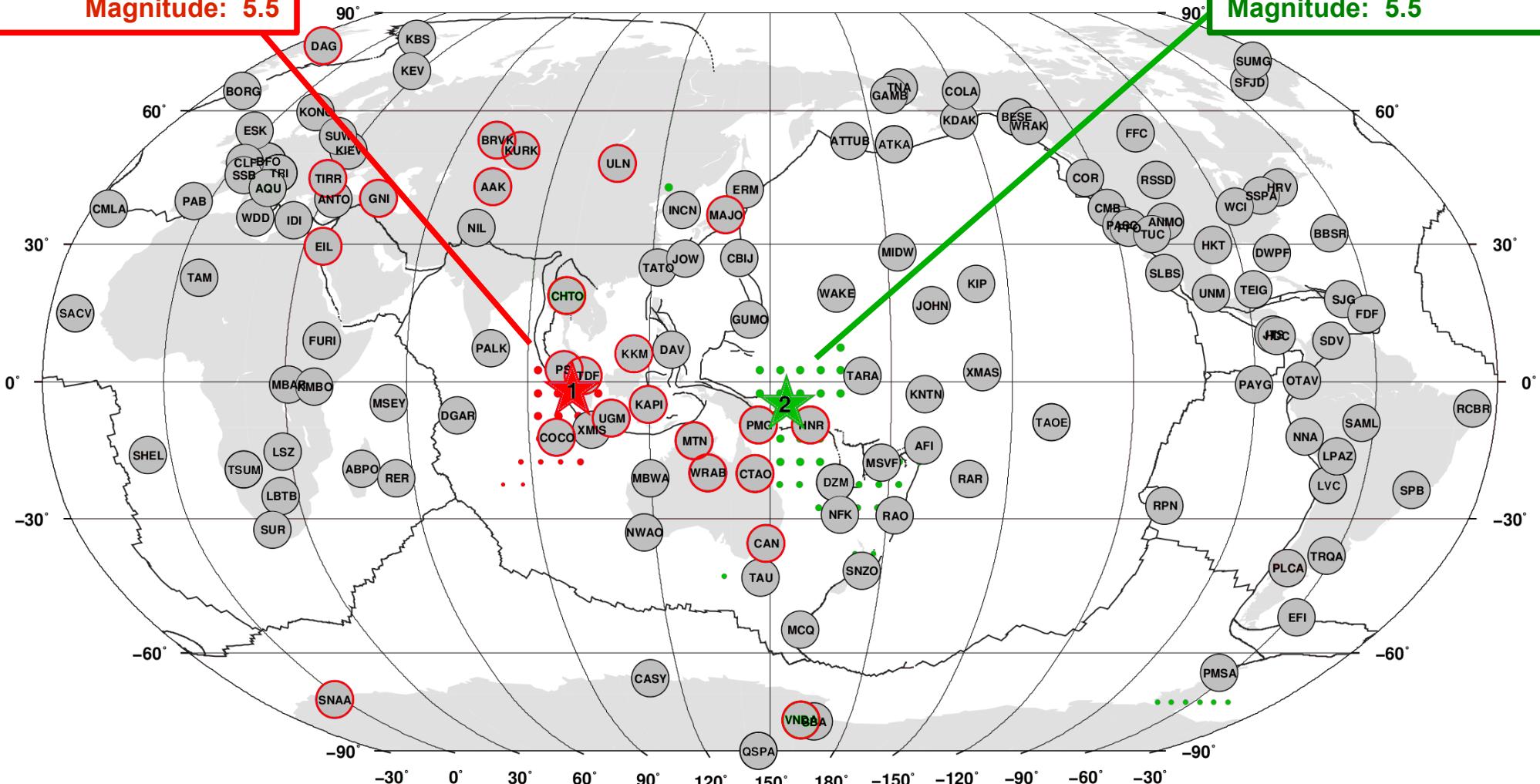
2009.04.15–18:40:40



Southern Sumatra
2009-04-15 17:47:27.9
Magnitude: 5.5

Solomon Islands
2009-04-15 18:26:39.5
Magnitude: 5.5

Time before last data (minutes)



Difficulties for picking, association, location

- **False picks (noise, signal problems, ...)**
- **Small, pre-cursor events (foreshocks, noise, ...)**
- **Simultaneous events**
- **Poor network geometry or station coverage around event**
- **...**

Real-Time Earthquake Location

2. Earthquake Location at local, regional and teleseismic distances: Probabilistic, global-search earthquake location

Anthony Lomax

ALomax Scientific, Mouans-Sartoux, France

Alberto Michelini

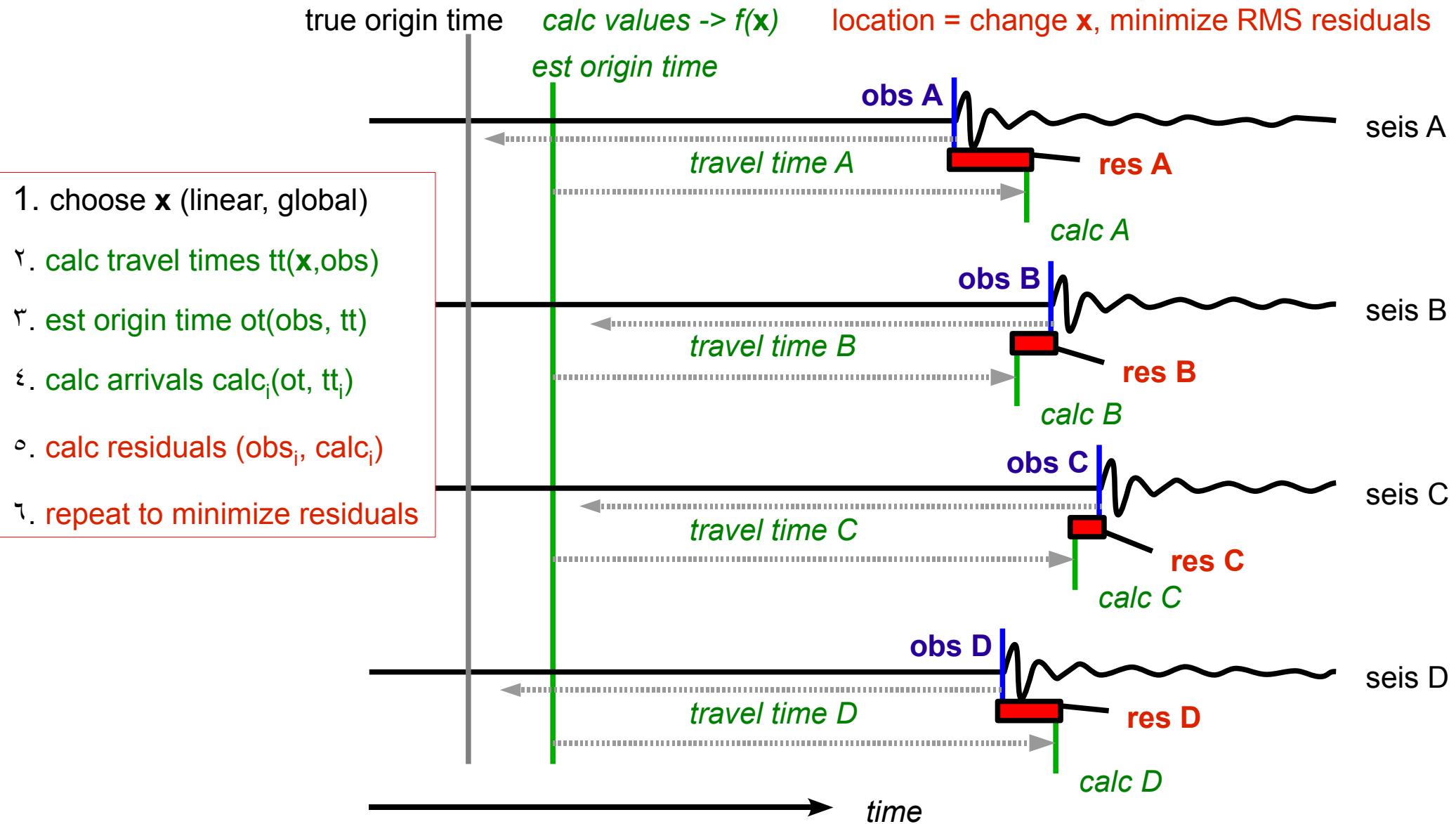
Istituto Nazionale di Geofisica e Vulcanologia, Roma, Italy

Andrew Curtis

ECOSSE, Grant Institute of GeoSciences, University of Edinburgh, Edinburgh, United Kingdom

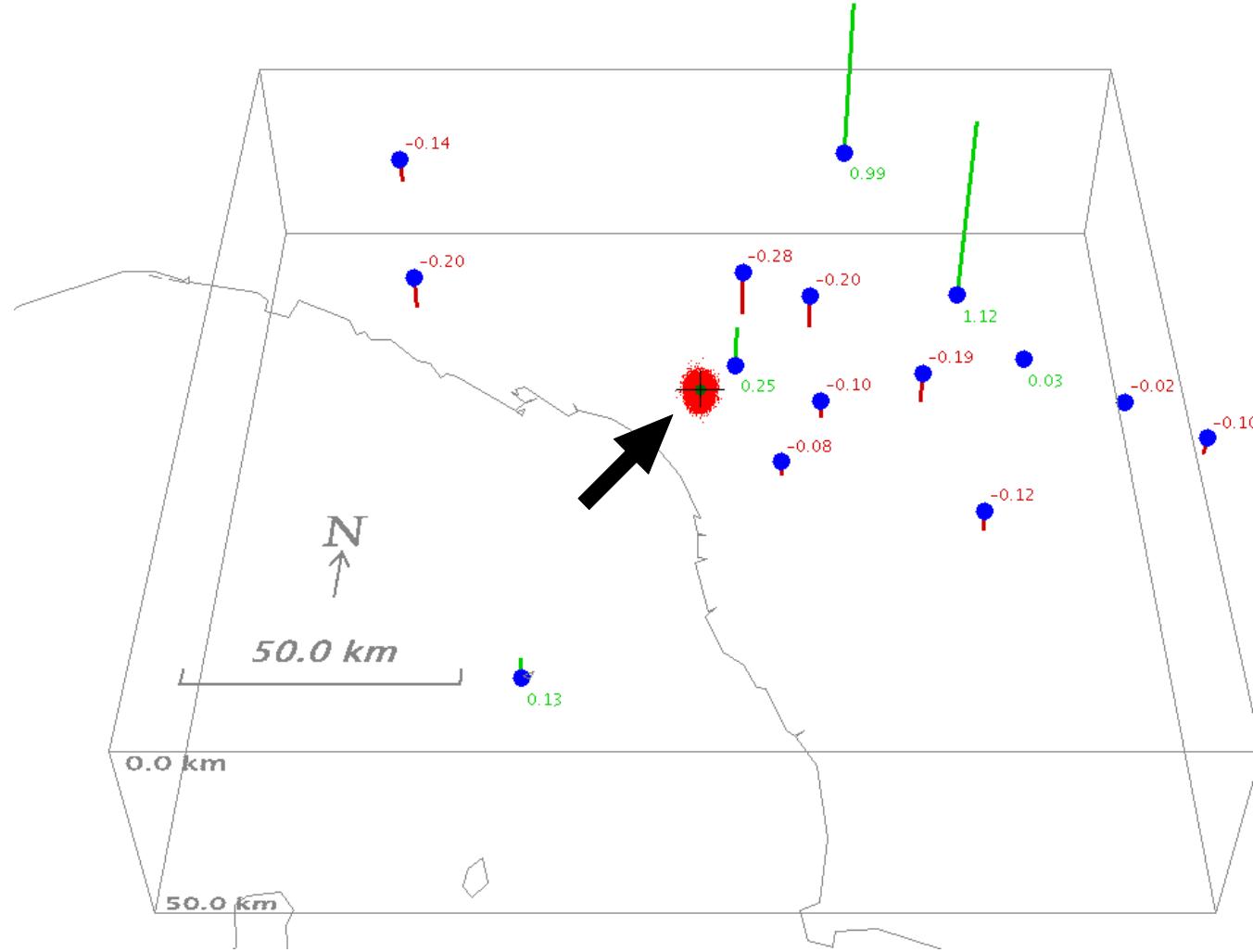
Real-Time Earthquake Location

basic least-squares location



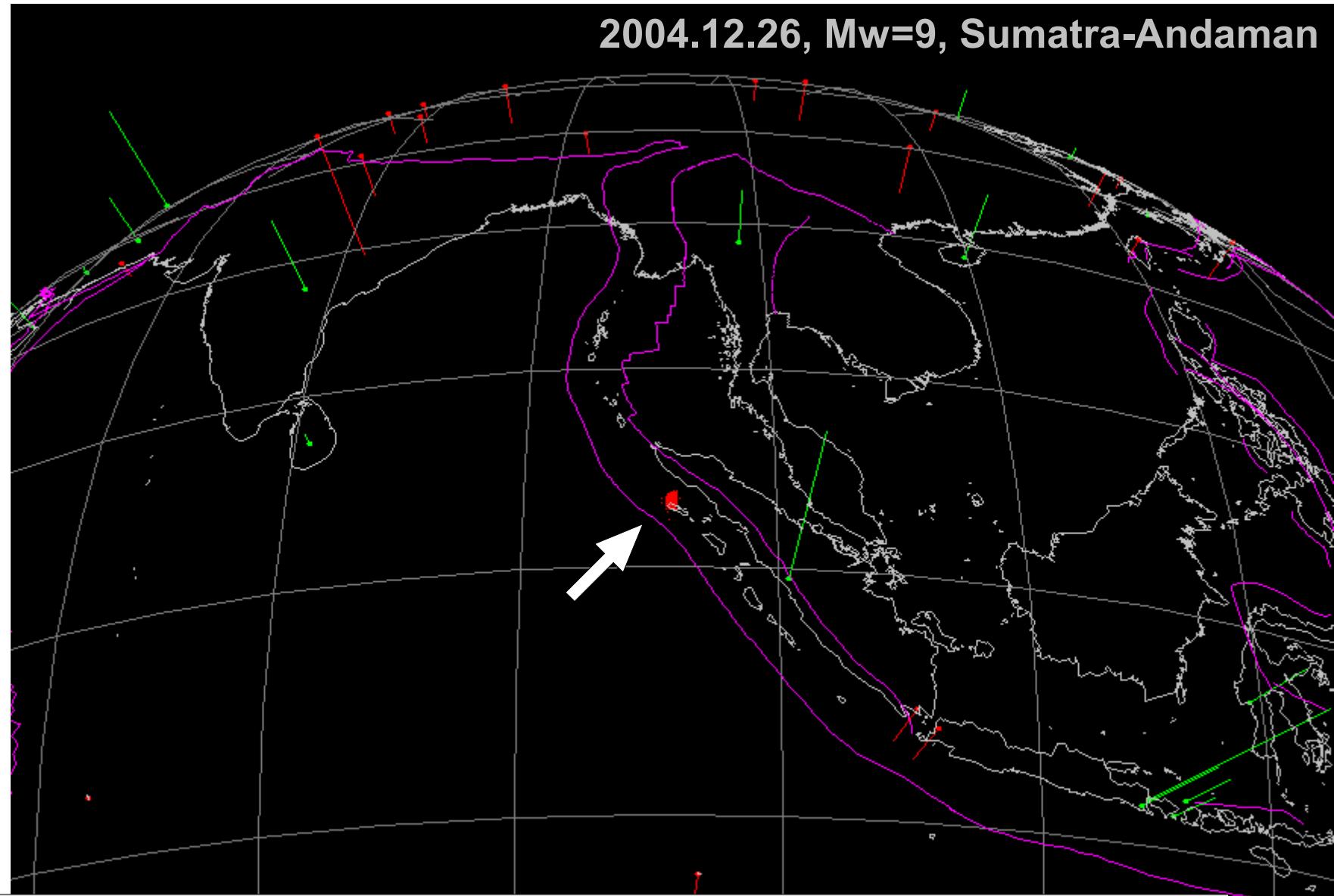
Real-Time Earthquake Location

basic least-squares location – local/regional – Cartesian coordinates



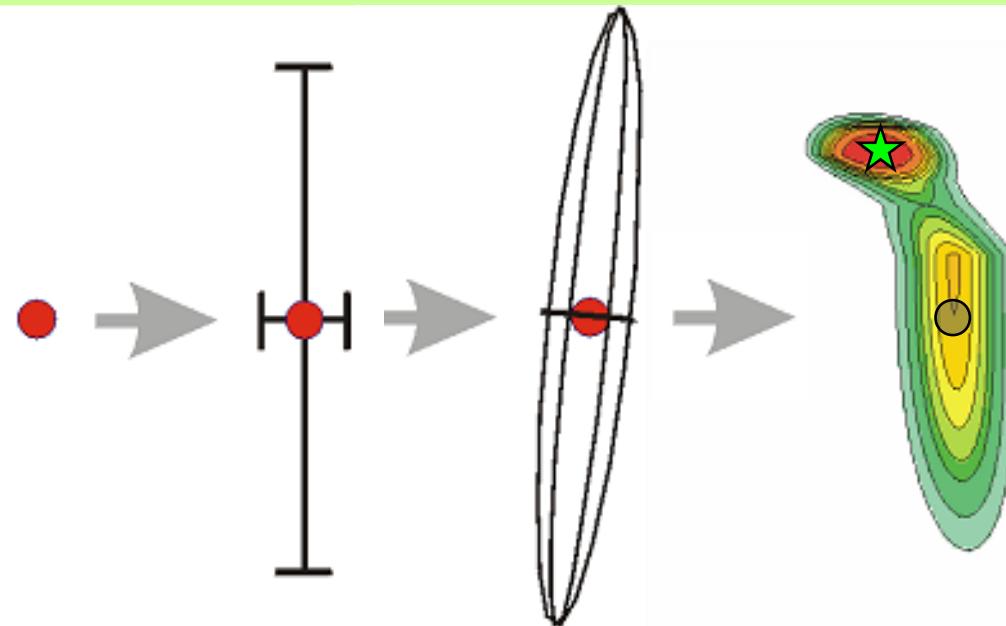
Real-Time Earthquake Location

basic least-squares location – teleseismic – spherical coordinates



e.g. Lahr, J.C. (1999) - Tarantola, A. (1987) – refs in Lomax, A., A. Michelini, A. Curtis (2009) - etc...

global methods



"optimal"
location

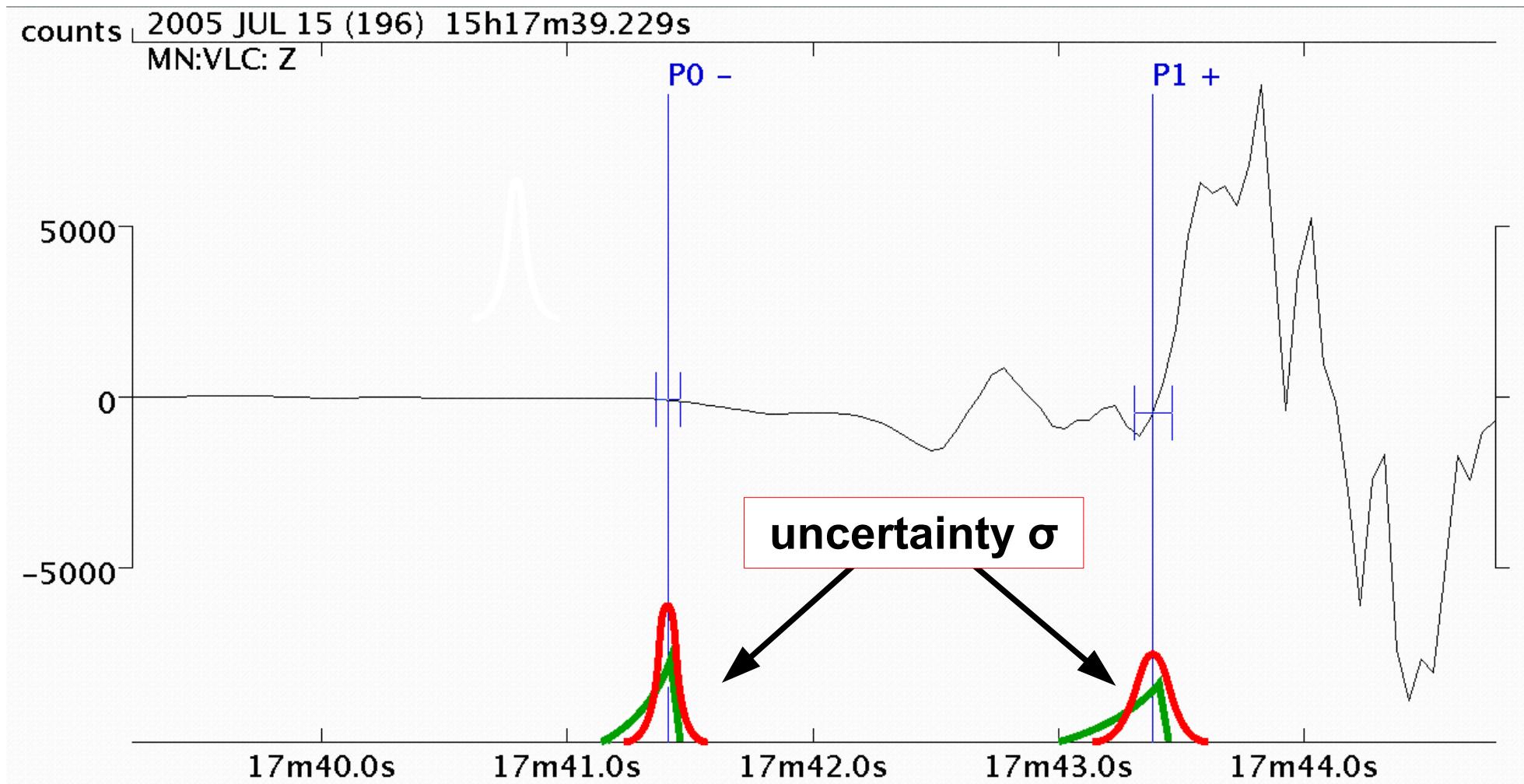
error
bars

Gaussian
confidence
ellipsoid
(~PDF)

probability
density
function
(PDF)

linear methods

Arrival times and pick uncertainty

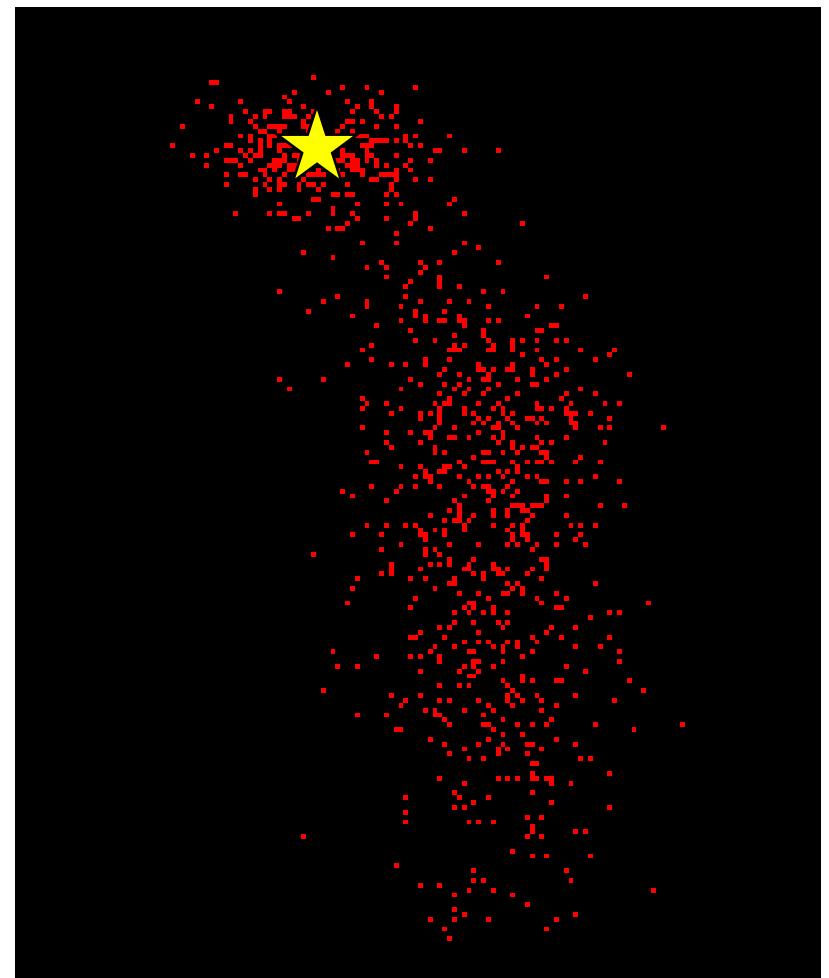
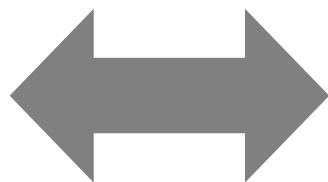
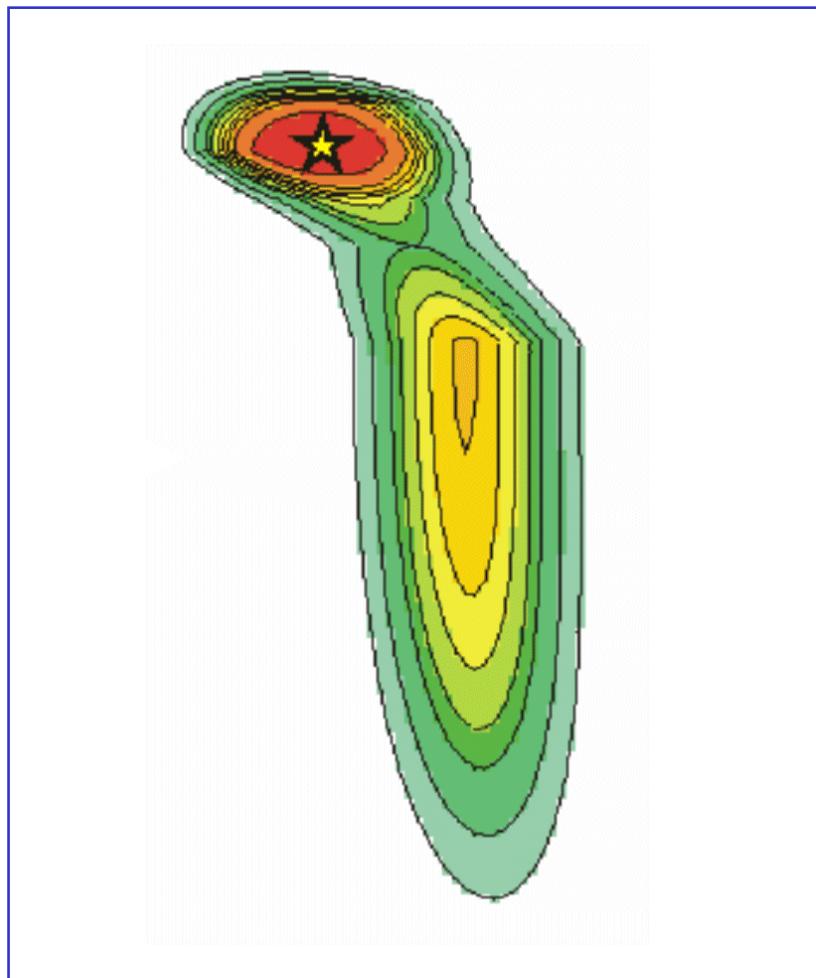


e.g. Tarantola, A. (1987) - refs in Lomax, A., A. Michelini, A. Curtis (2009) - etc...

Probabilistic, global-search event location

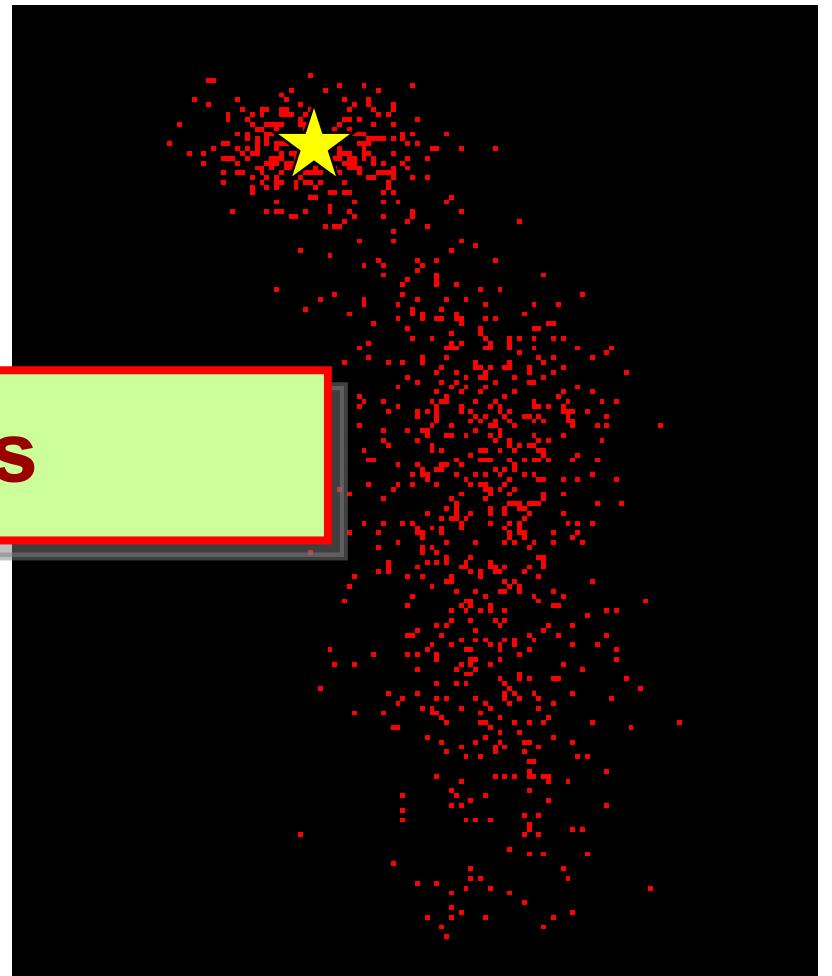
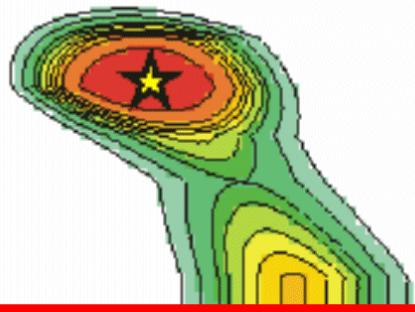
Probability Density Function:

$$pdf(\mathbf{x}) = k e^{-f(\text{misfit}(\mathbf{x})/\sigma)}$$

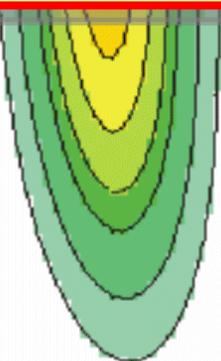


Probabilistic, global-search event location

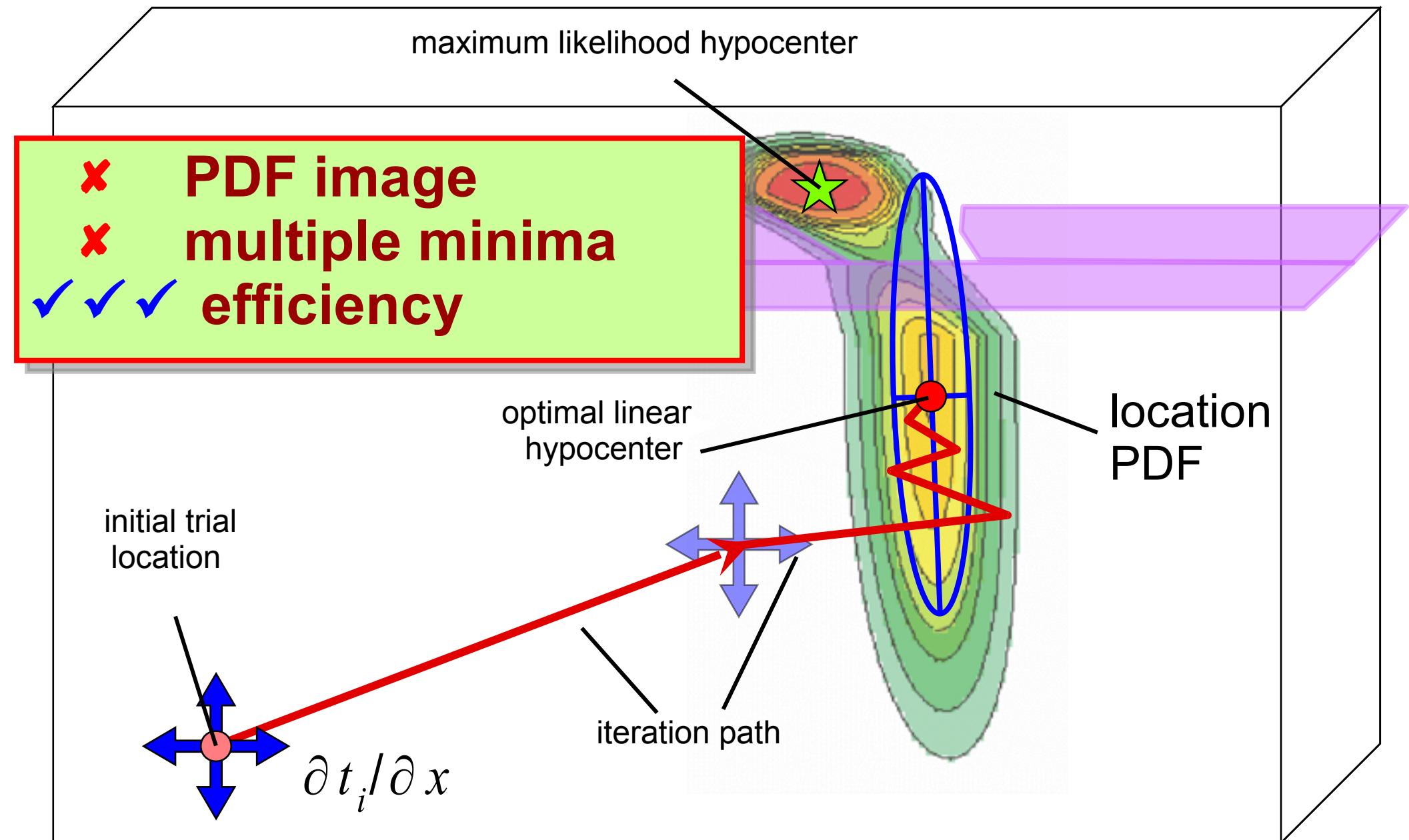
- PDF image
- multiple minima
- efficiency



→ 3D & complex models

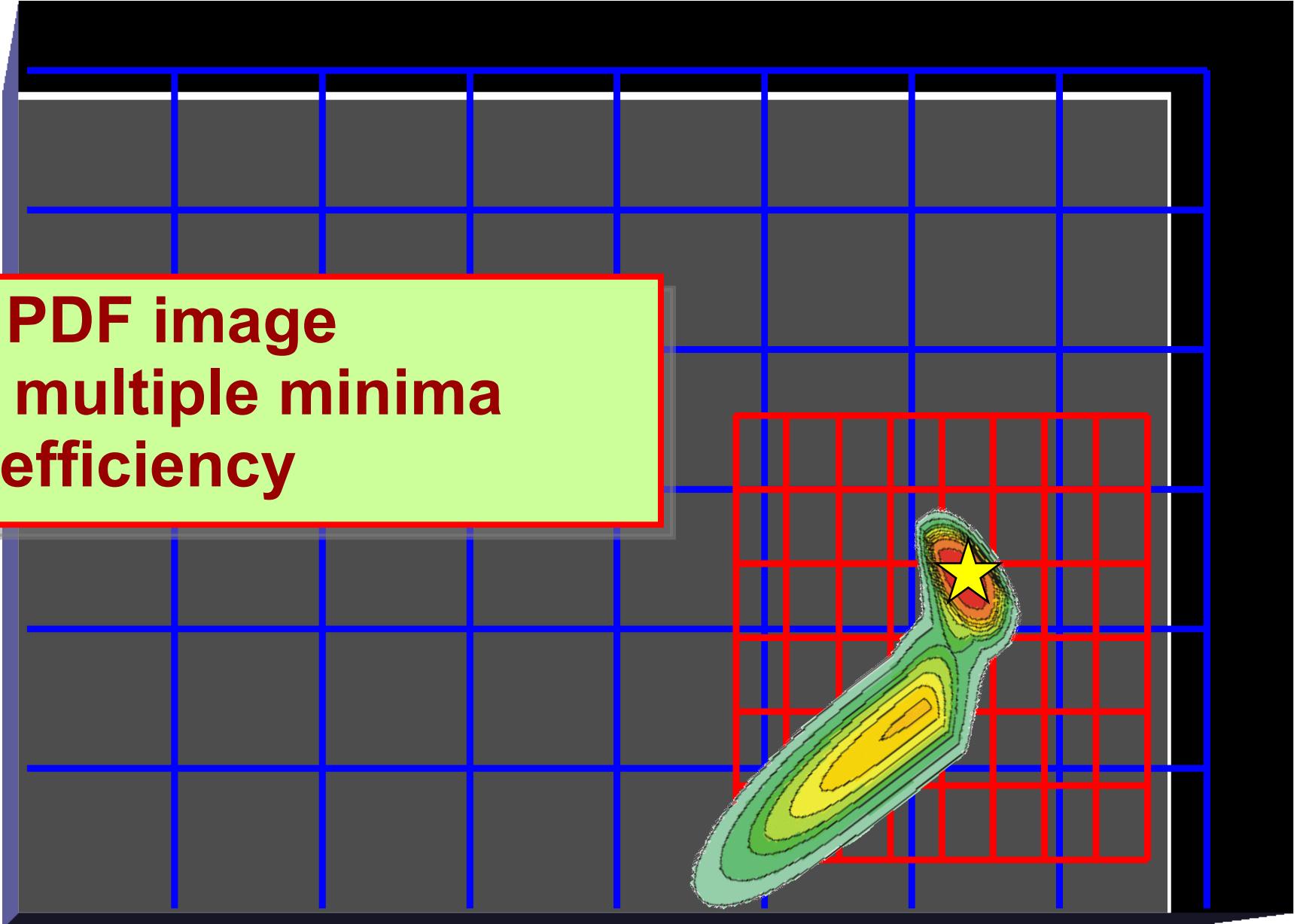


Iterative-linearized location

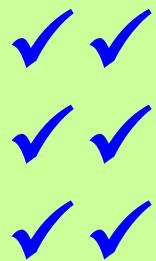


Global-Search methods: Grid search

✓✓ PDF image
✓✓ multiple minima
✗ efficiency



Global-Search methods: Directed walk

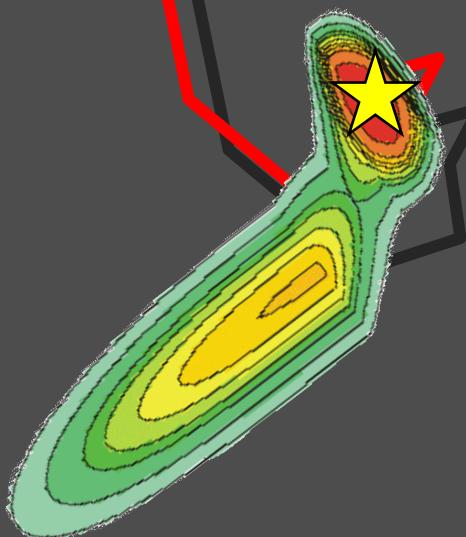


PDF image
multiple minima
efficiency

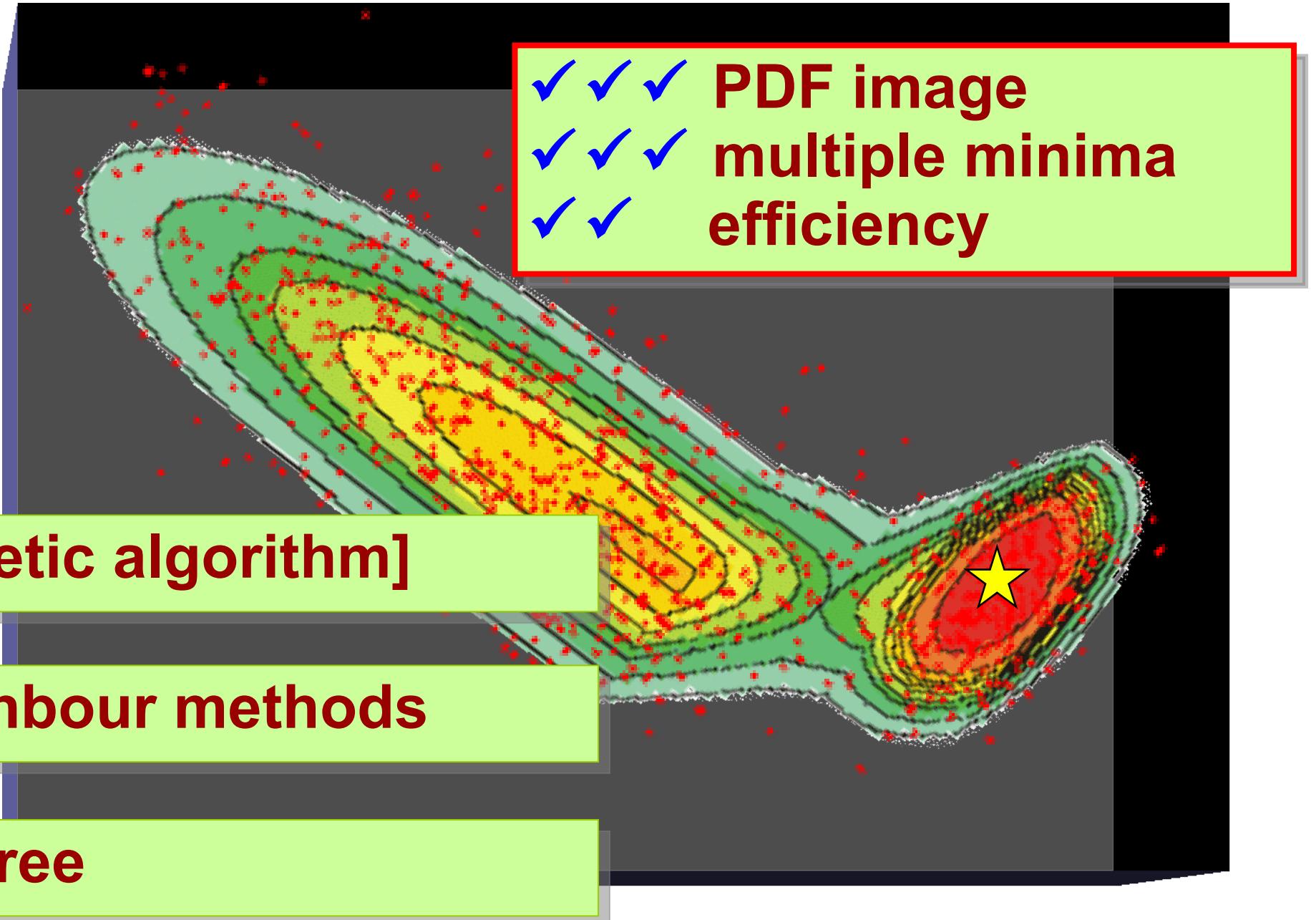
simulated annealing

metropolis methods

simplex...

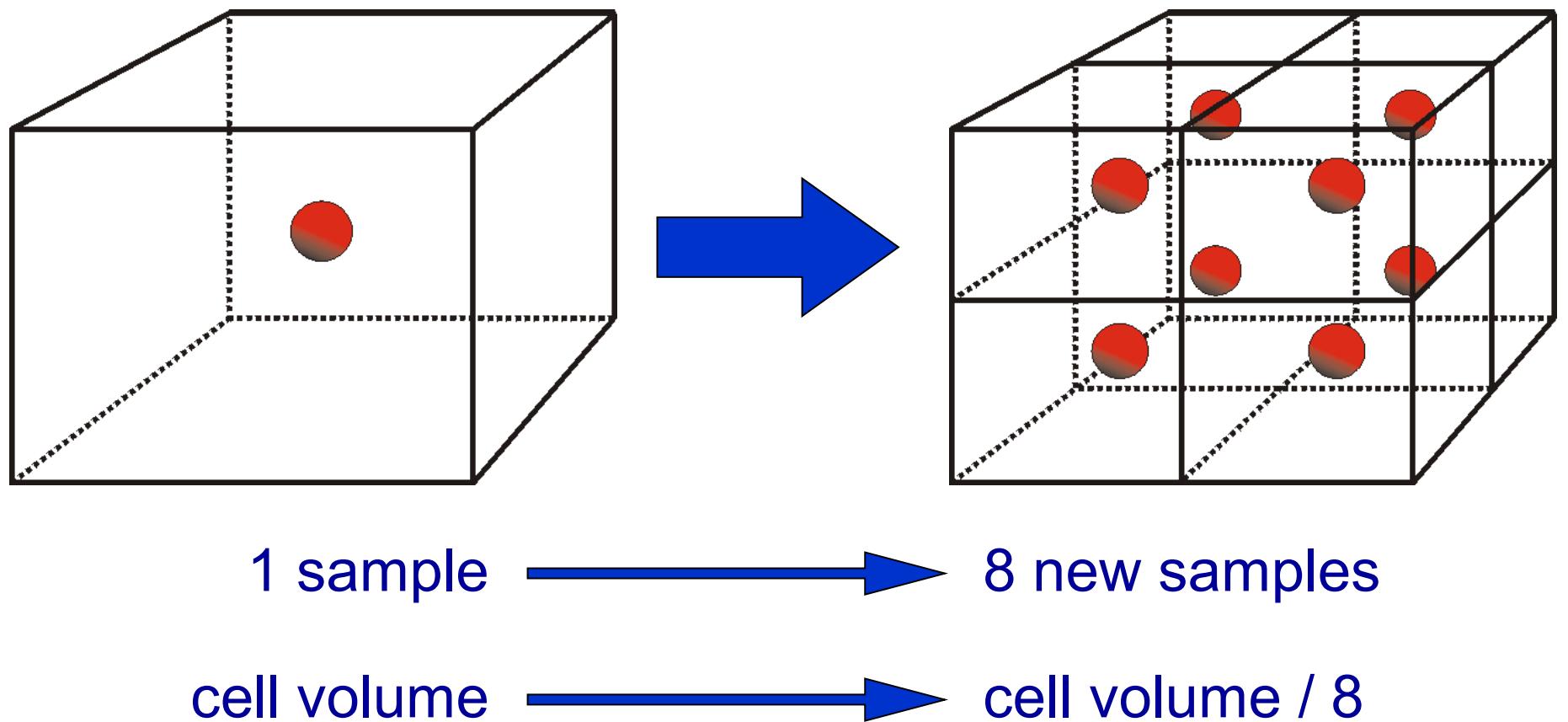


Search methods: Importance sampling

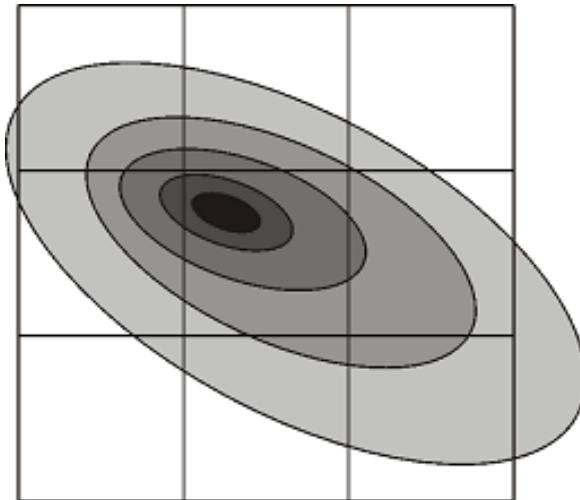


2. Probabilistic, global-search earthquake location **The Oct-tree importance sampling method**

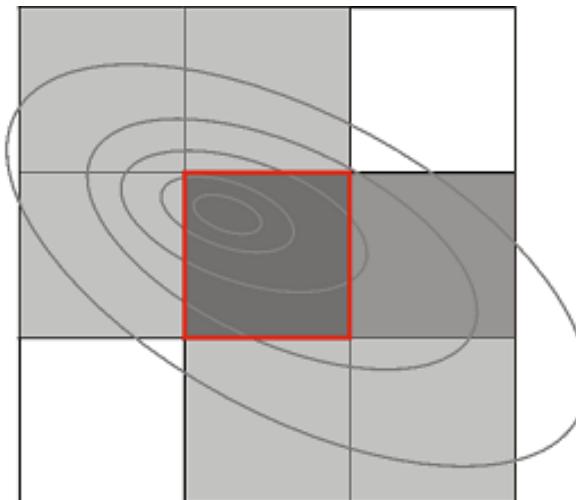
Sub-division of highest probability cell:



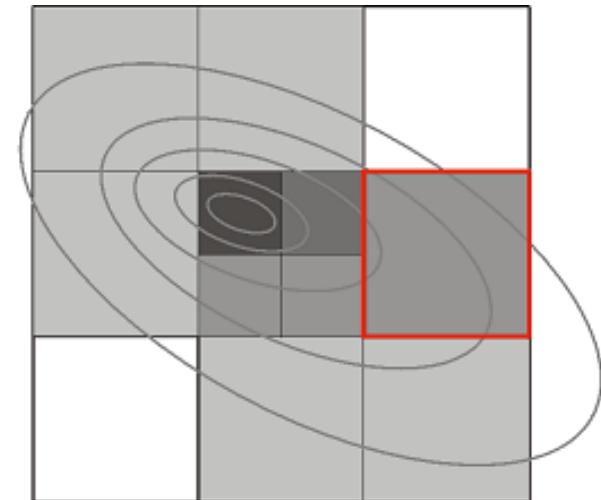
Oct-Tree sampling procedure



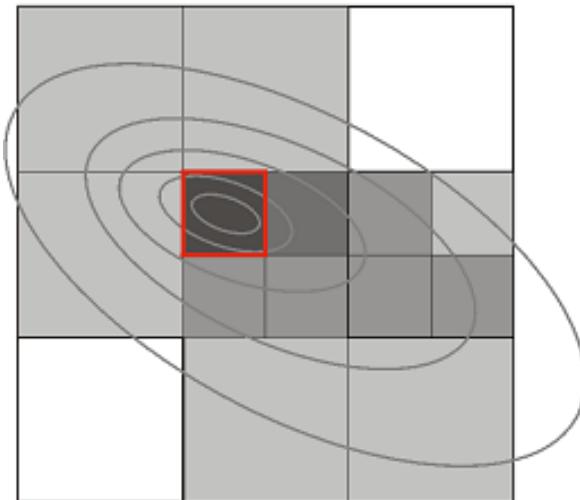
a) true PDF



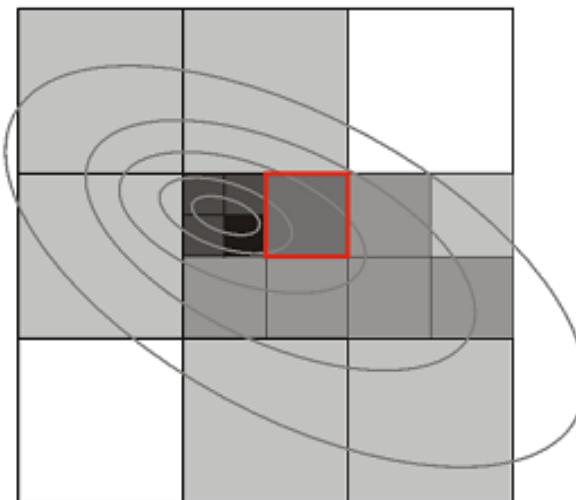
b) initial sampling



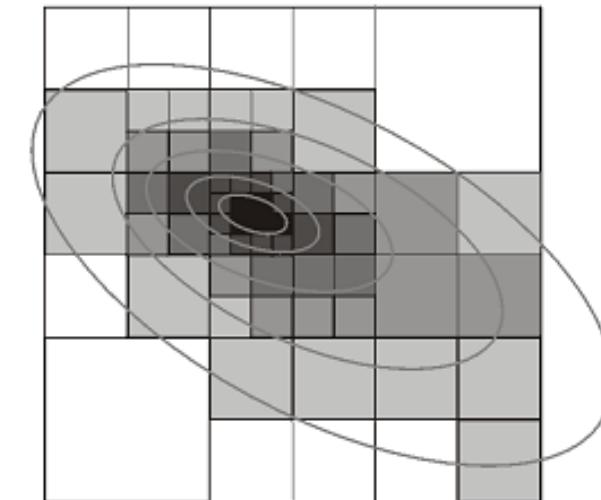
c) subdivision



d) subdivision



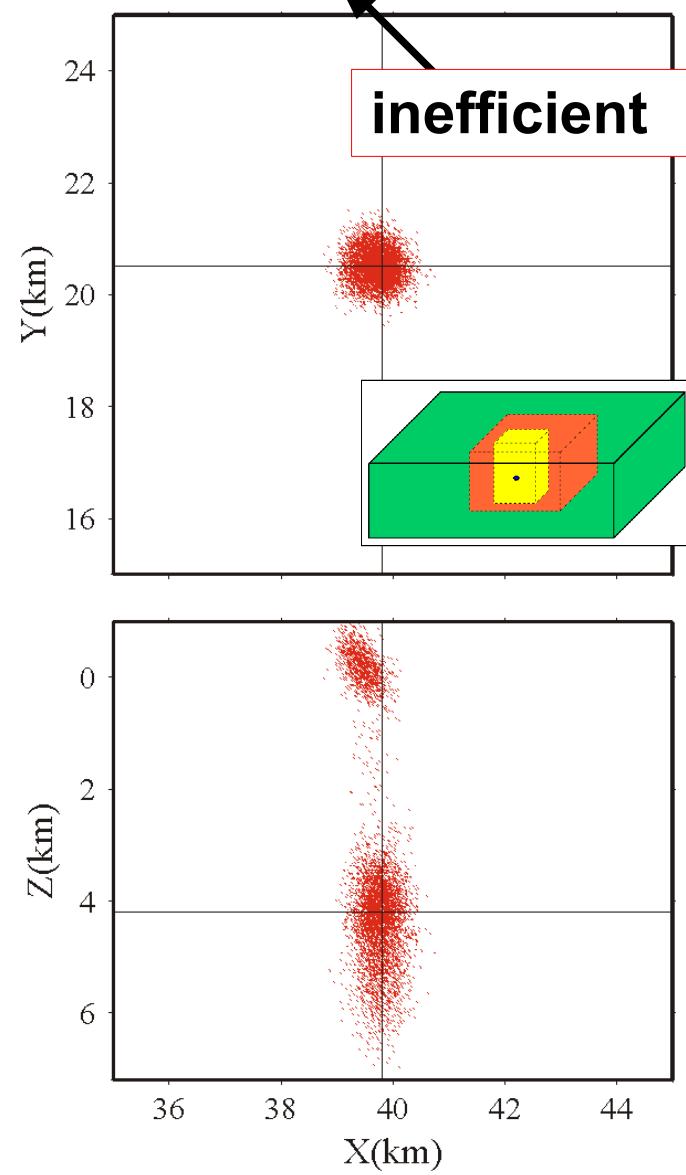
e) subdivision



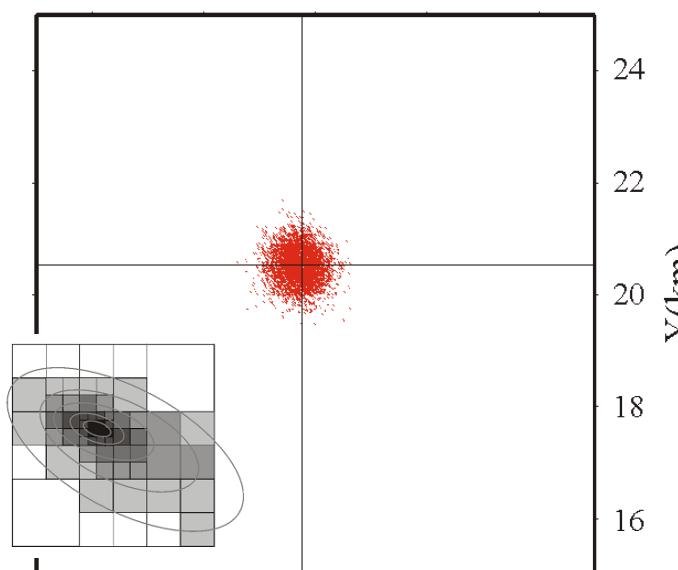
f) many subdivisions

Example: PDF with two maxima

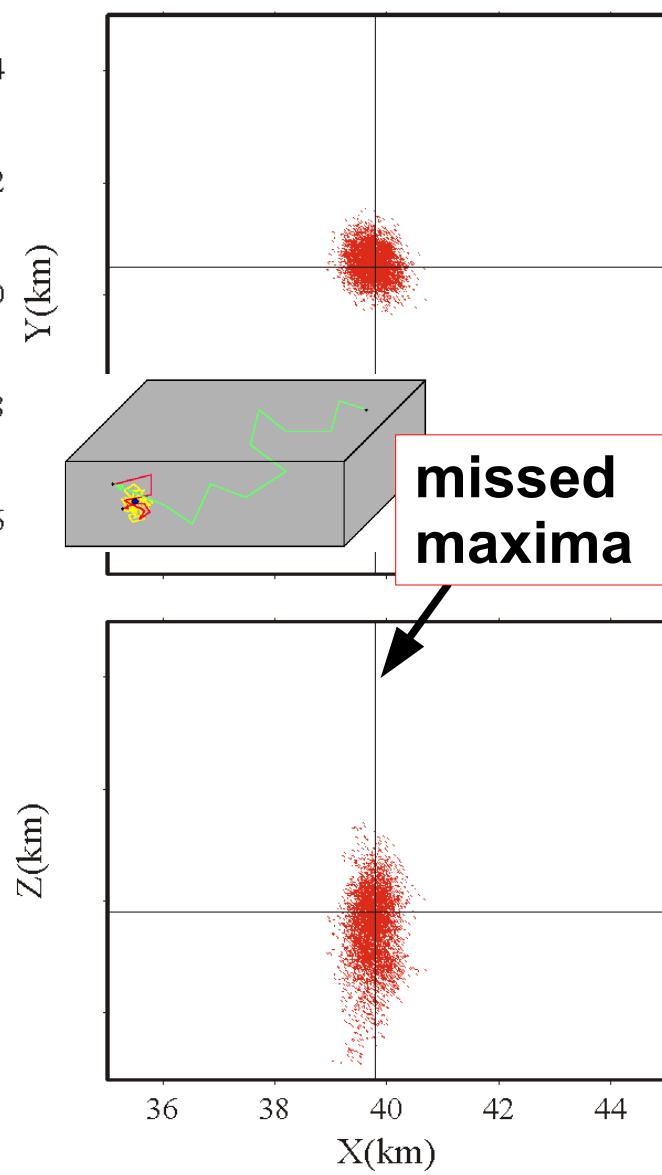
Grid search
(800,000 samples)



Oct-Tree search
(10,000 samples)



Metropolis search
(10,000 samples)



2. Probabilistic, global-search earthquake location

The EDT Probability Density Function

RMS/L2-norm vs EDT Probability Density Function

RMS/L2-norm

$$pdf(x, t_0) \propto e^{-\frac{1}{2} \sum_{obs_i} \frac{[T_{obs_i}(x) - T_{calc_i}(x)]^2}{\sigma^2}}$$

“satisfy **all** the observations”

EDT (Equal Differential Time)

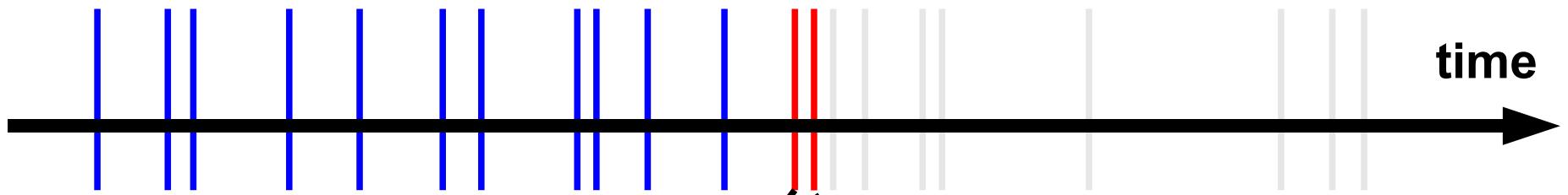
$$pdf(x) \propto \left[\sum_{obs_a, obs_b} e^{-\frac{[(T_{obs_a}(x) - T_{obs_b}(x)) - (T_{Tcalc_a}(x) - T_{Tcalc_b}(x))]^2}{\sigma^2}} \right]^N$$

“satisfy **the most pairs** of observations”

- independent of origin time

Phase association and event detection → EDT

picks (phase arrivals, noise, ...)



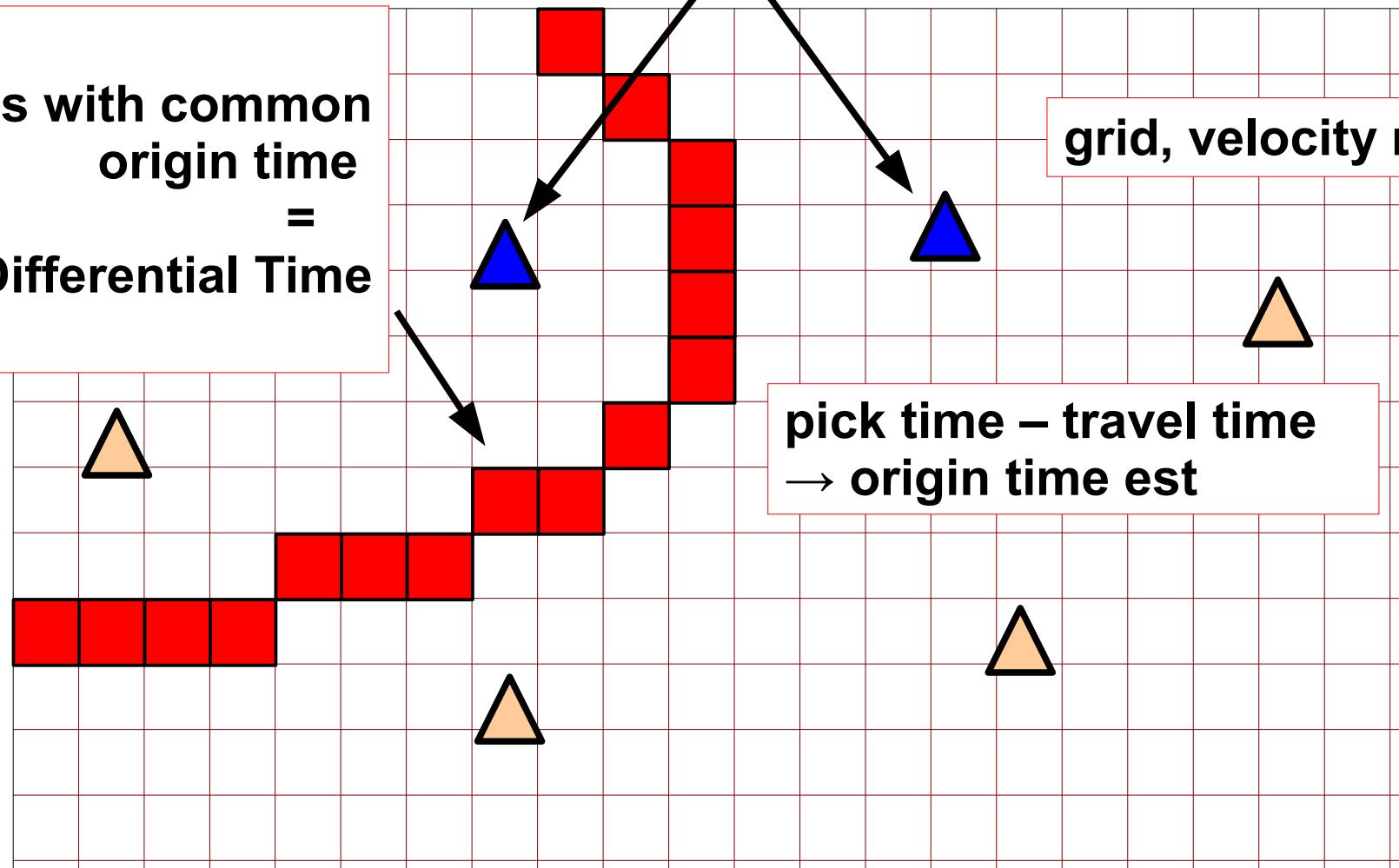
cells with common
origin time

=

Equal Differential Time

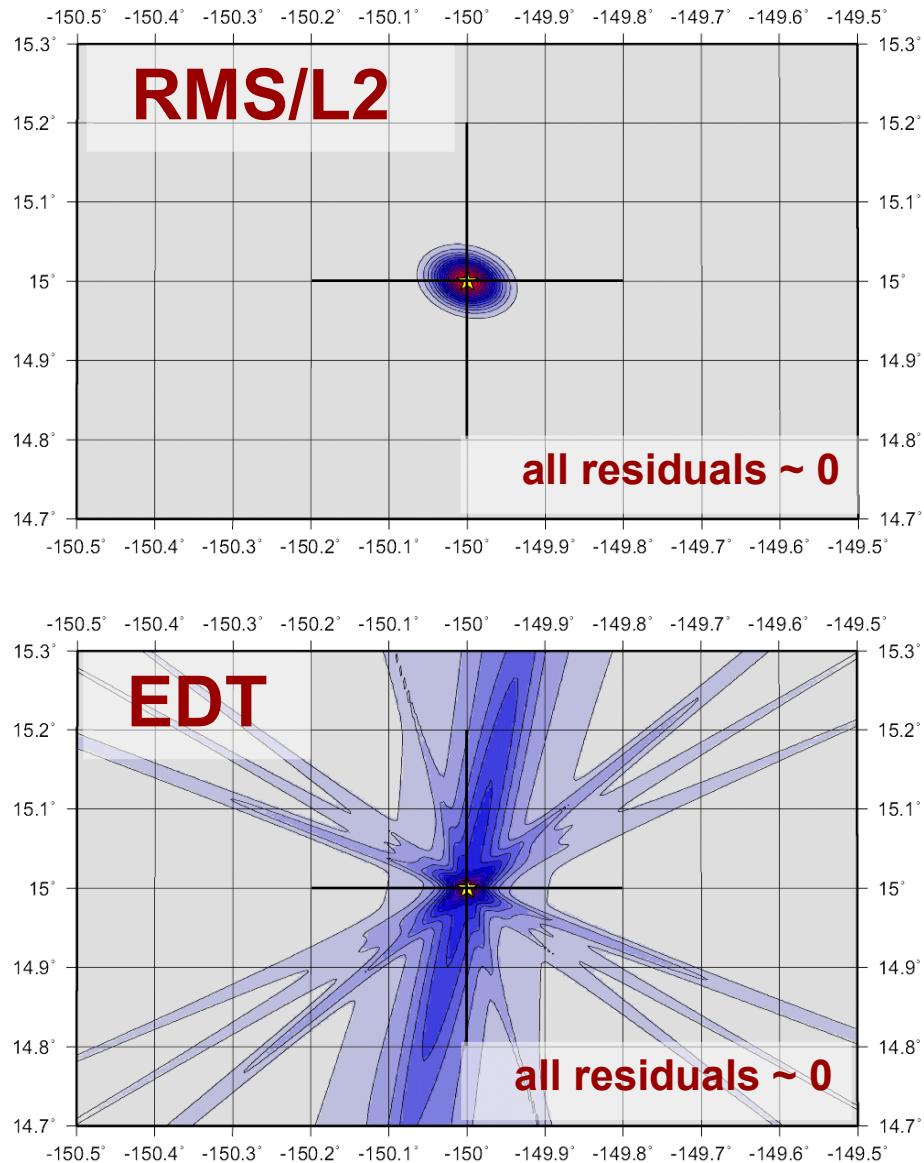
grid, velocity model

pick time – travel time
→ origin time est

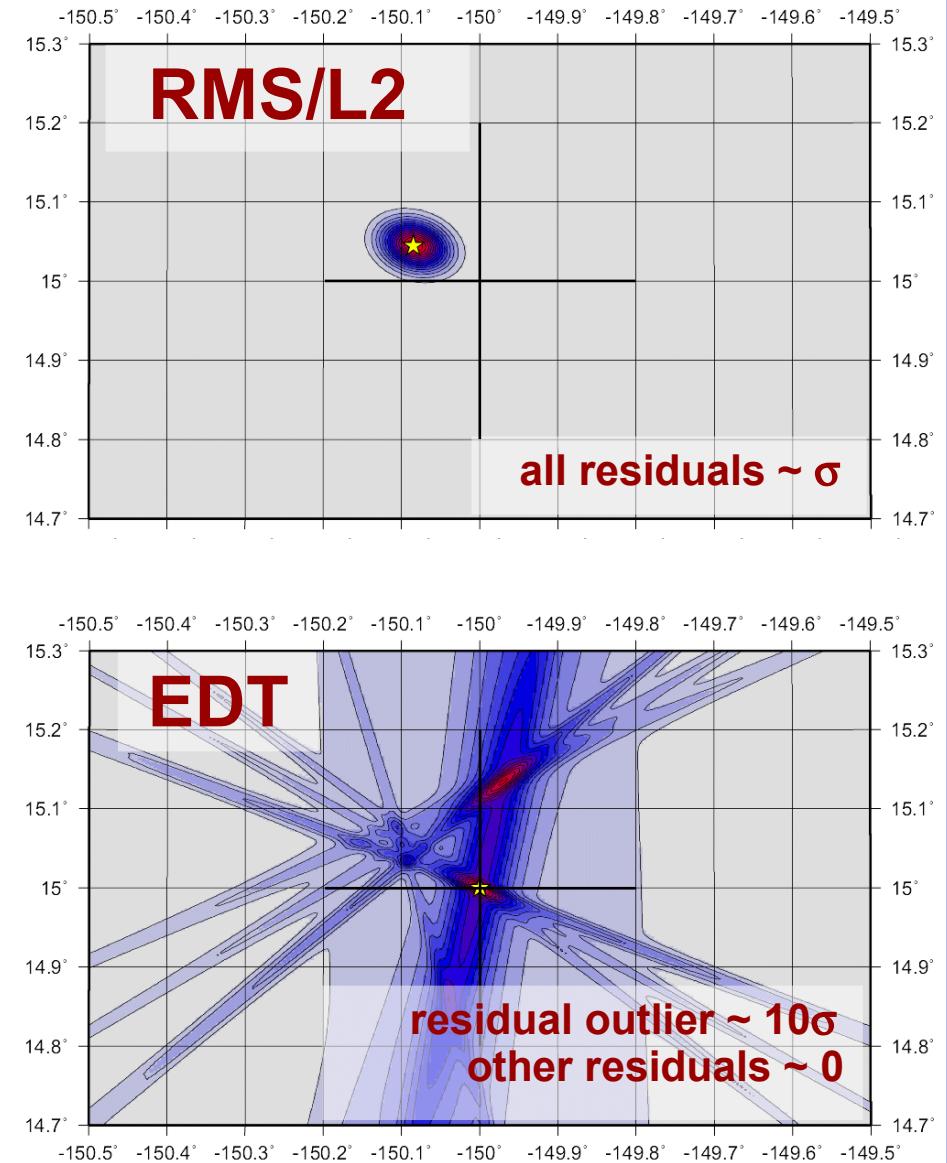


RMS/L2 vs EDT with outlier data

perfect data (6 obs)



1 outlier data (err=10 σ)



Real-Time Earthquake Location

3. New perspectives in observatory analysis: Illustrative examples of global-search earthquake location

Anthony Lomax

ALomax Scientific, Mouans-Sartoux, France

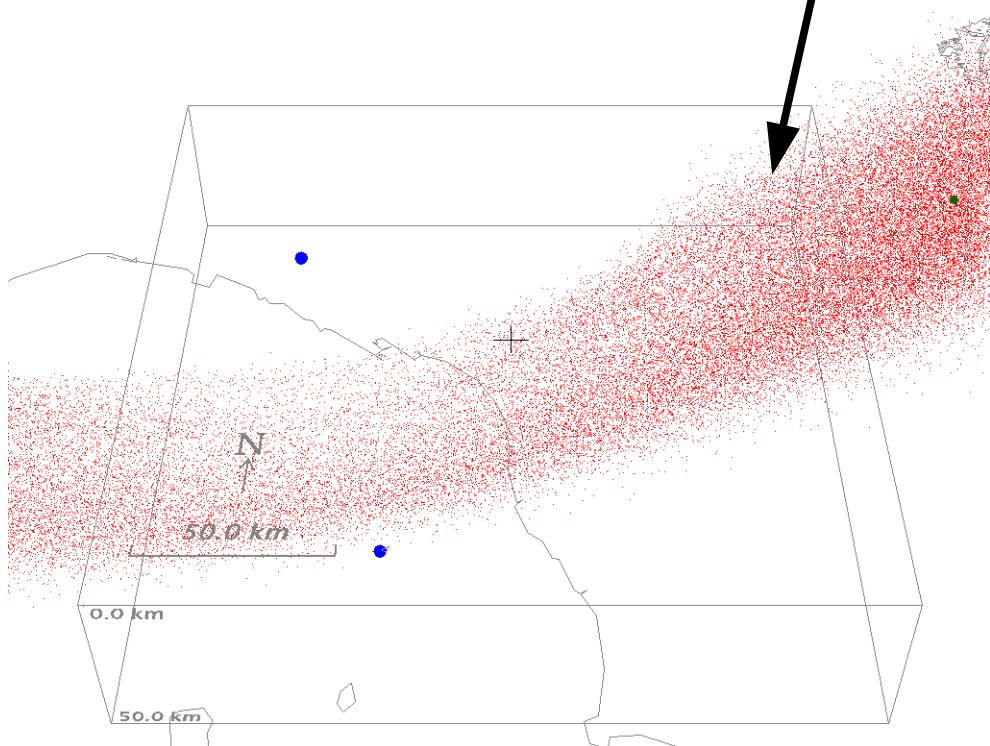
Alberto Michelini

Istituto Nazionale di Geofisica e Vulcanologia, Roma, Italy

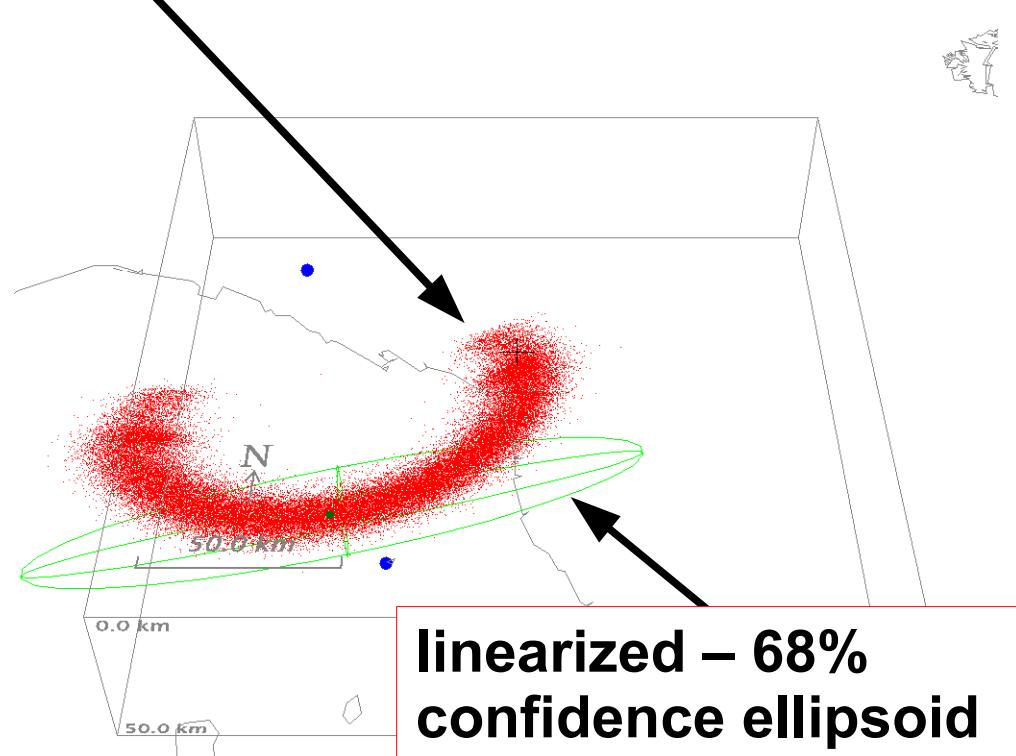
Andrew Curtis

ECOSSE, Grant Institute of GeoSciences, University of Edinburgh, Edinburgh, United Kingdom

global search – probability density function (PDF)



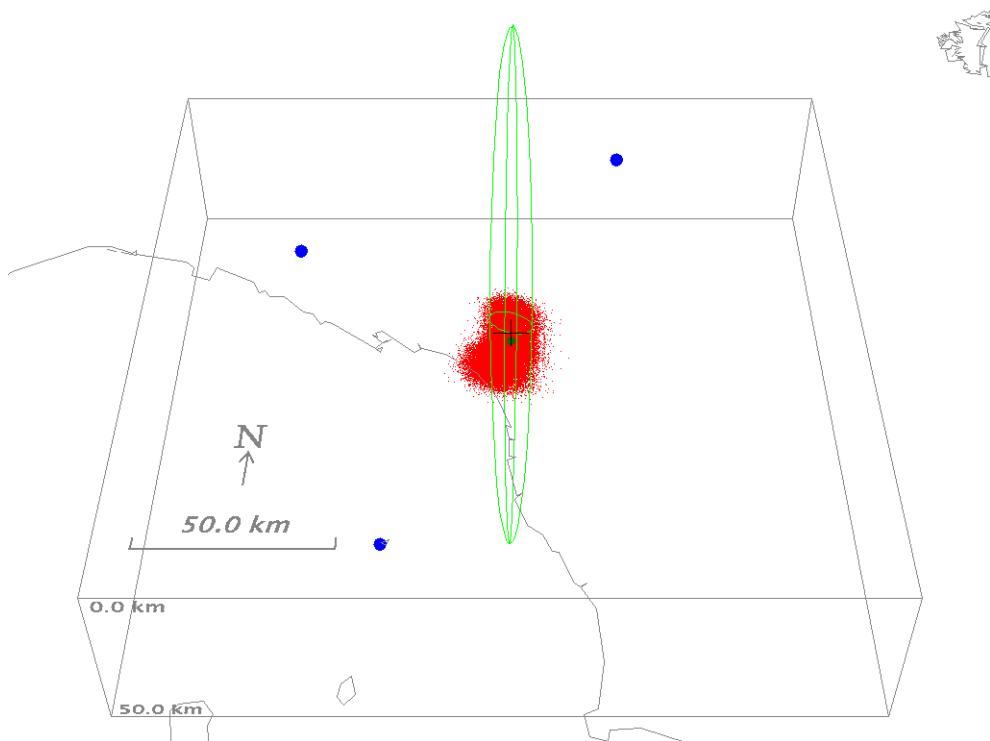
2P phases (2 stations)



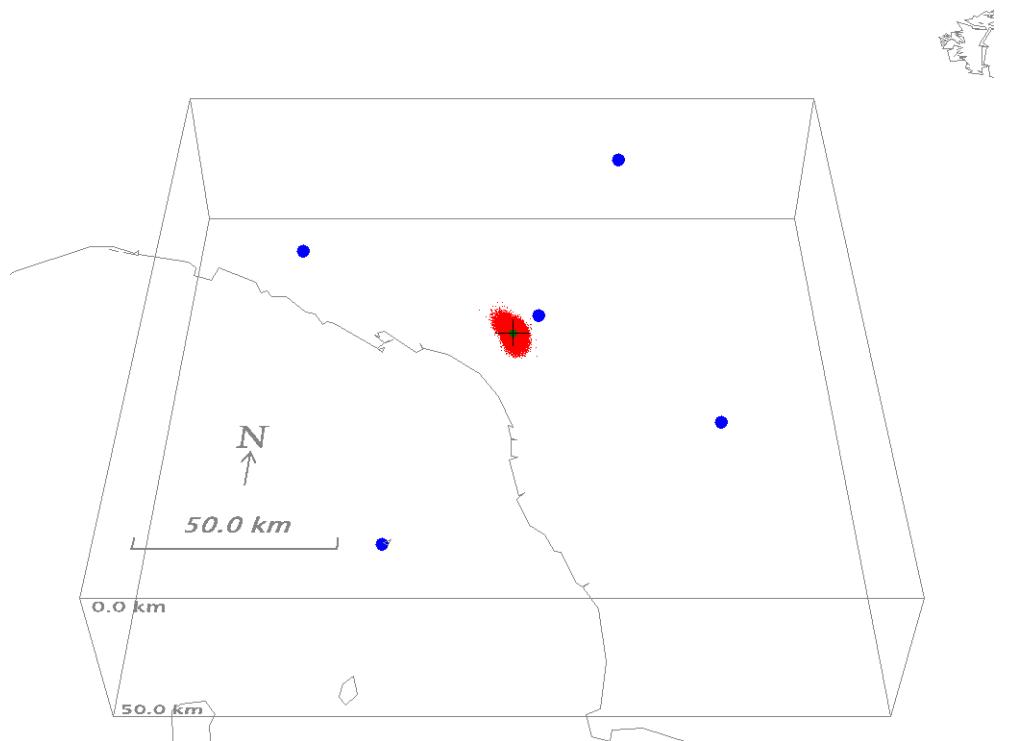
2P and 2 S phases (2 stations)

linearized – 68%
confidence ellipsoid

Few available stations (cont)

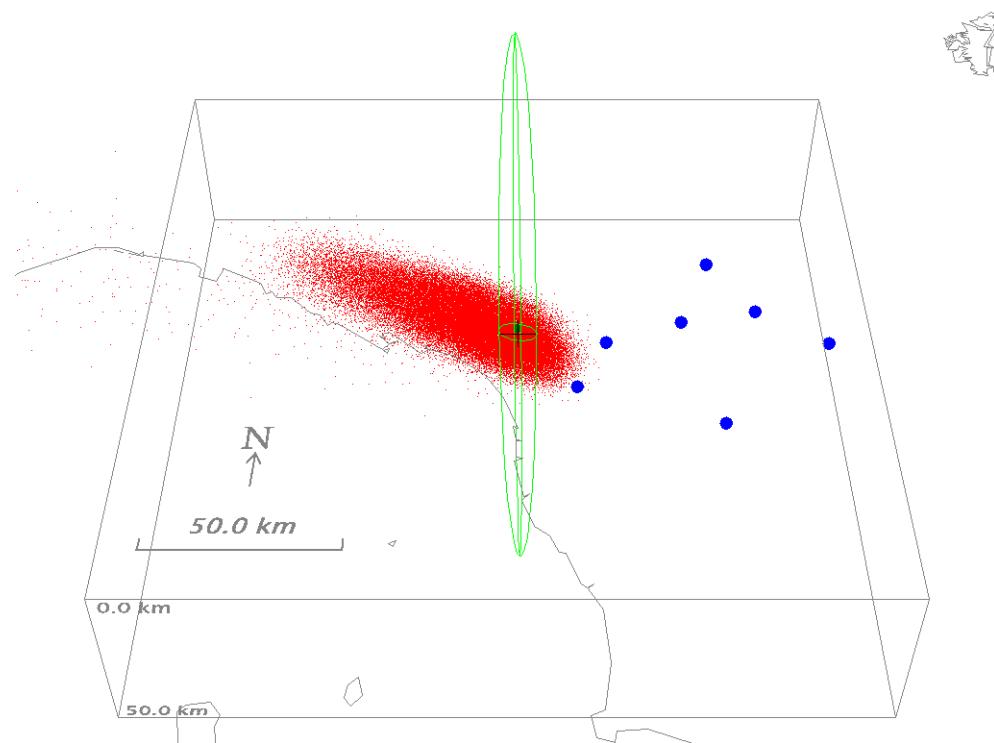


3P phases (3 stations)



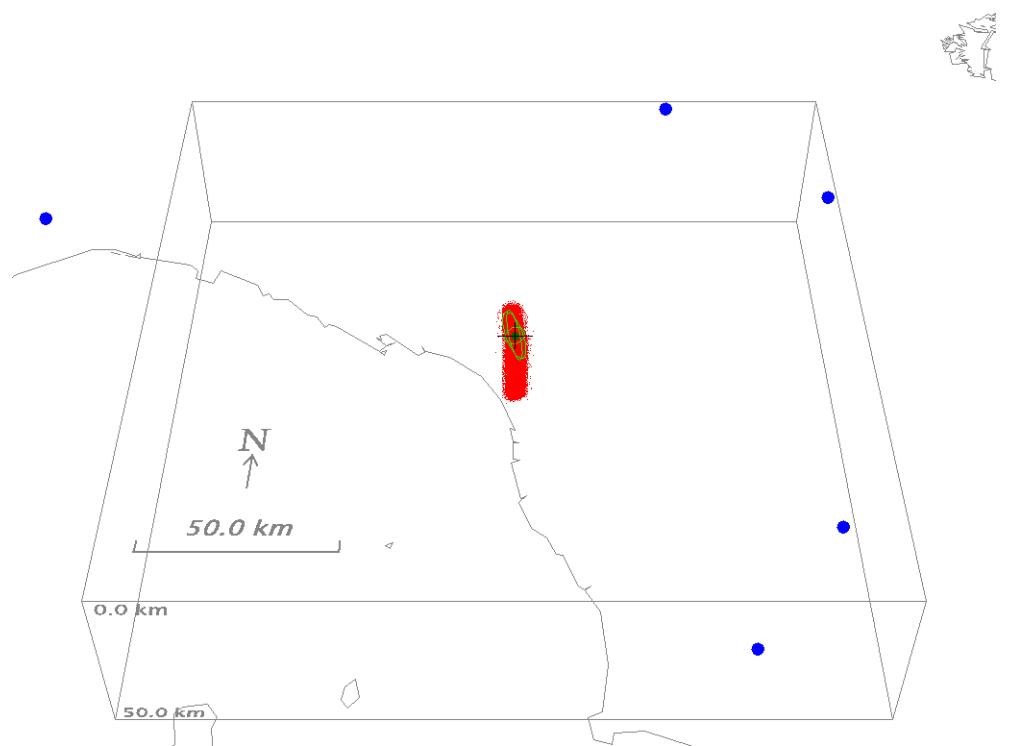
5P and 3S phases (5 stations)

Stations to one side of the event

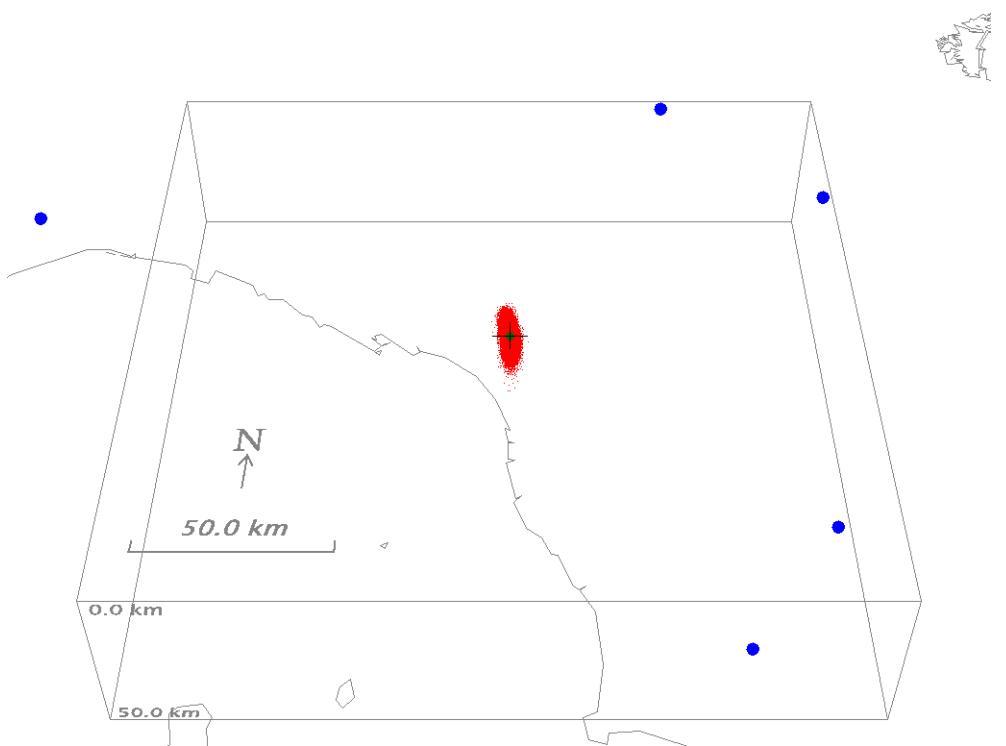


P-wave arrival times at 7 stations

Stations far from the event

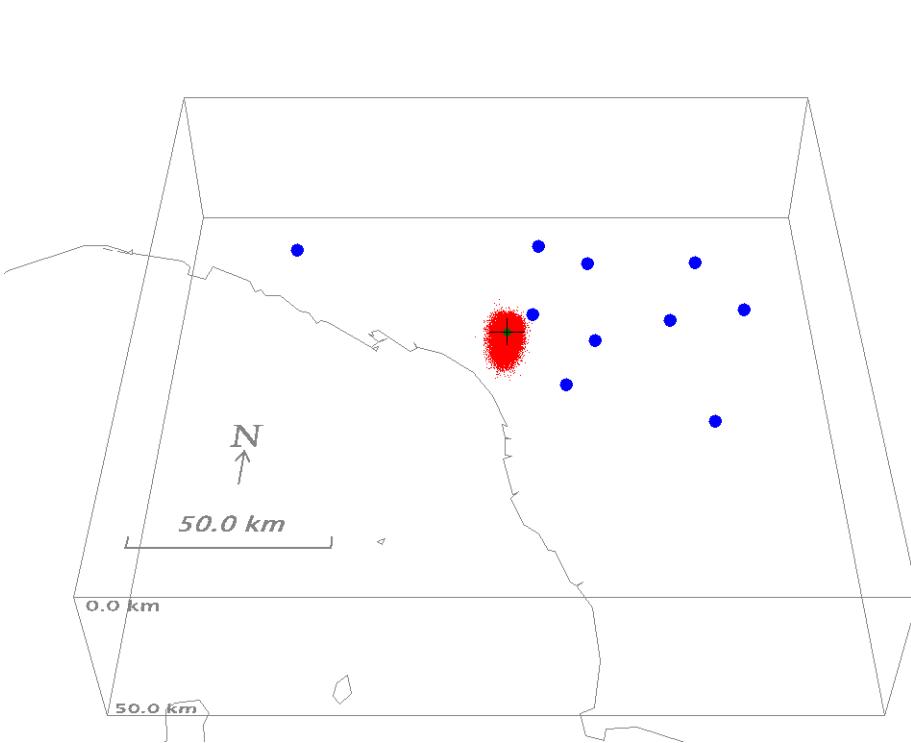


P arrival times only

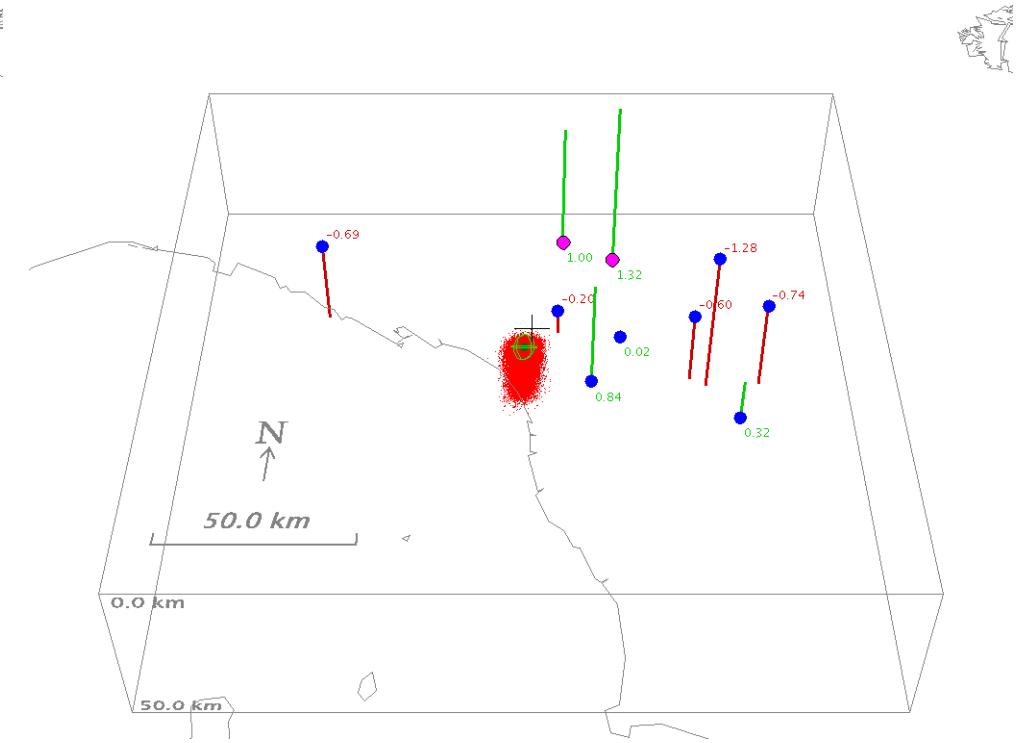


P and S arrival times

Incorrect picks and phase id - outlier data: L2-norm

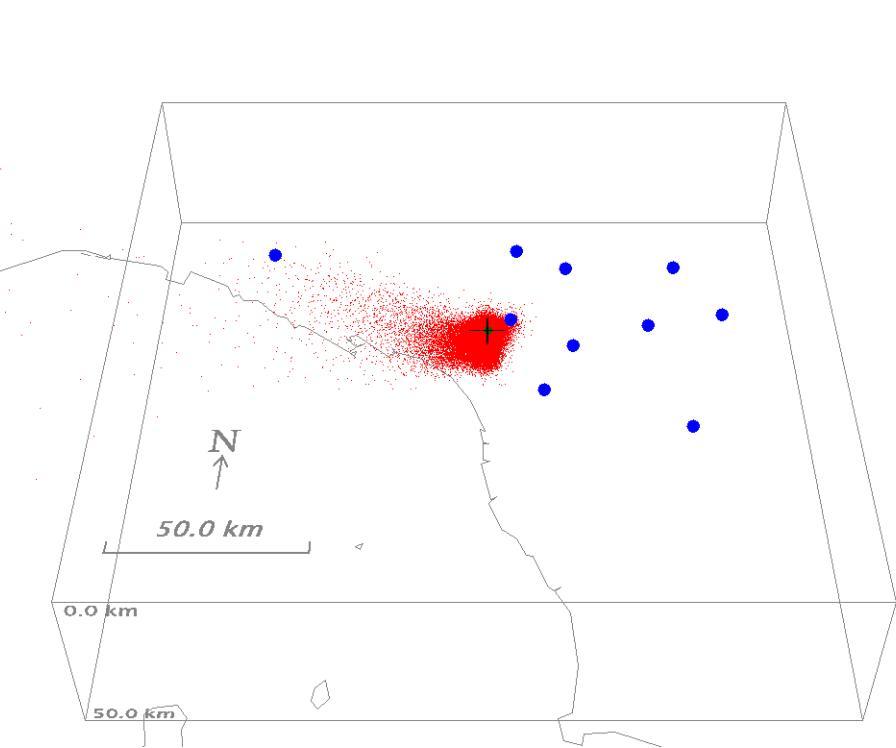


no outliers

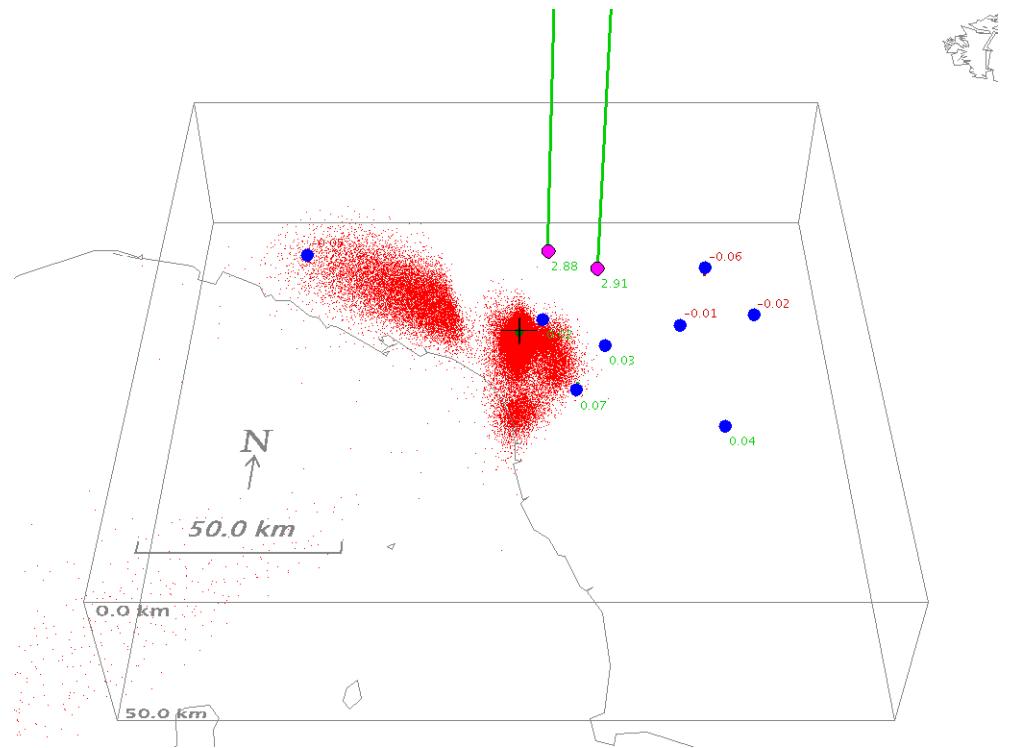


two arrival-time outliers

Incorrect picks and phase id - outlier data: EDT

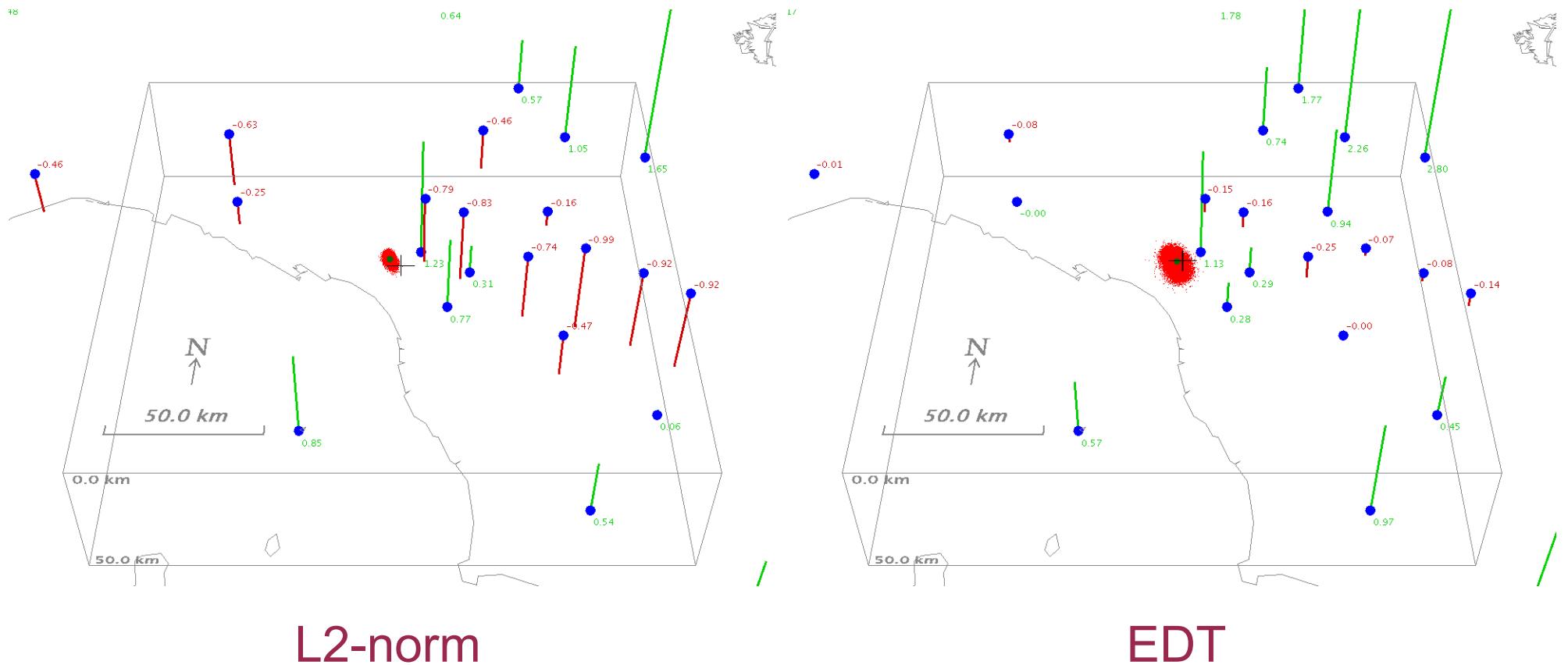


no outliers

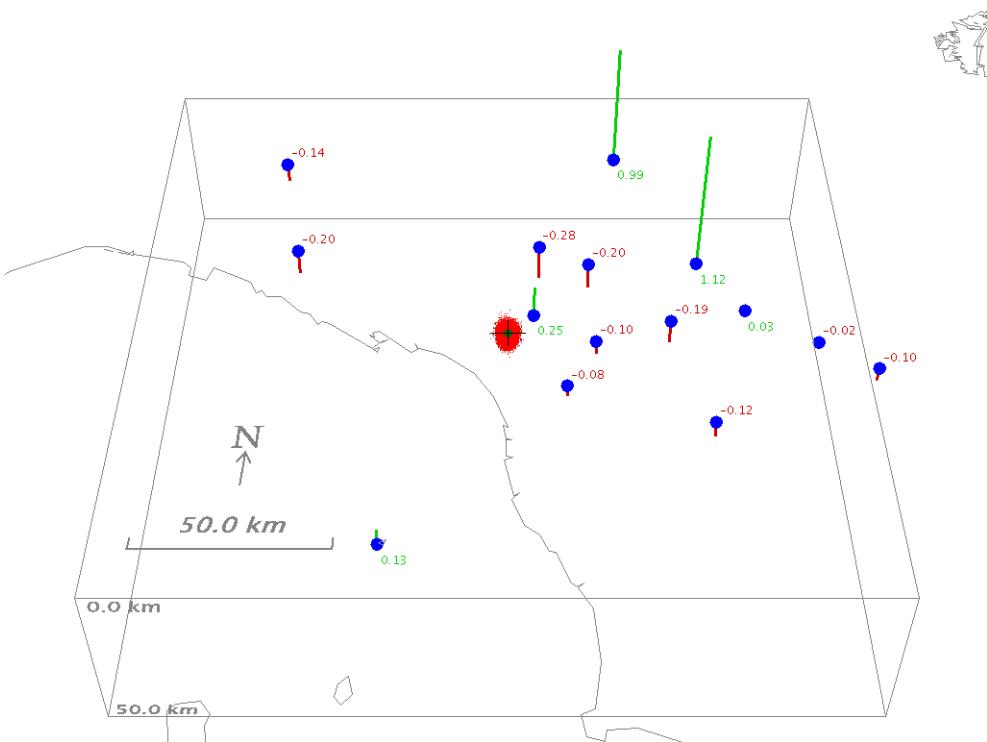


two arrival-time outliers

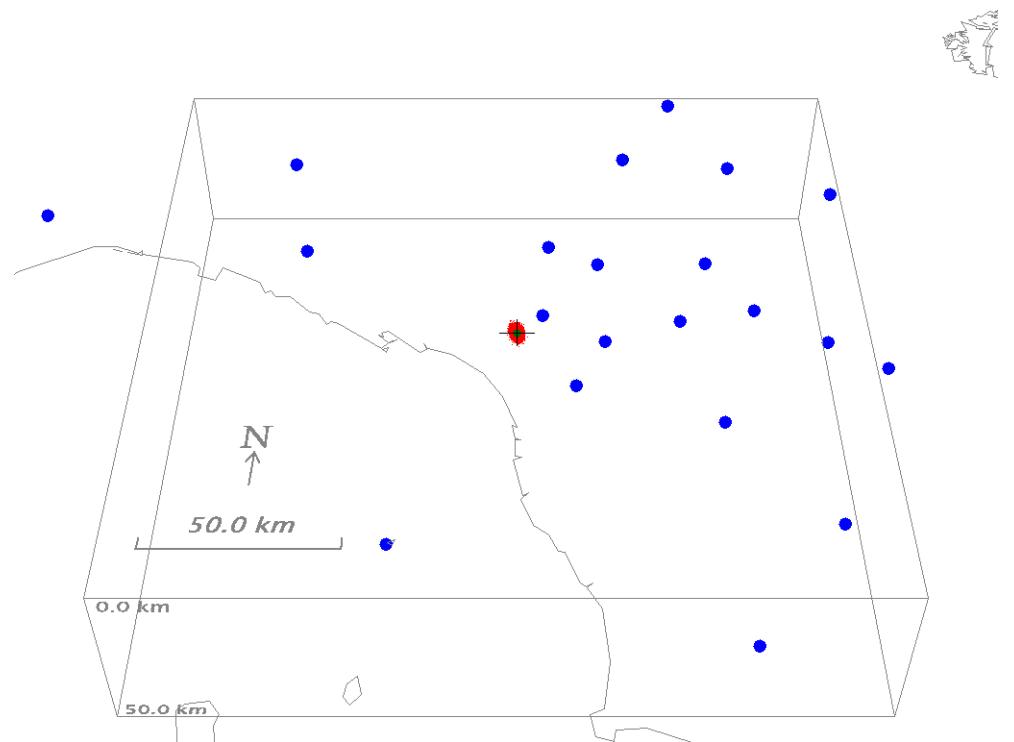
Incorrect velocity model



Station corrections



Original location



Location with corrected times

3. New perspectives in observatory analysis: Illustrative examples of global-search earthquake location

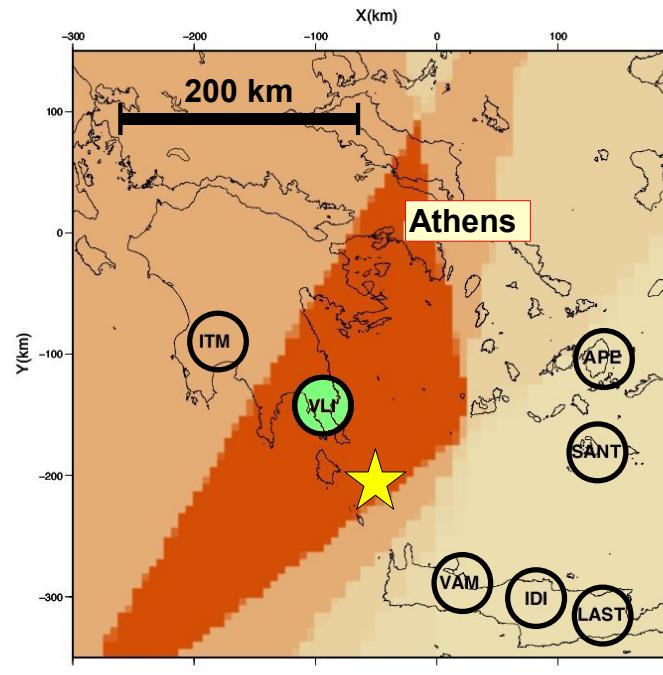
Evolutionary, early-warning location

Evolutionary Location – 2006.01.08 M6.8 Greece



Early warning scenario:

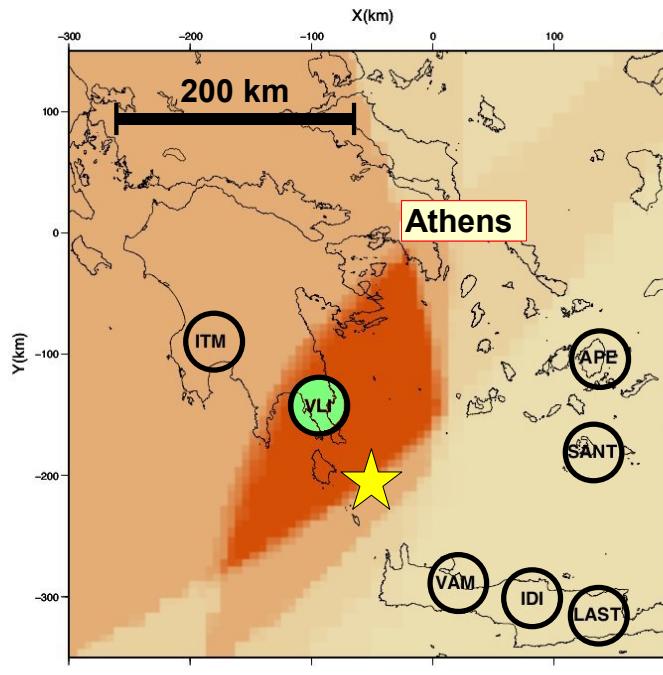
How early before S wave arrival in Athens (t^s) can the location be determined?



$\Delta t = 0.00 \text{ s}$
 $t_{\text{now}} = 14.90 \text{ s}$
 $t^s_{\text{Athens}} = -40.00 \text{ s}$

RTLoc

Evolutionary Location – 2006.01.08 M6.8 Greece

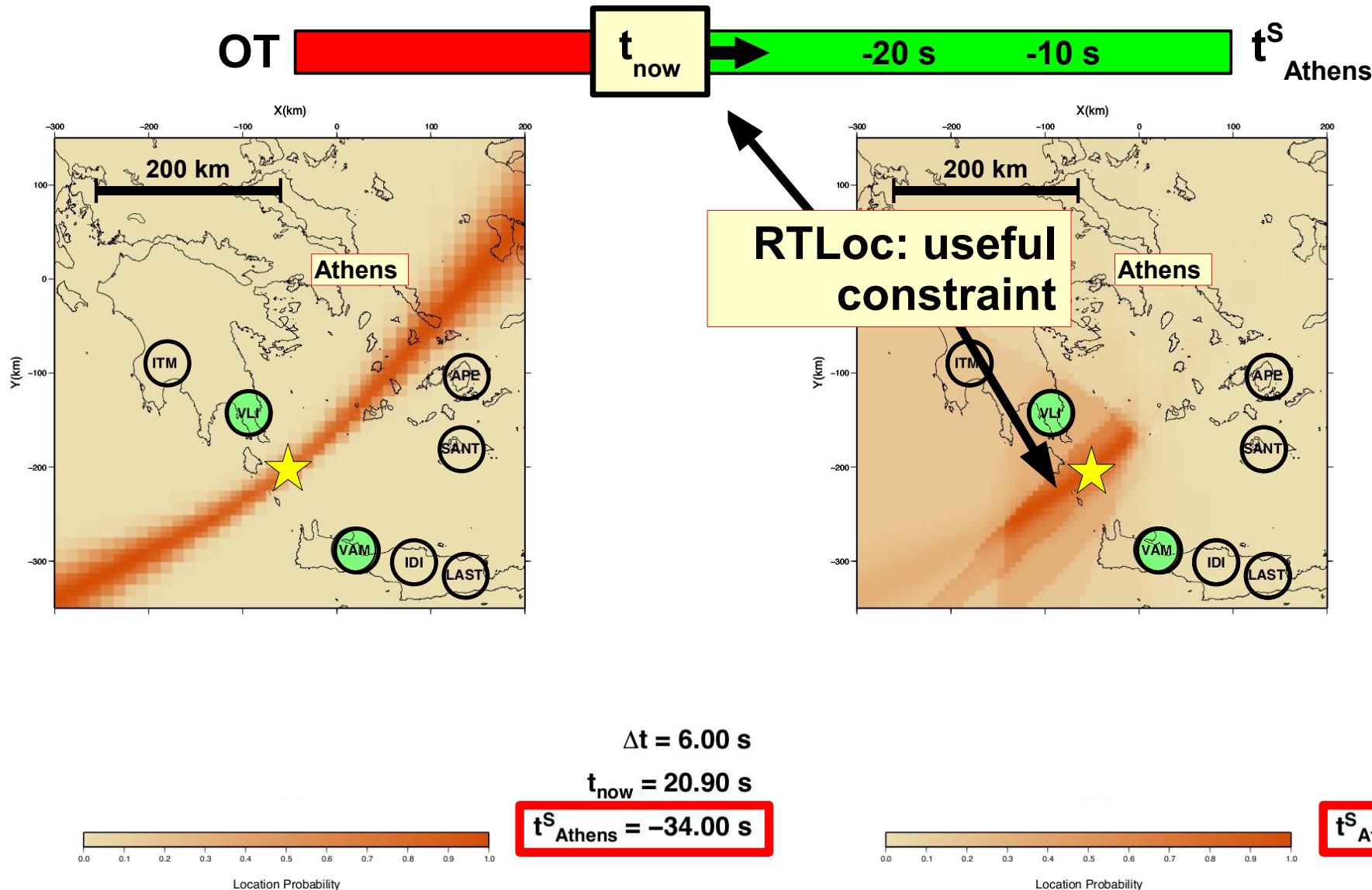


$\Delta t = 4.00 \text{ s}$
 $t_{\text{now}} = 18.90 \text{ s}$
 $t^S_{\text{Athens}} = -36.00 \text{ s}$

Location Probability

RTLoc

Evolutionary Location – 2006.01.08 M6.8 Greece



NLLoc

Lomax, et al., 2000

RTLoc

C. Satriano - 2007/07/11

Evolutionary Location – 2006.01.08 M6.8 Greece

OT

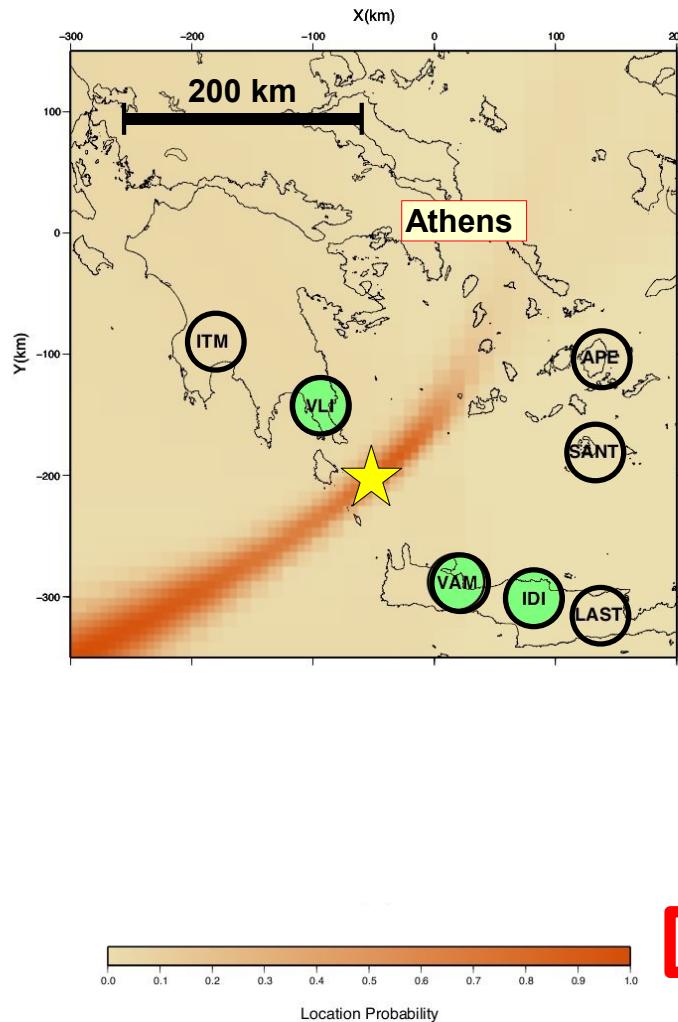
t_{now}

→

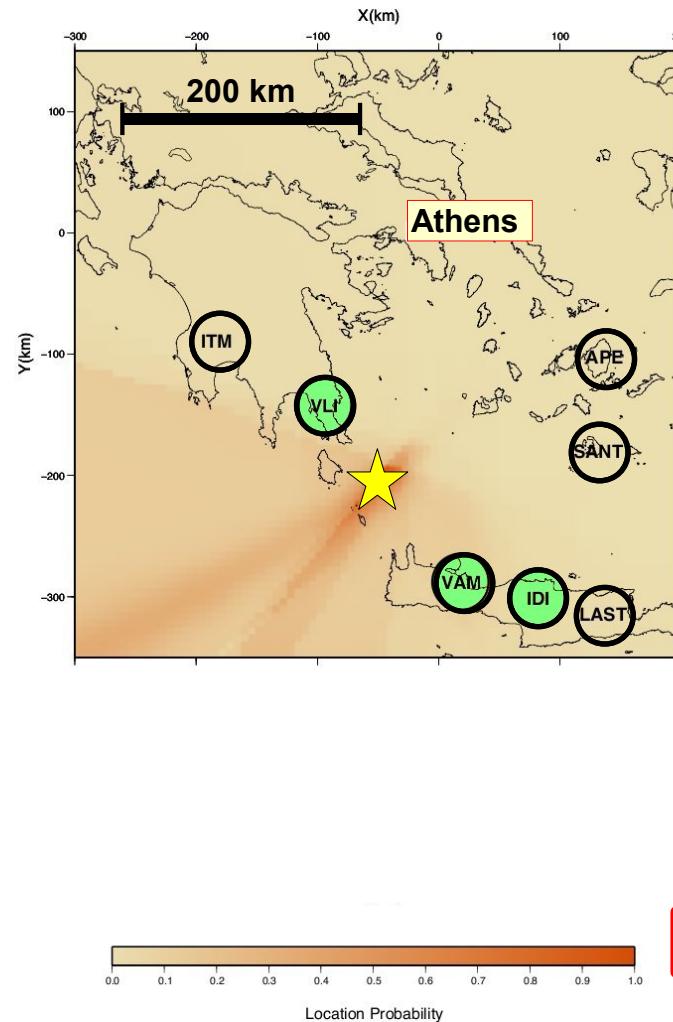
-20 s

-10 s

t^s_{Athens}



NLLoc



RTLoc

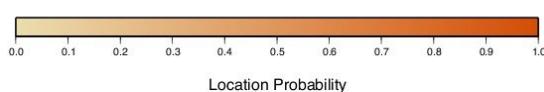
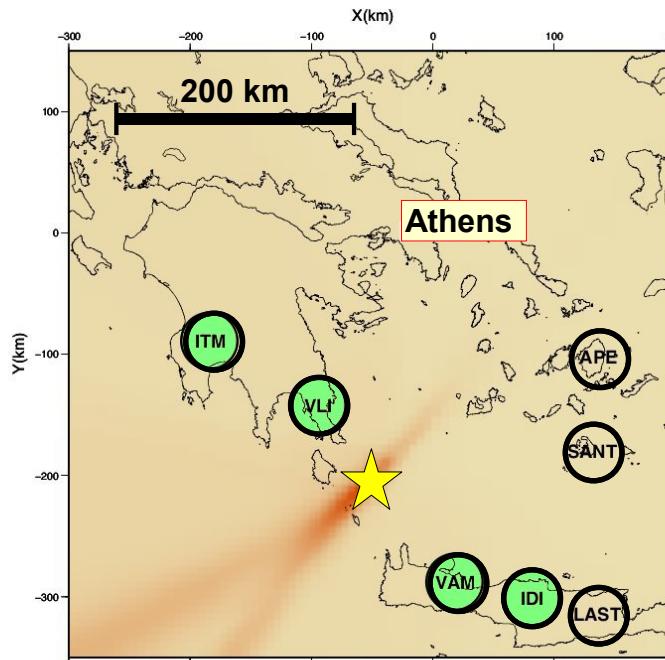
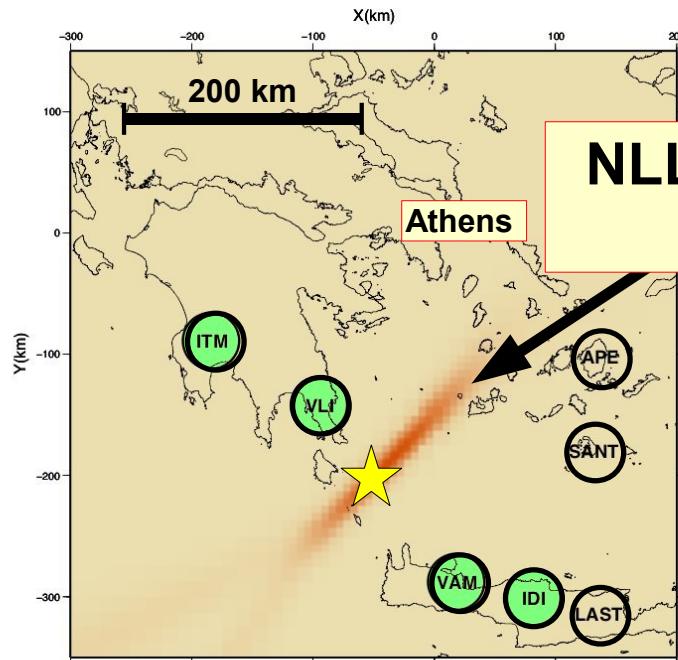
Evolutionary Location – 2006.01.08 M6.8 Greece

OT

t_{now}

-10 s

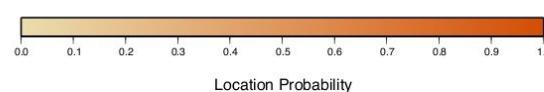
t^s_{Athens}



$$\Delta t = 14.00 \text{ s}$$

$$t_{\text{now}} = 28.90 \text{ s}$$

$$t^s_{\text{Athens}} = -26.00 \text{ s}$$



$$\Delta t = 14.00 \text{ s}$$

$$t_{\text{now}} = 28.90 \text{ s}$$

$$t^s_{\text{Athens}} = -26.00 \text{ s}$$

NLLoc

RTLoc

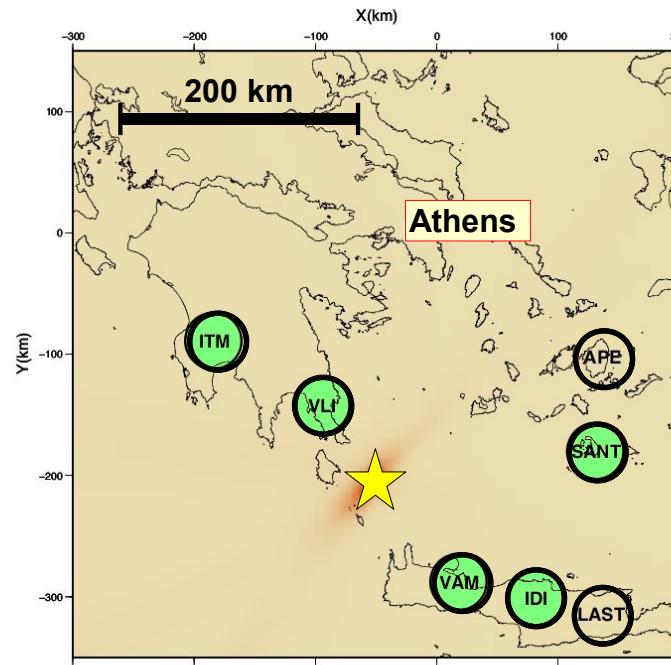
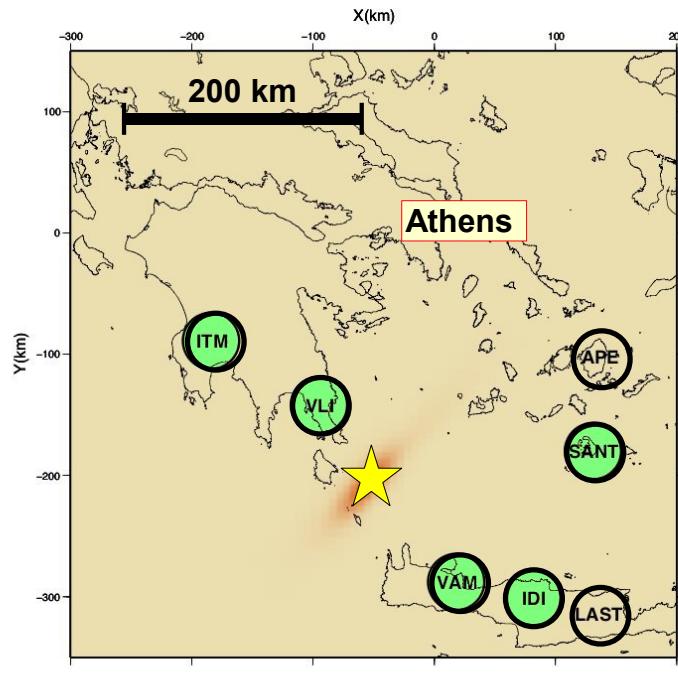
Evolutionary Location – 2006.01.08 M6.8 Greece

OT

t_{now}

-10 s

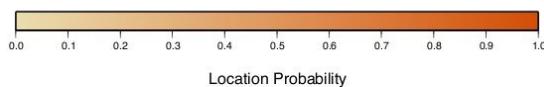
t^s_{Athens}



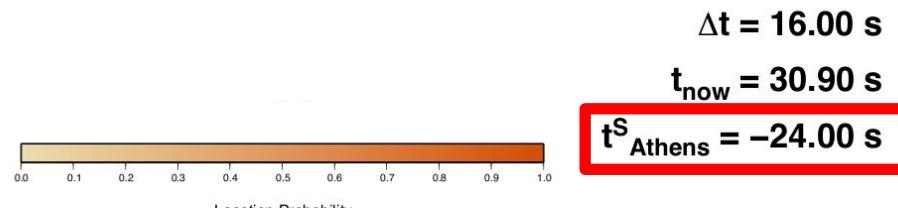
$$\Delta t = 16.00 \text{ s}$$

$$t_{\text{now}} = 30.90 \text{ s}$$

$$t^s_{\text{Athens}} = -24.00 \text{ s}$$



NLLoc



RTLoc

3. New perspectives in observatory analysis: Illustrative examples of global-search earthquake location

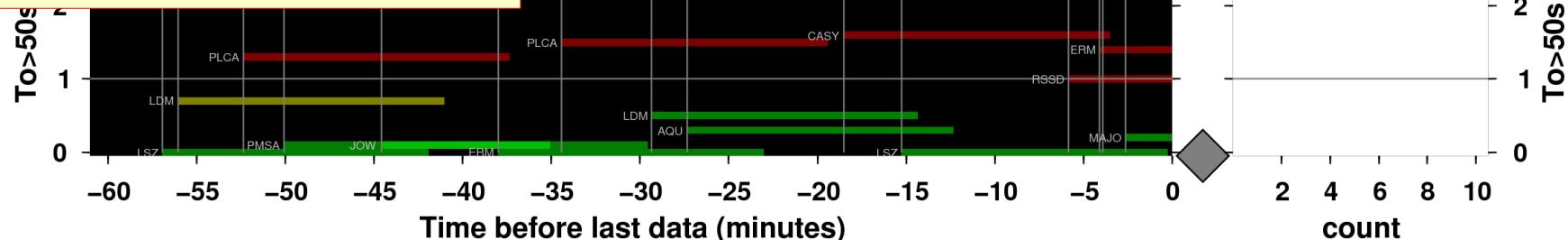
**Real-time display of derived quantities:
Tsunami early-warning**

2009.04.28-10:24:50 UTC

2009.04.28-11:25:51

Tsunami early-warning based on rupture duration > 50s

Time history of warning levels



To>50sec Exceedance

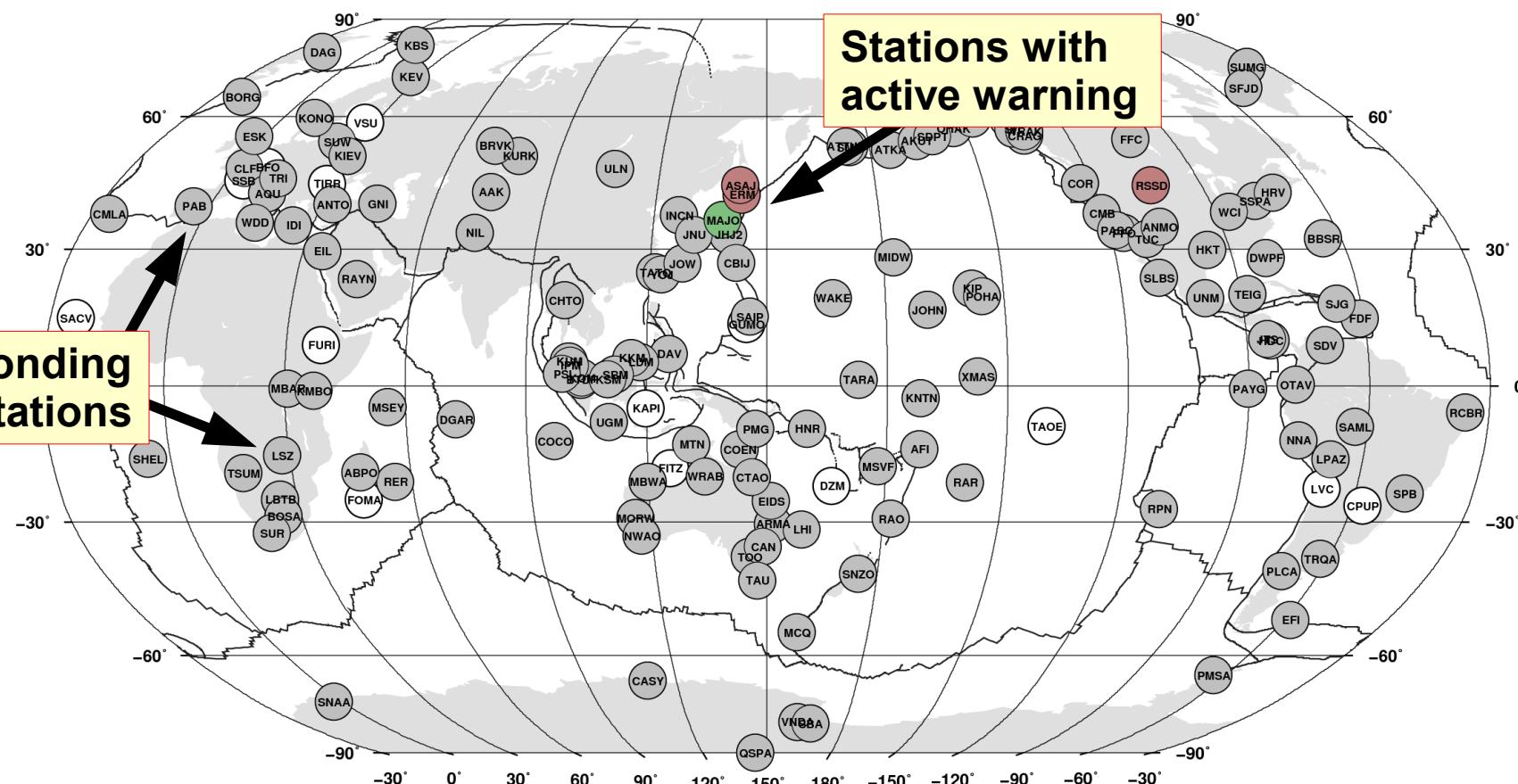
nStations: resp=146/161

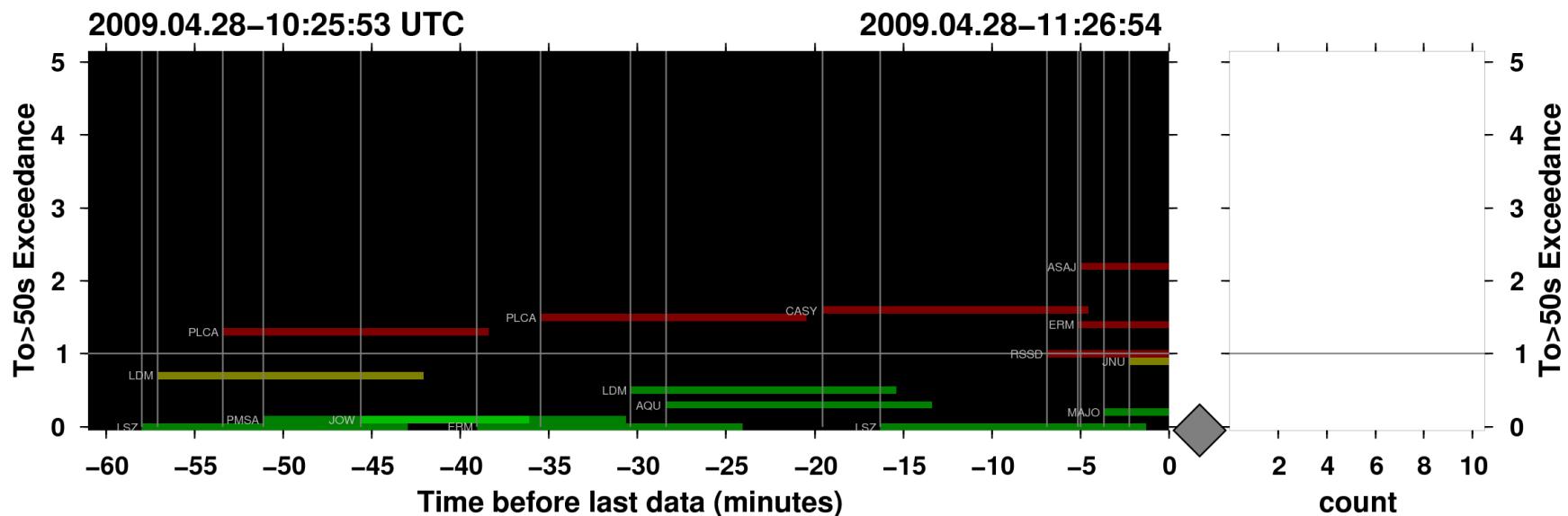
nWarning=0

2009.04.28.11.25.51

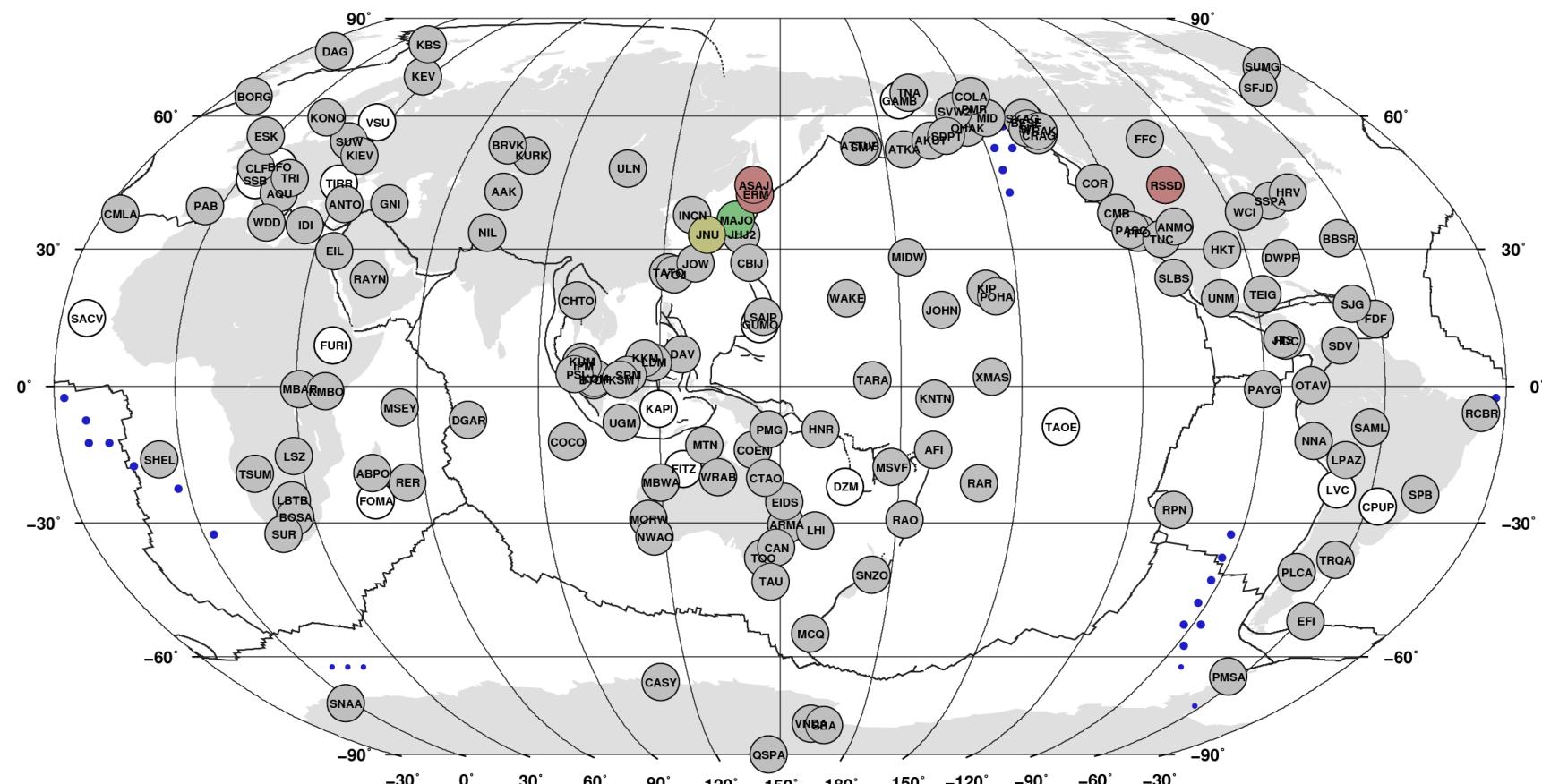
Stations with active warning

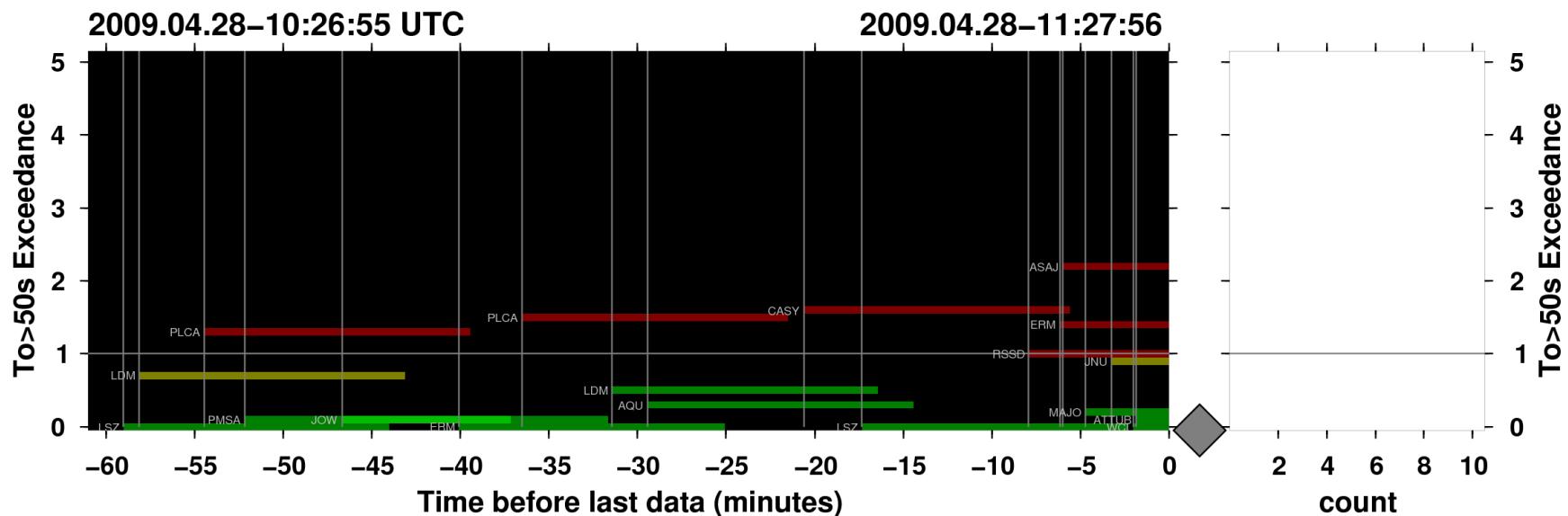
Responding stations



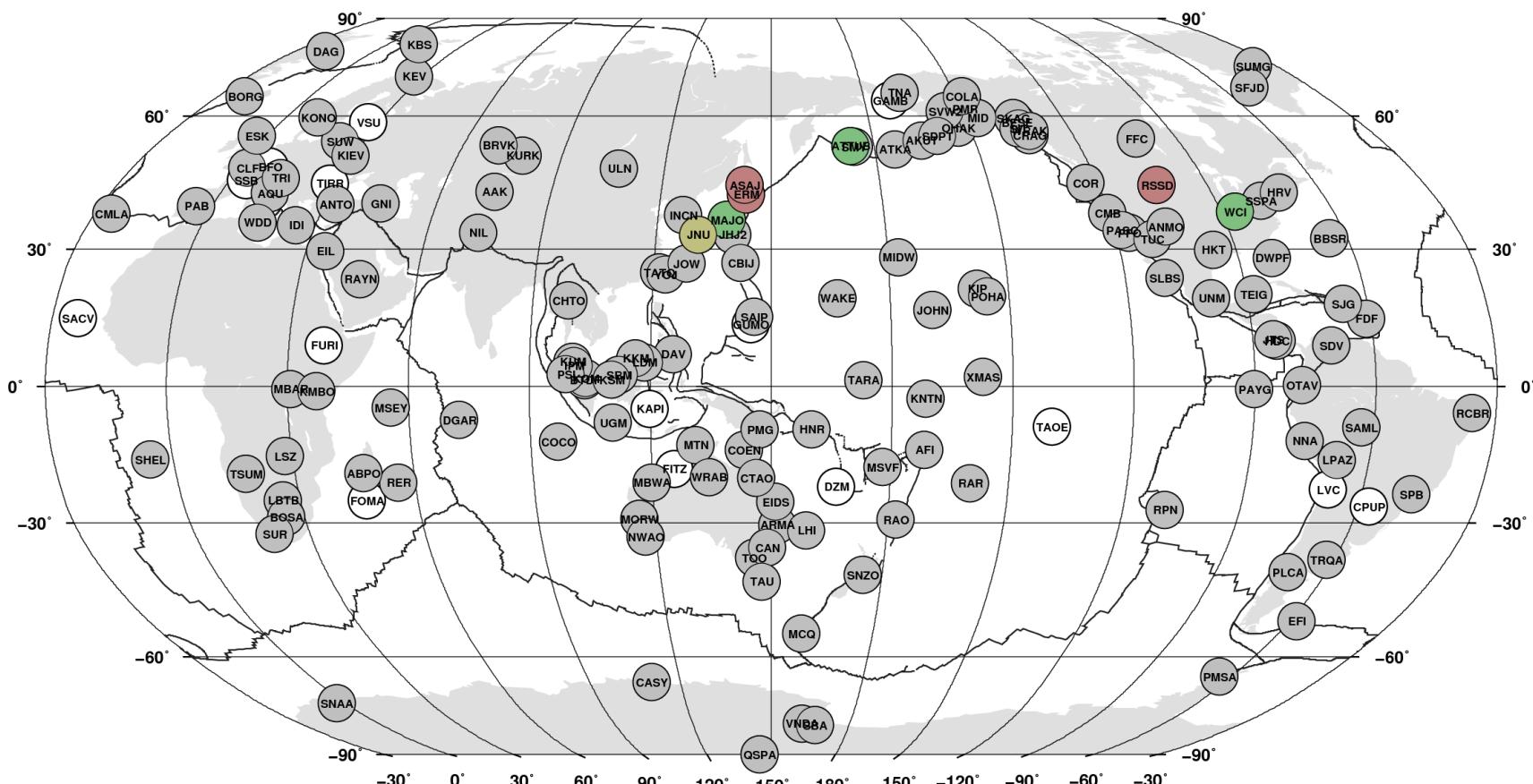


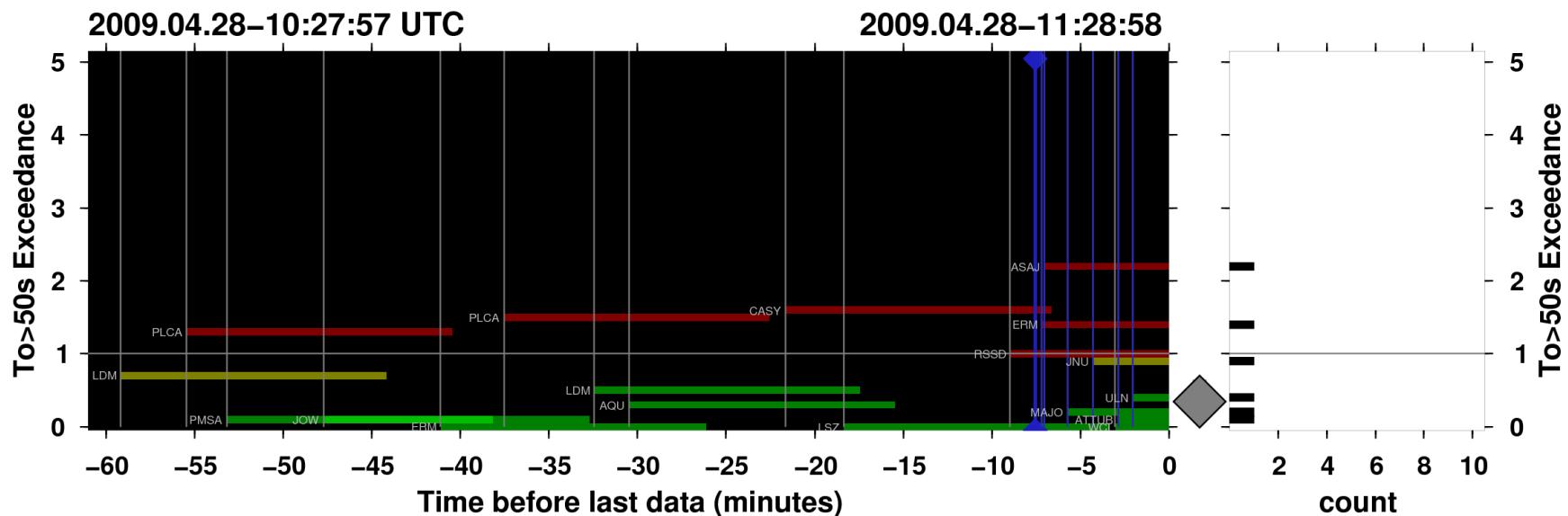
To>50sec Exceedance nStations: resp=146/161 nWarning=0 2009.04.28.11.26.54



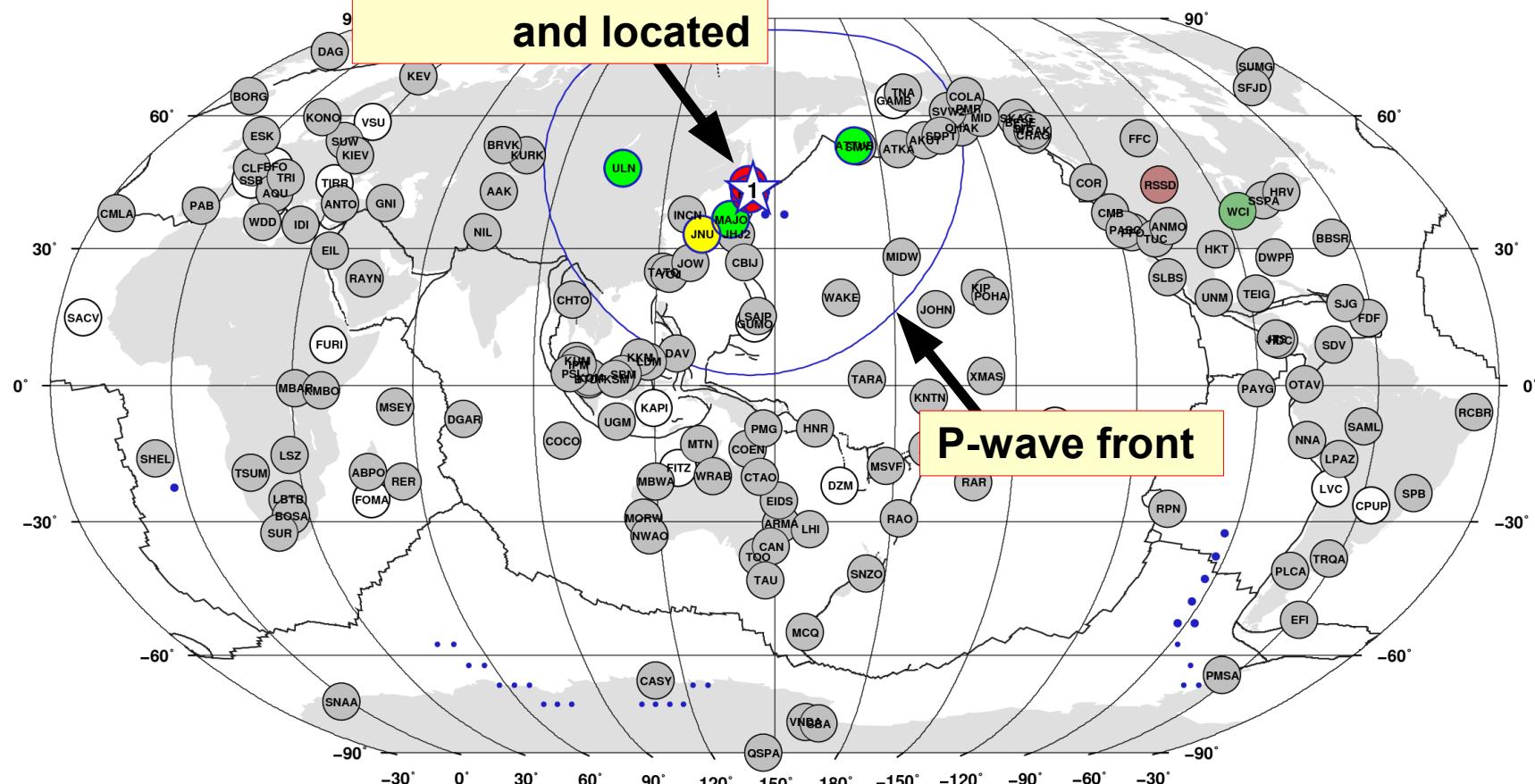


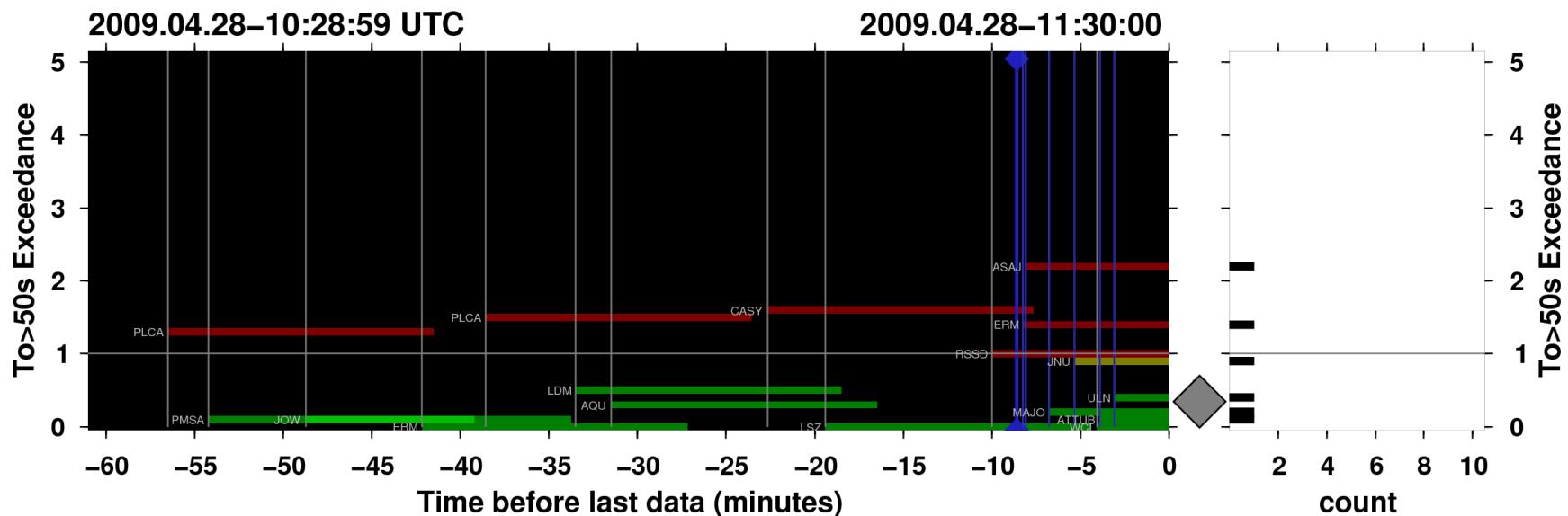
To>50sec Exceedance nStations: resp=146/161 nWarning=0 2009.04.28.11.27.56



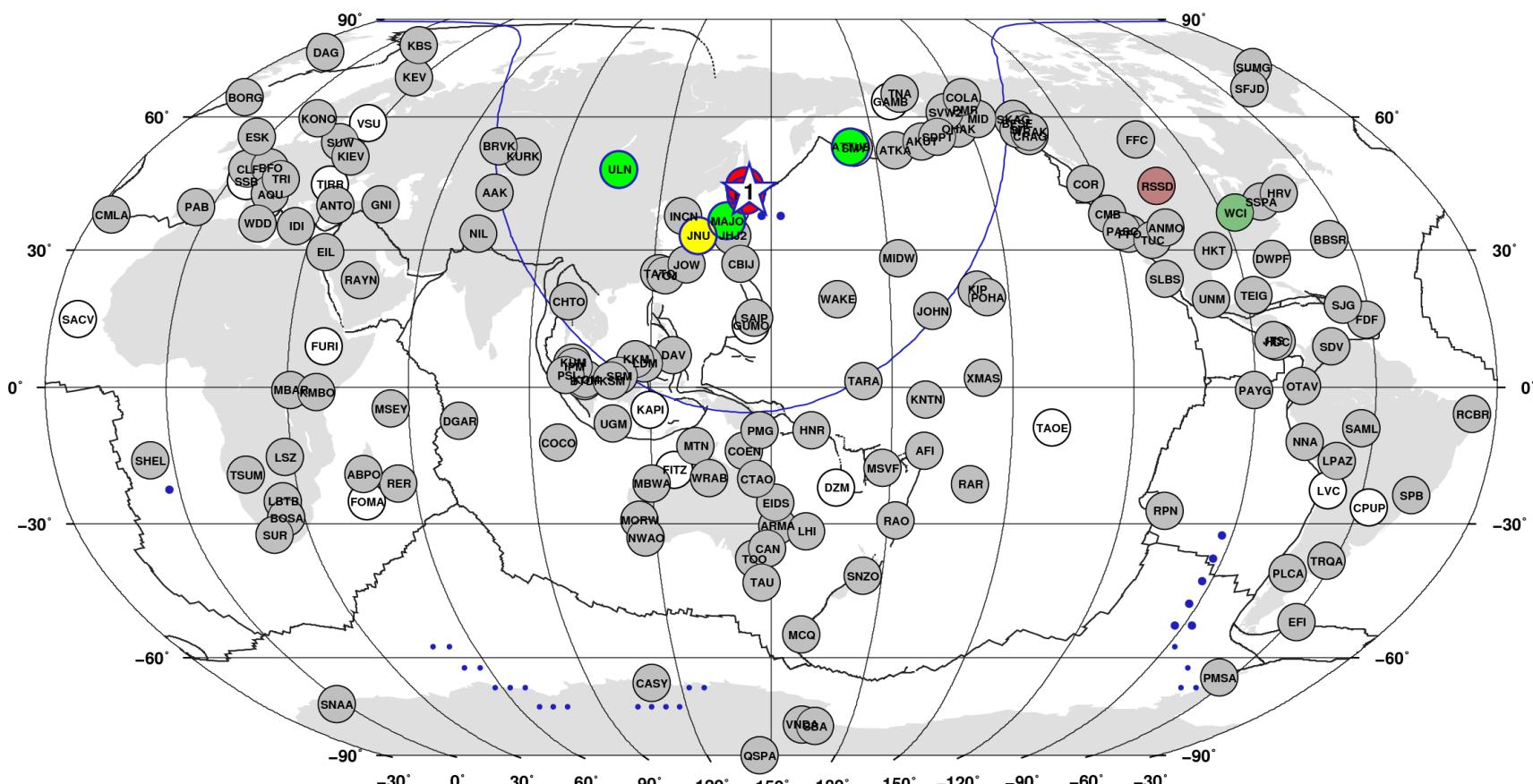


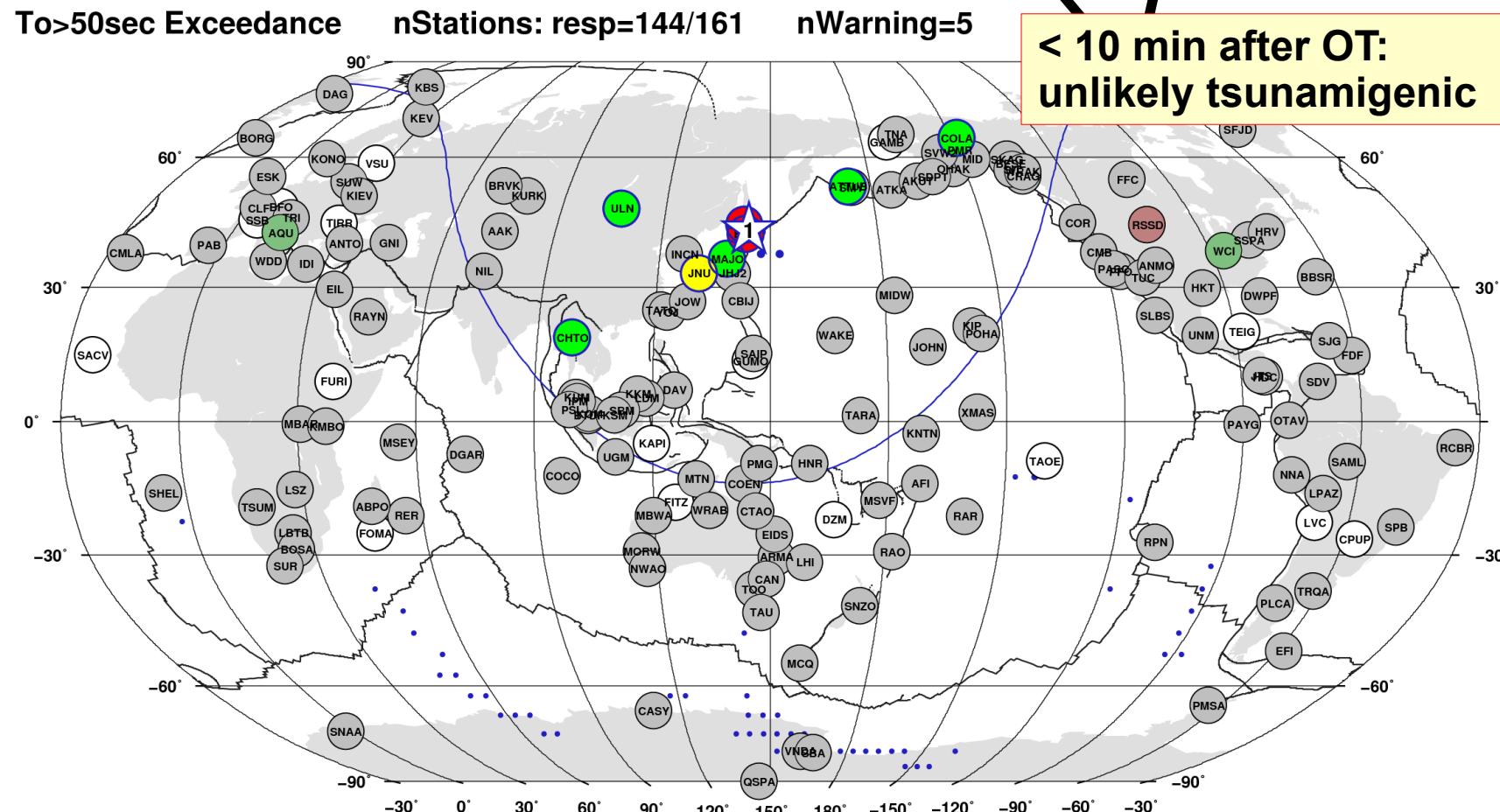
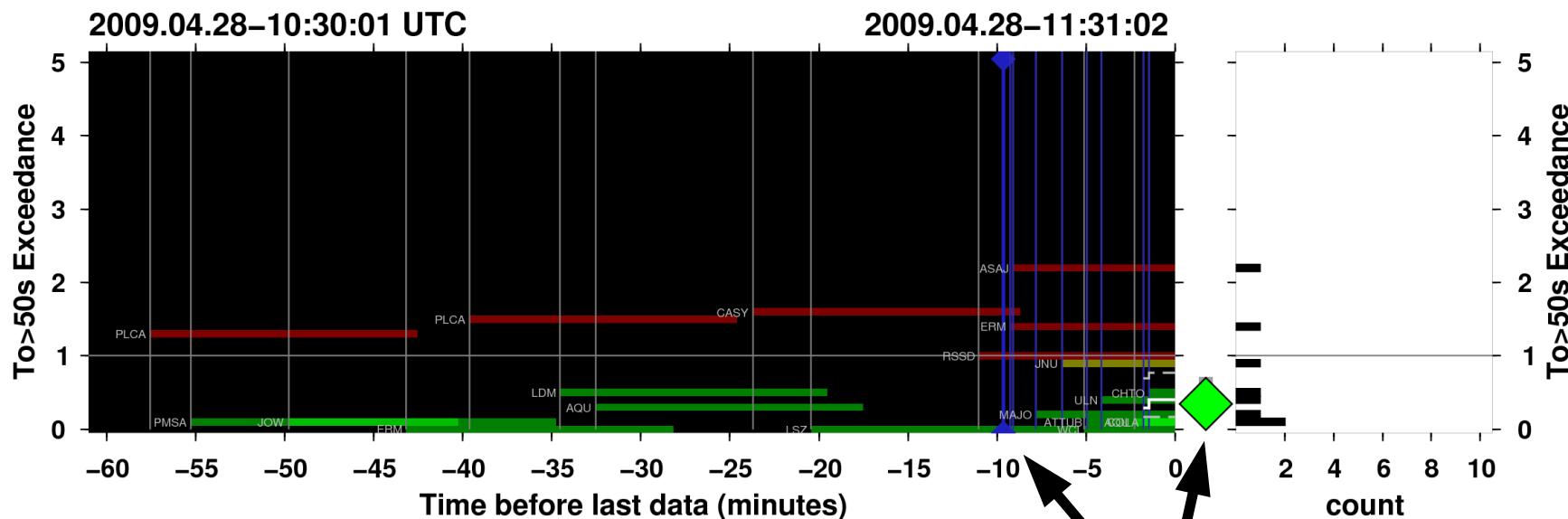
To>50sec Exceedance Event associated and located nWarning=3 2009.04.28.11.28.58

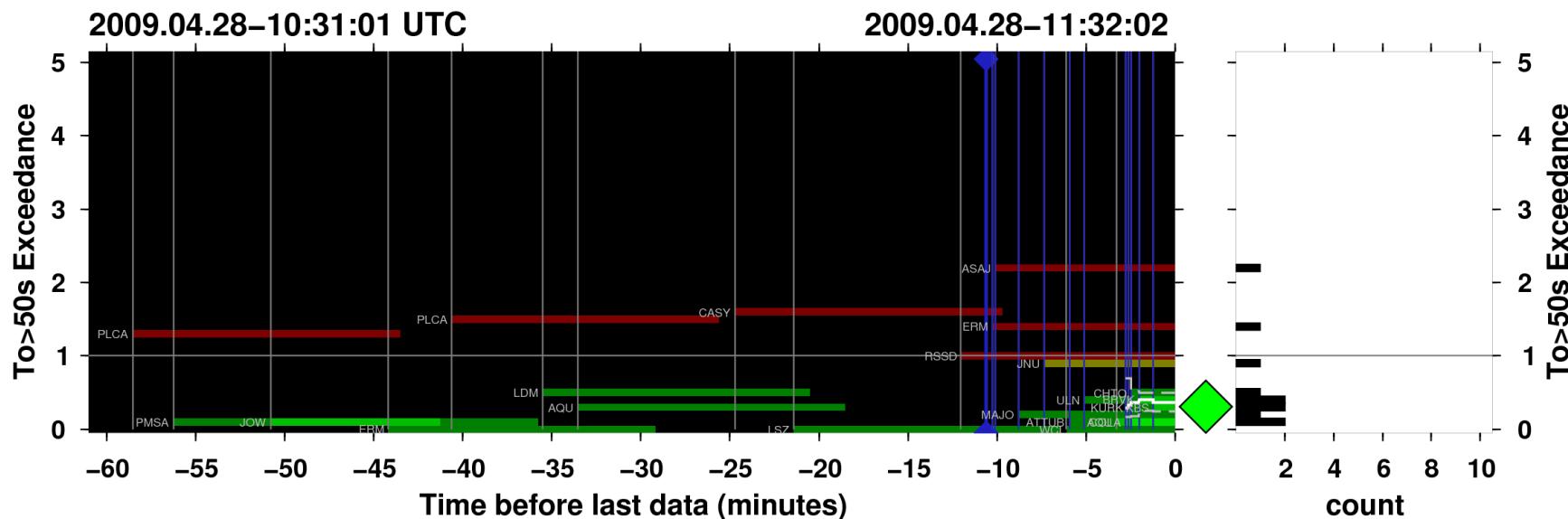




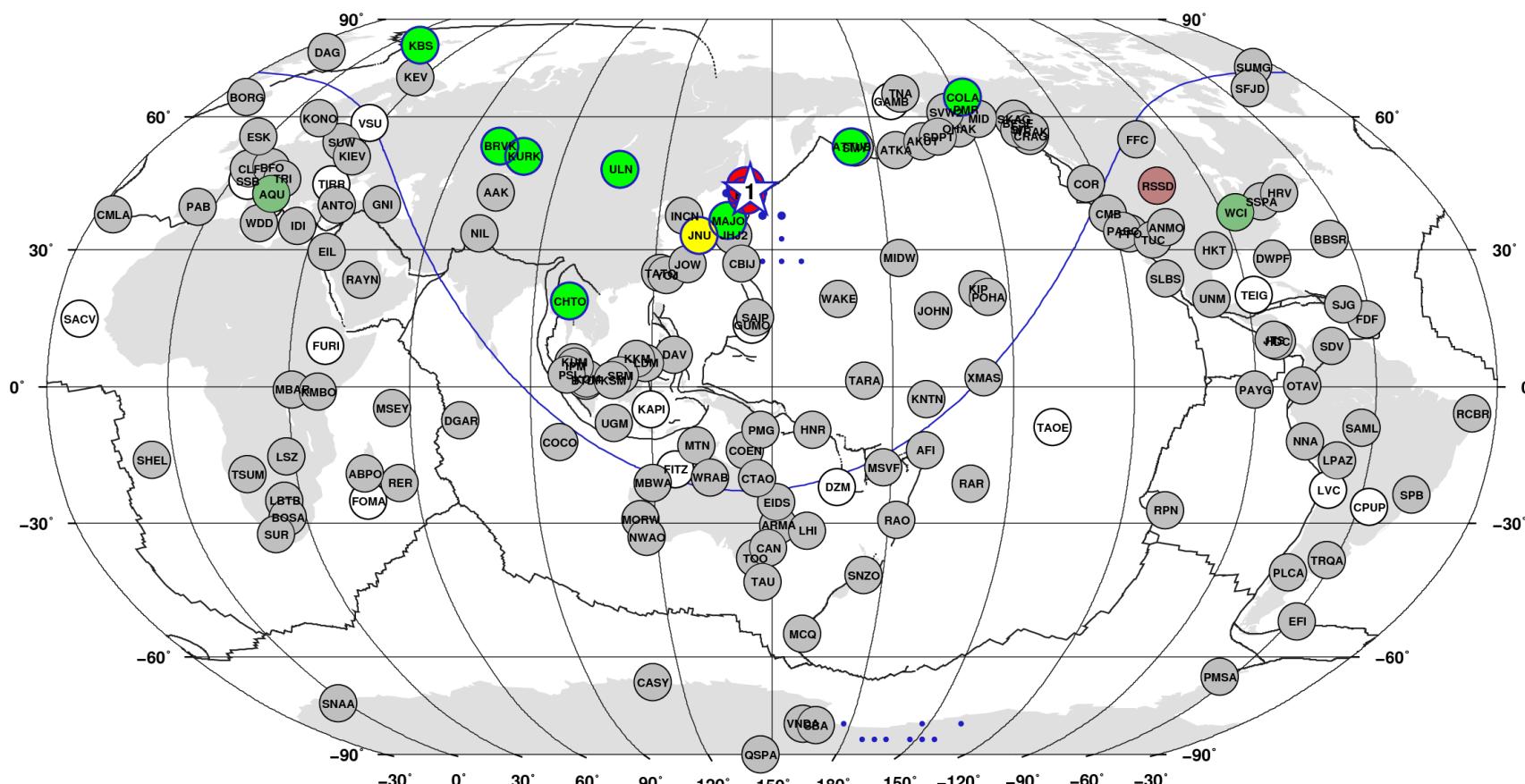
To>50sec Exceedance nStations: resp=146/161 nWarning=3 2009.04.28.11.30.00

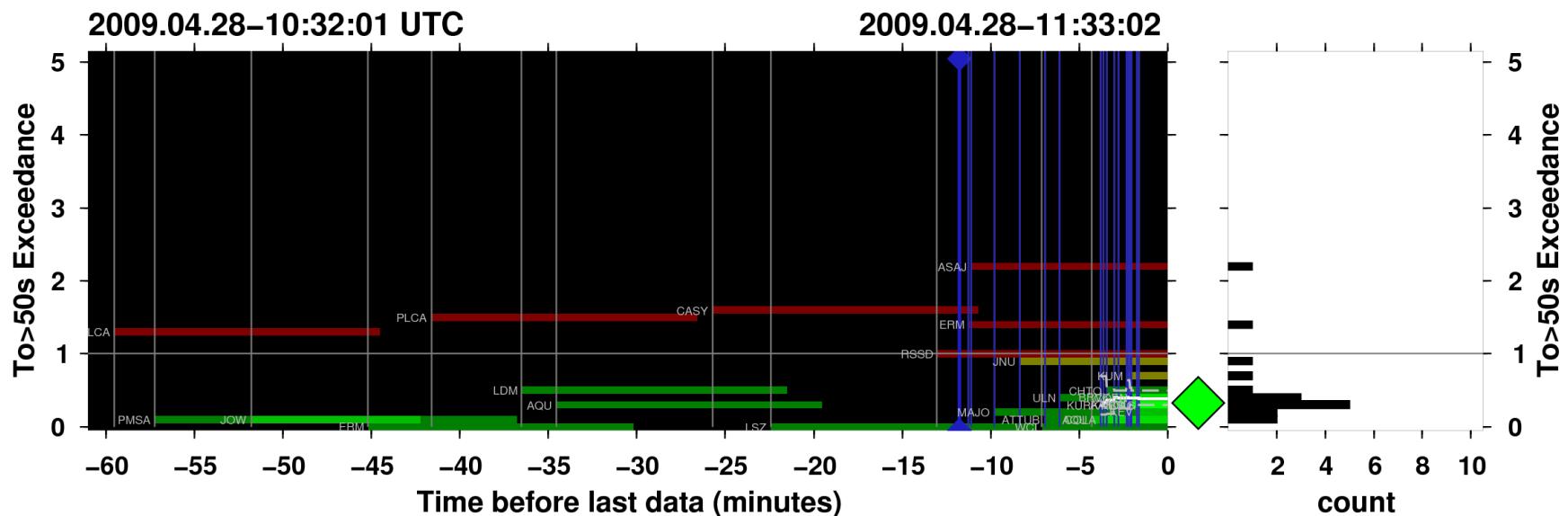




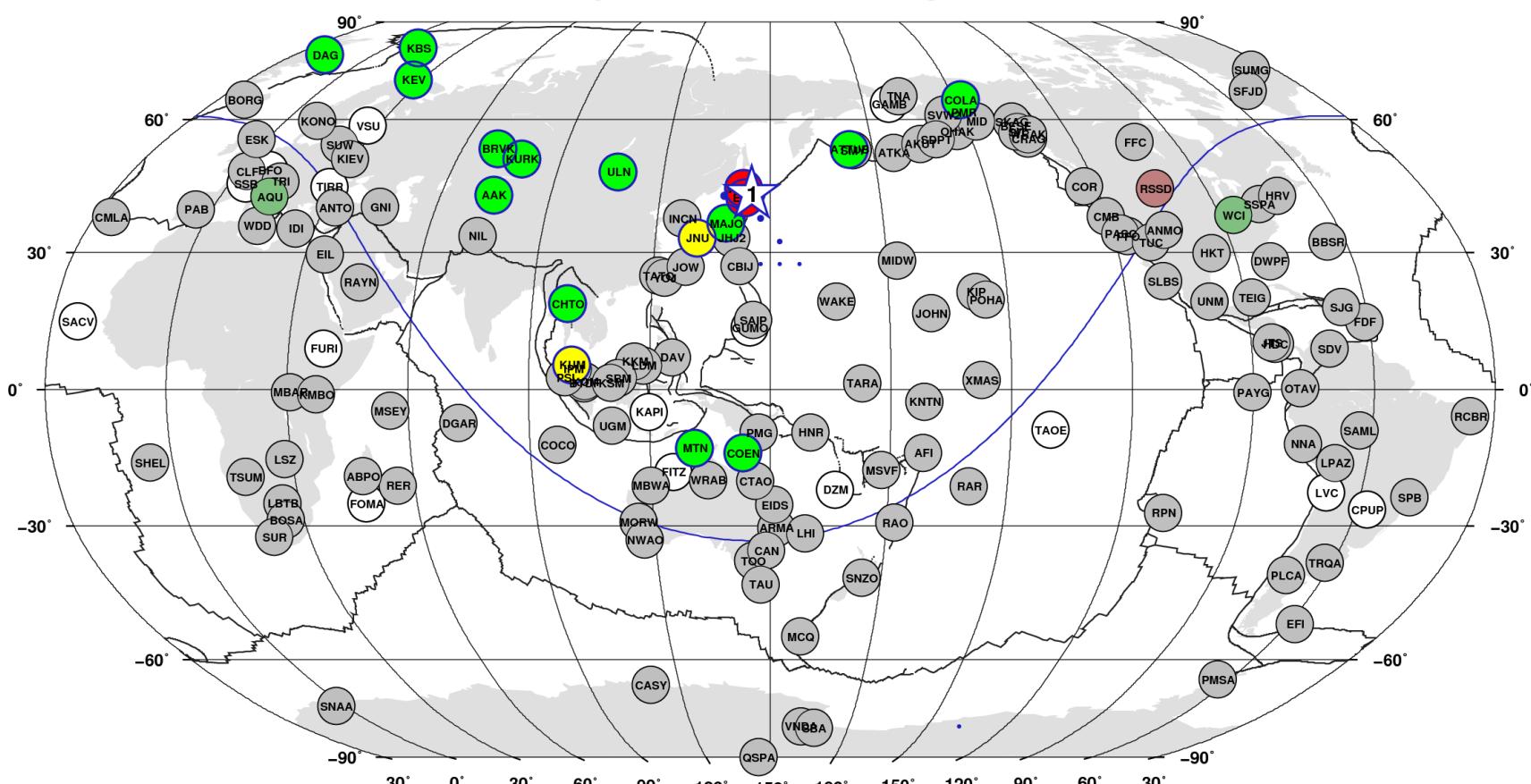


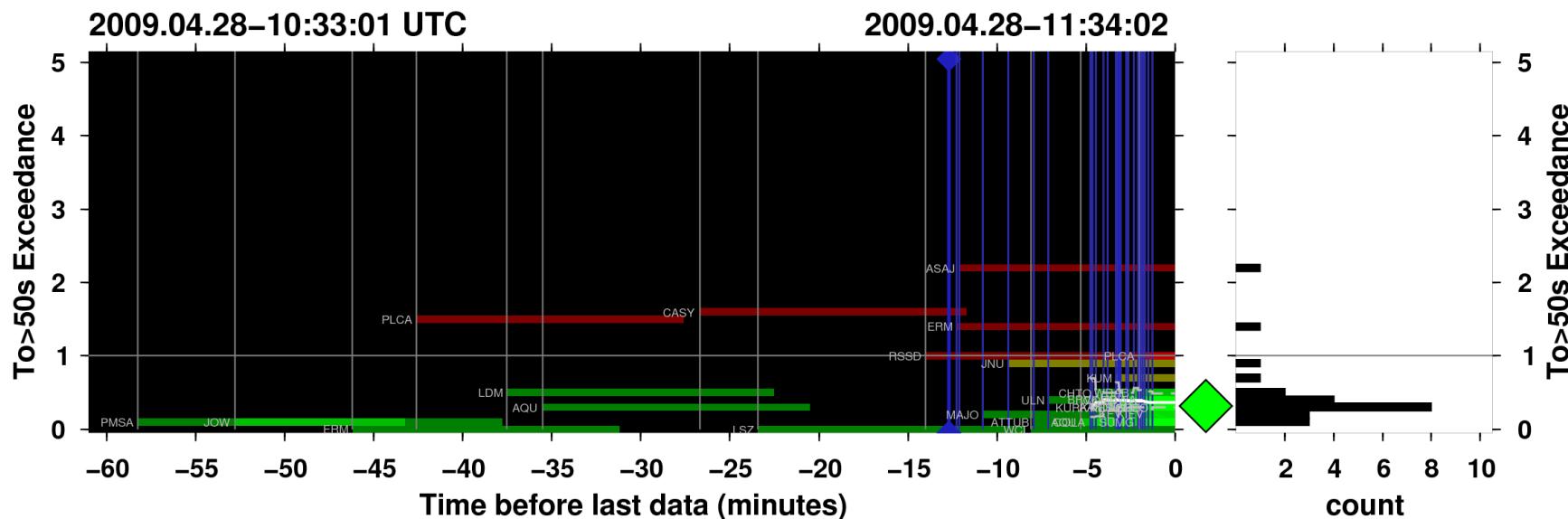
To>50sec Exceedance nStations: resp=145/161 nWarning=8 2009.04.28.11:32:02



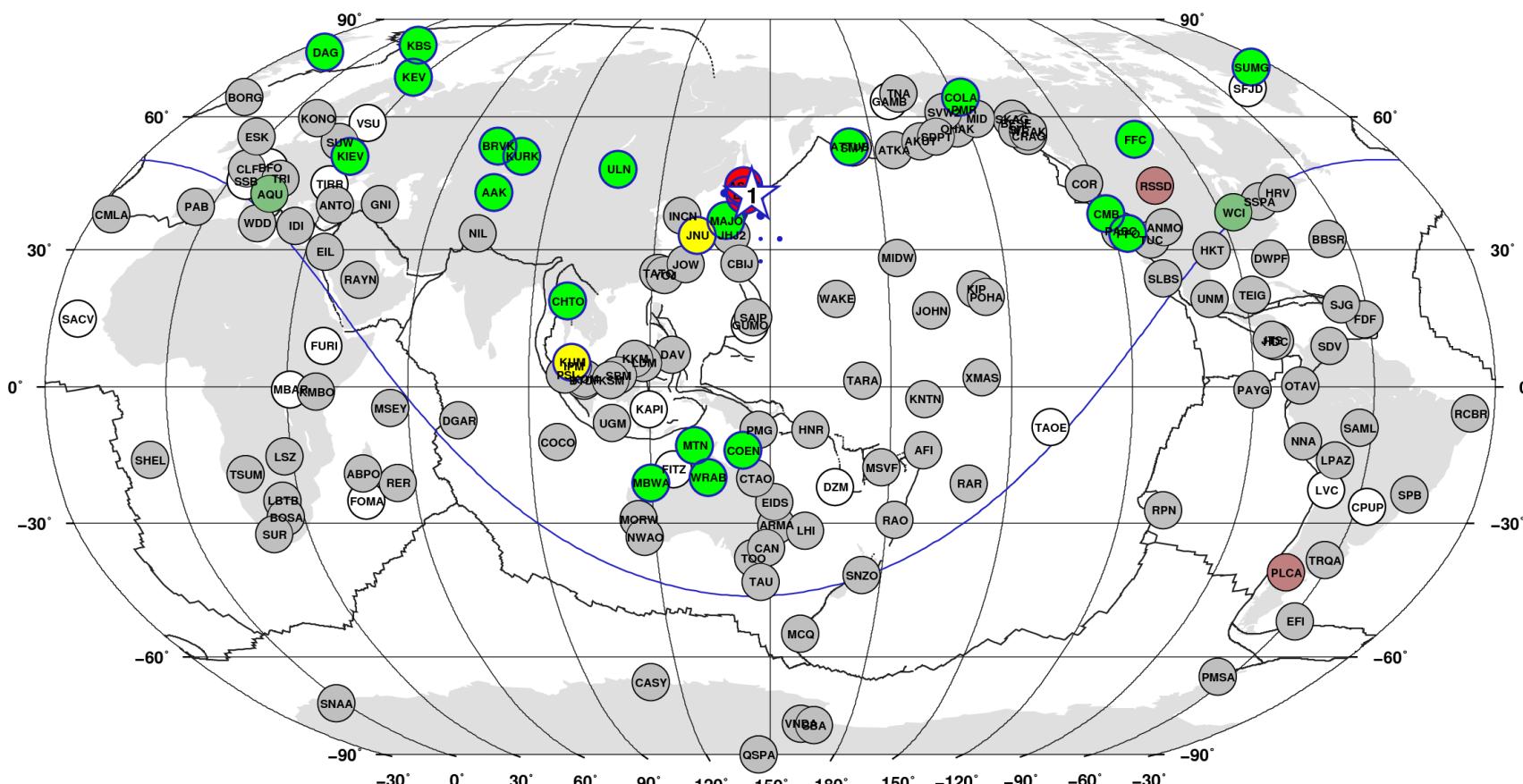


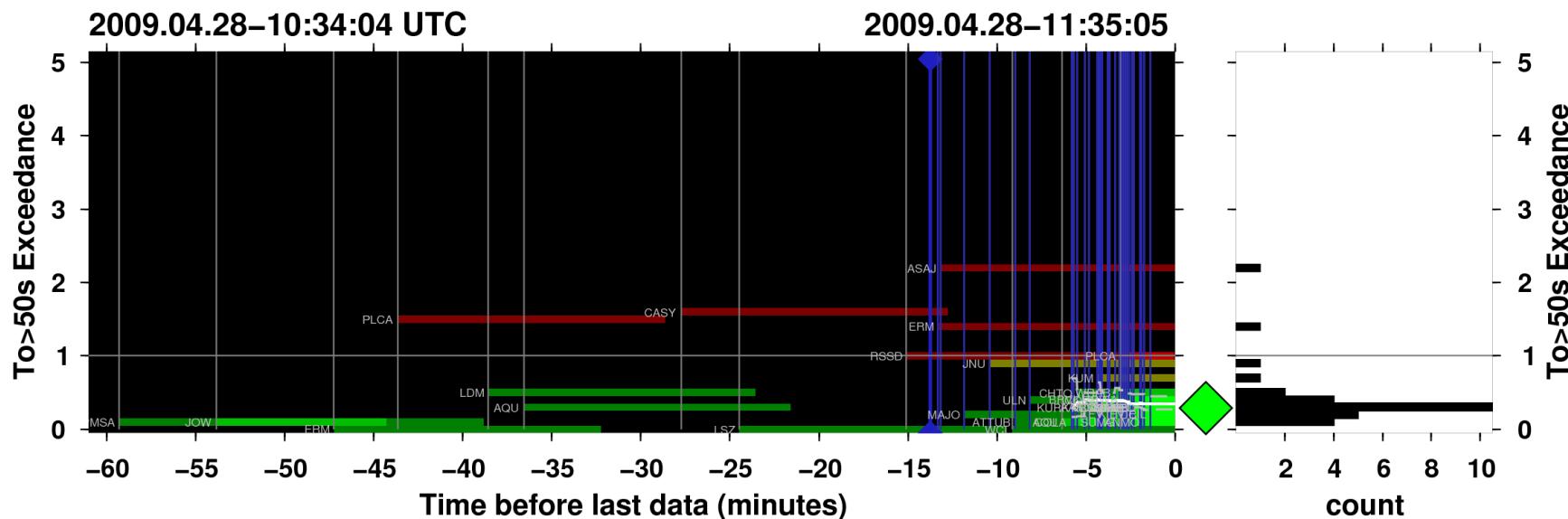
To>50sec Exceedance nStations: resp=145/161 nWarning=14 2009.04.28.11.33.02



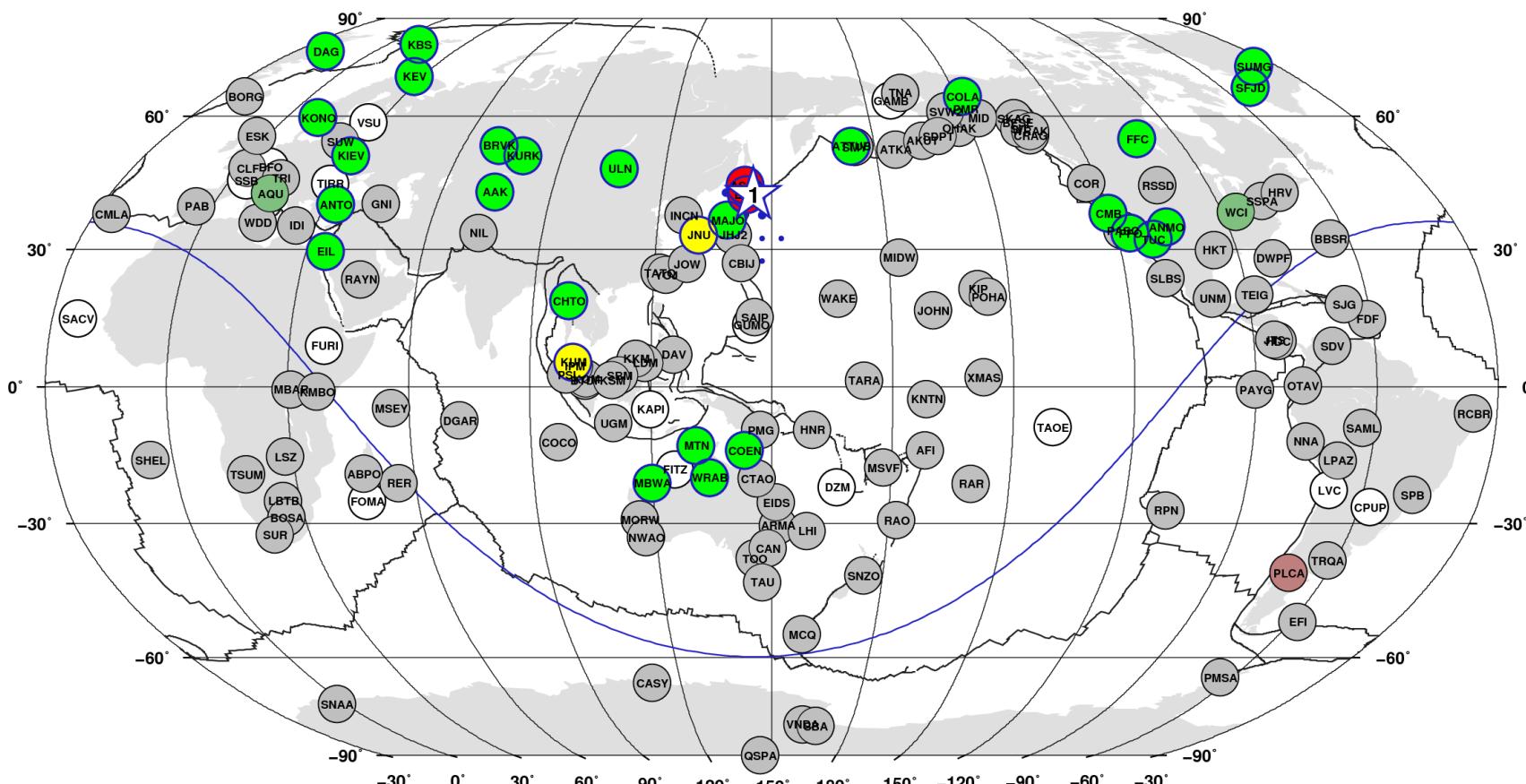


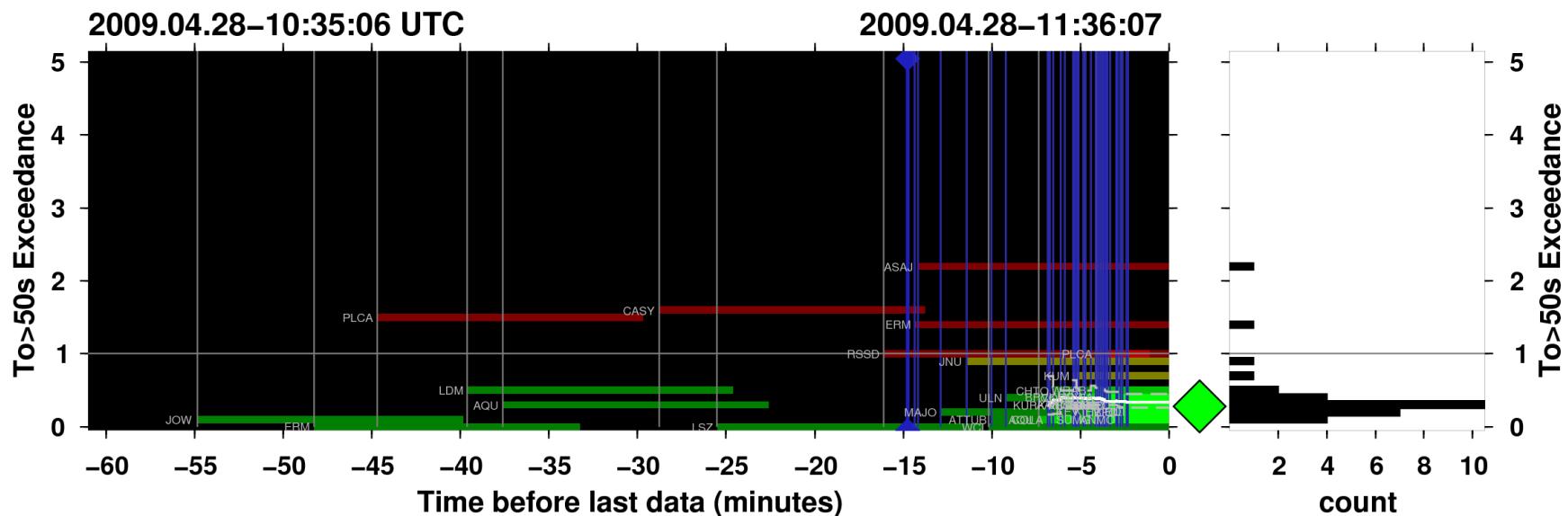
To>50sec Exceedance nStations: resp=143/161 nWarning=21 2009.04.28.11.34.02



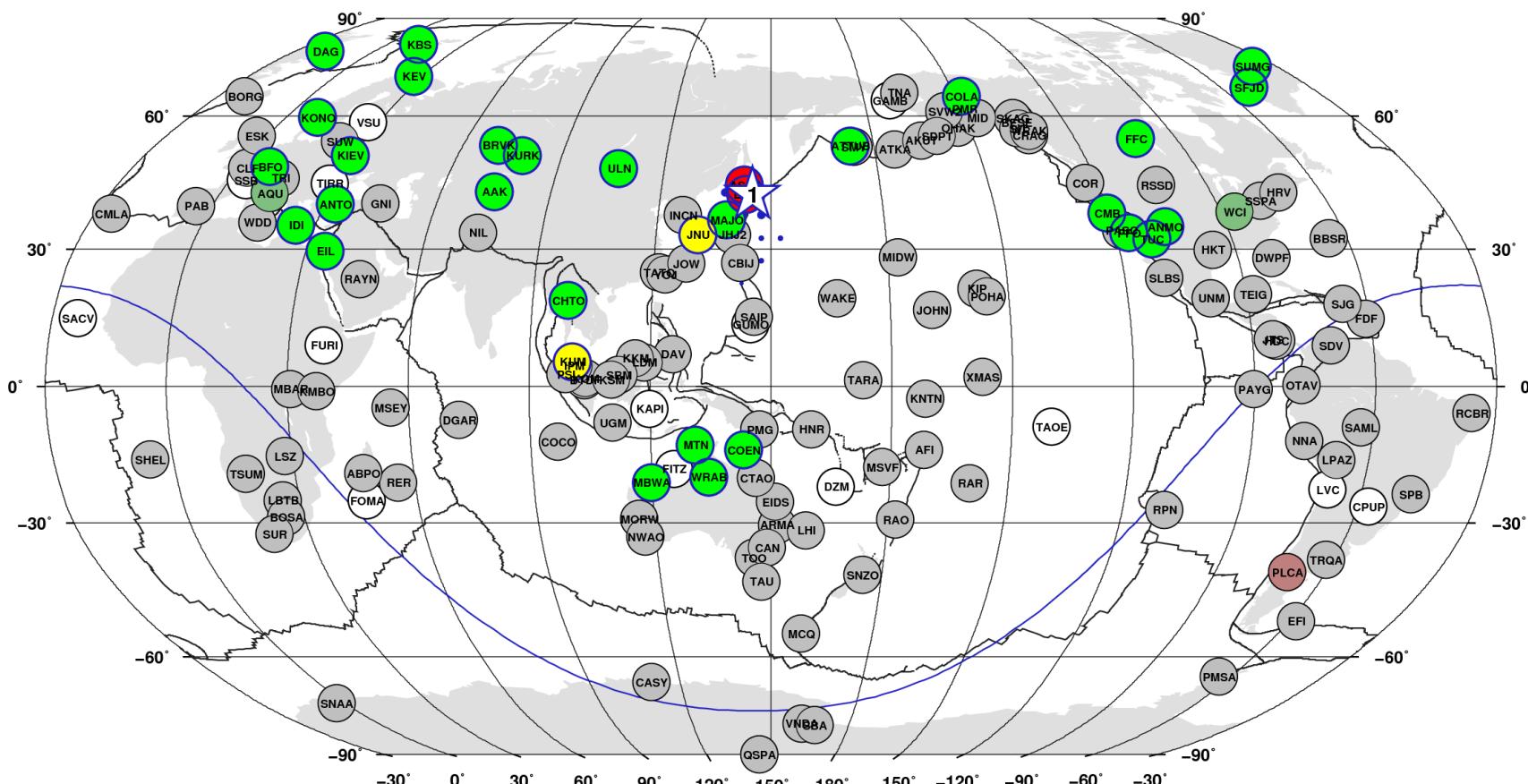


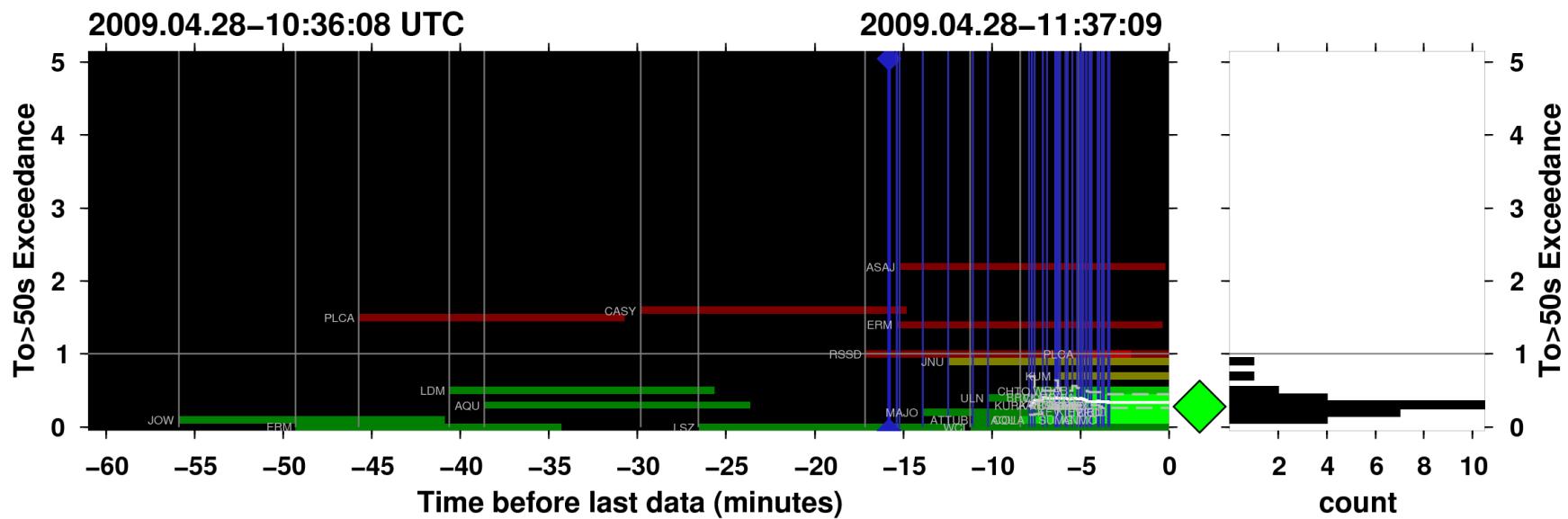
To>50sec Exceedance nStations: resp=144/161 nWarning=27 2009.04.28.11.35.05



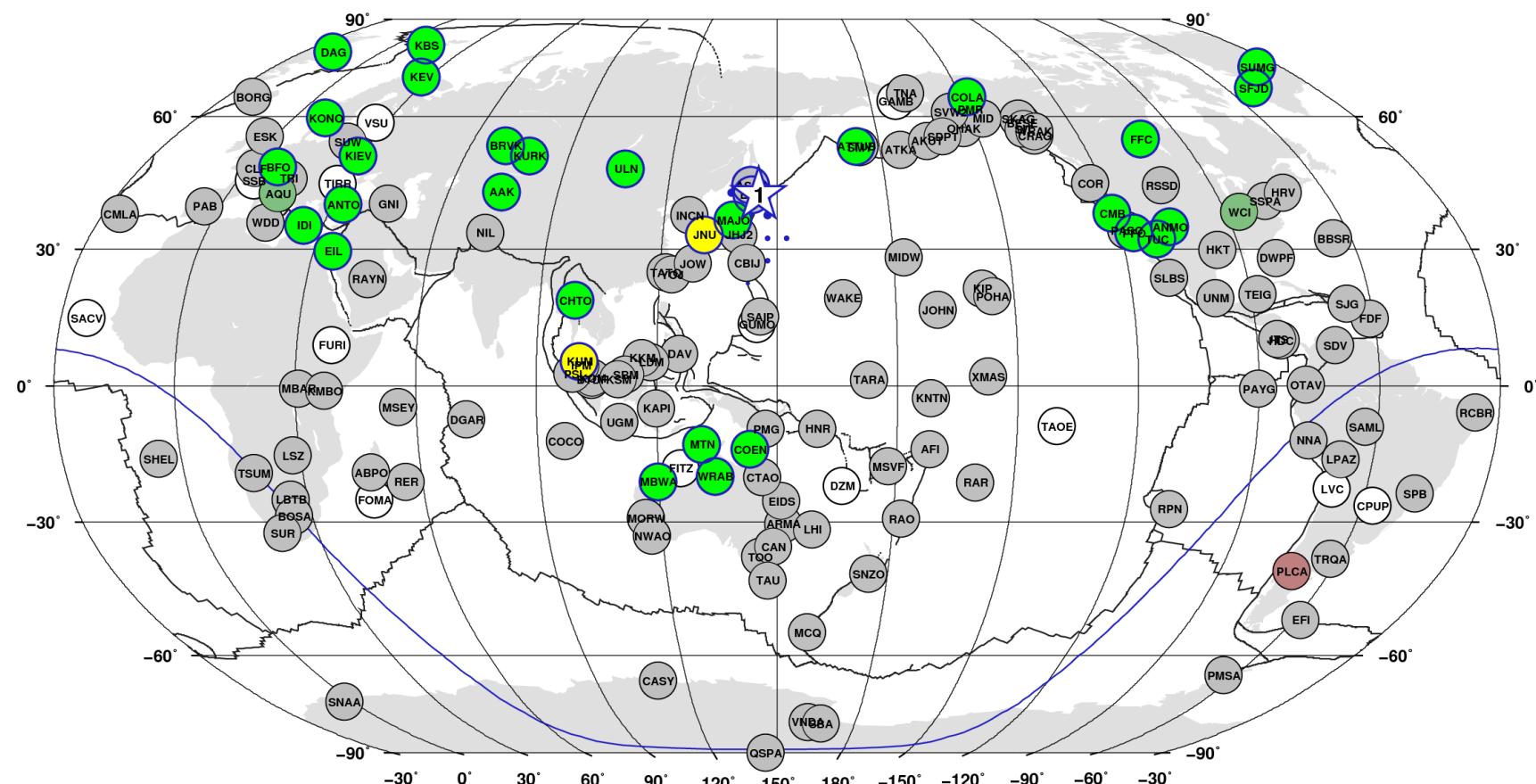


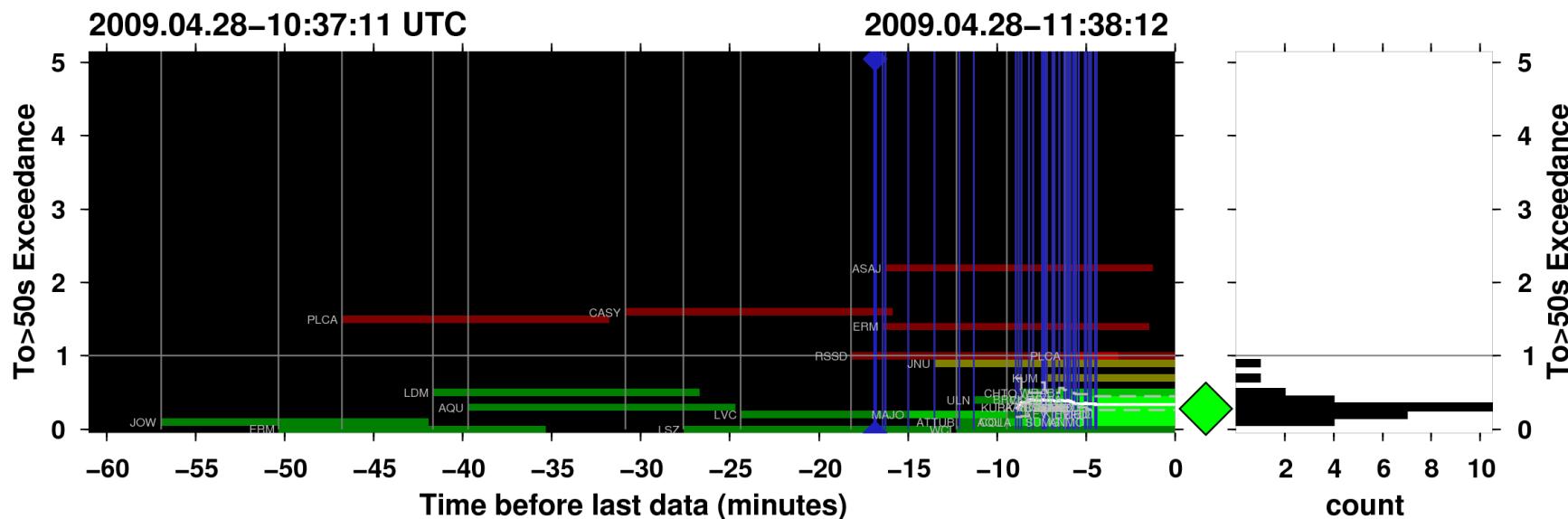
To>50sec Exceedance nStations: resp=146/161 nWarning=29 2009.04.28.11.36.07



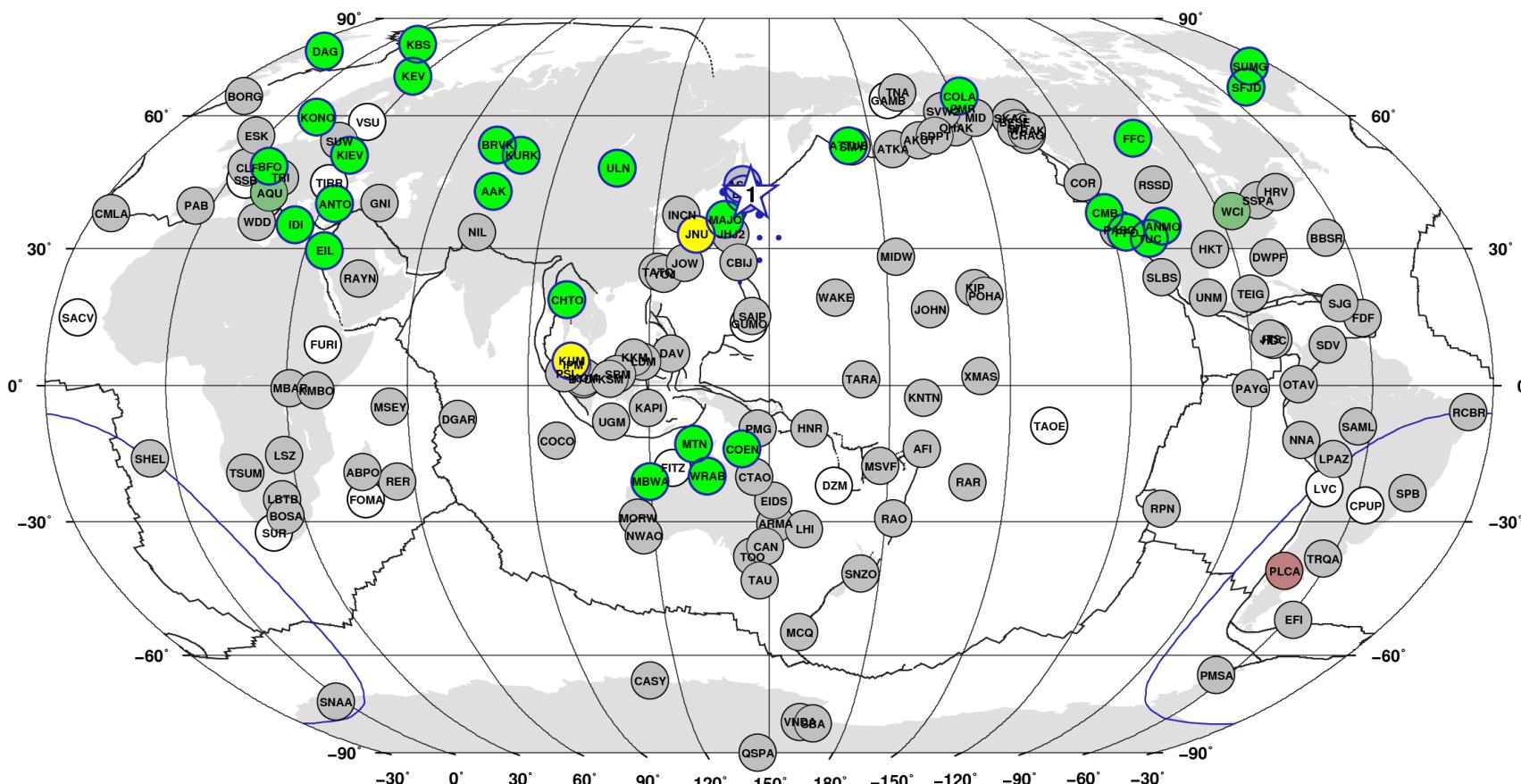


To>50sec Exceedance nStations: resp=146/161 nWarning=29 2009.04.28.11.37.09

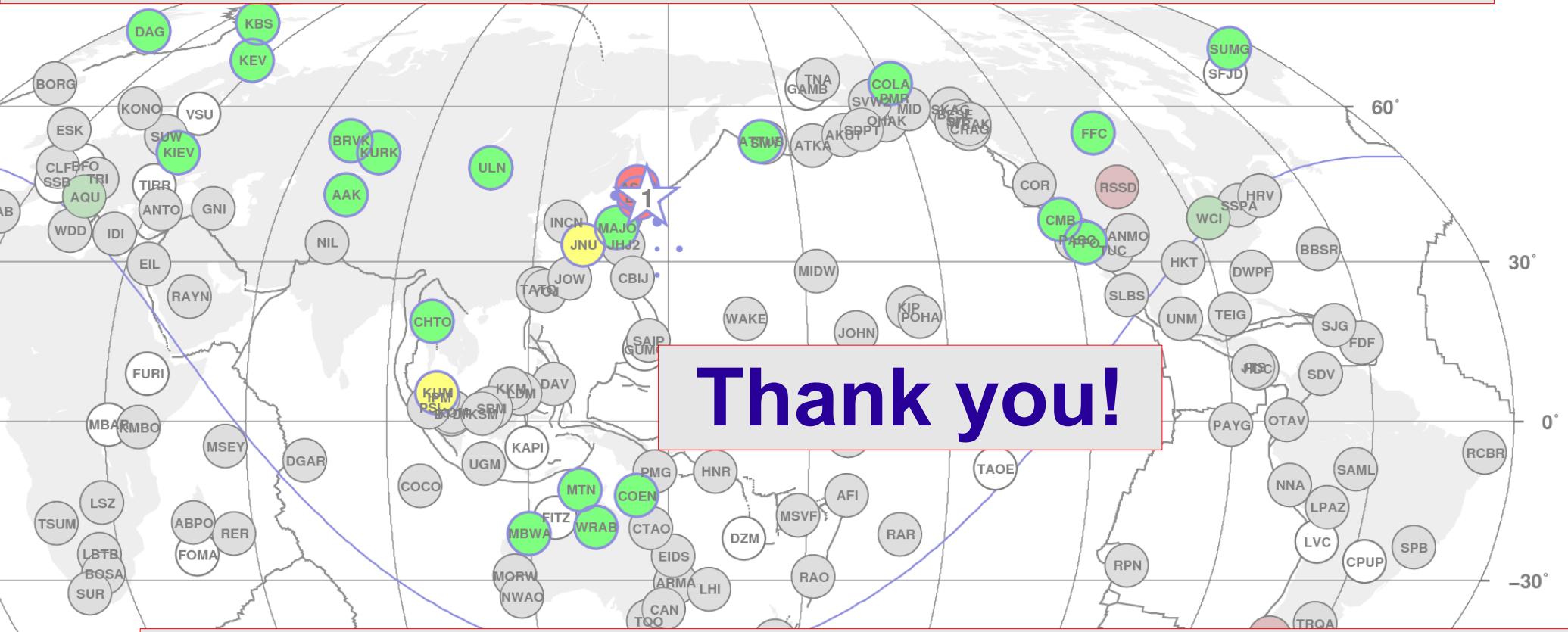




To>50sec Exceedance nStations: resp=146/161 nWarning=29 2009.04.28.11.38.12



Real-Time Earthquake Location



Anthony Lomax
ALomax Scientific, Mouans-Sartoux, France

Alberto Michelini
Istituto Nazionale di Geofisica e Vulcanologia, Roma, Italy

Andrew Curtis
ECOSSE, Grant Institute of GeoSciences, University of Edinburgh, Edinburgh, United Kingdom

References

- Lomax, A., A. Michelini, A. Curtis (2009), Earthquake Location, Nonlinear, in *Complexity In Earthquakes, Tsunamis And Volcanoes And Forecasting And Early Warning Of Their Hazards*, W.H.K. Lee, ed., Encyclopedia of Complexity and System Science, Springer, Heidelberg.
[EarthqkLoc-Direct-Search_v2.0.pdf](#)
- Allen, R.V. (1978), Automatic earthquake recognition and timing from single traces. *Bull. Seism. Soc. Am.*, **68**, 1521-1531.
- Allen, R.V. (1982), Automatic phase pickers: their present use and future prospects. *Bull. Seism. Soc. Am.*, **72**, S225-S242.
- Bai C-Y and Kennett B.L.N. (2000), Automatic phase-picking and identification by full use of a single three-component broadband seismogram, *Bull. Seism. Soc. Am.*, **90**, 187-198.
- Baer, M., and U. Kradolfer (1987), An automatic phase picker for local and teleseismic events. *Bull. Seism. Soc. Am.*, **77**, 1437-1445.
- Cichowicz, A. (1993), An automatic s phase picker, *Bull. Seism. Soc. Am.*, **83**, 180-189.
- Greenhalgh, S., I. M. Mason and B. Zhou (2005), An analytical treatment of single station triaxial seismic direction finding, *J. Geophys. Eng.*, **2**, 8-15, doi:10.1088/1742-2132/2/1/002.
- Hendrick, N. and S. Hearn (1999), Polarisation Analysis: What is it? Why do you need it? How do you do it?, *Explor. Geophys.*, **30**, 177-190.
- Johnson, C. E., A. Lindh, B. Hirshorn (1994), Robust regional phase association, U.S. Geol. Surv. Open-File Rept. 94-621.
- Leonard, M. (2000), Comparison of Manual and Automatic Onset Time Picking, *Bull. Seism. Soc. Am.*, **90**, 1384-1390.
- Lahr, J.C. (1984), Description of the weighted regression and quality estimation used in the earthquake location program hypoellipse, *U.S. Geological Survey Open-File Report 84-766*, <http://jclahr.com/science/software/hypoellipse/of84-766.pdf>.
- Lahr, J.C. (1999), HYPOELLIPE: A Computer Program for Determining Local Earthquake Hypocentral Parameters, Magnitude, and First-Motion Pattern (Y2K Compliant Version), *U.S. Geological Survey Open-File Report 99-23*, <http://pubs.usgs.gov/of/1999/ofr-99-0023/>.
- Lomax, A. (2005), A Reanalysis of the Hypocentral Location and Related Observations for the Great 1906 California Earthquake, *Bull. Seism. Soc. Am.*, **91**, 861-877.
- Lomax, A.J. and A. Michelini (1988), The use of spherical coordinates in the interpretation of seismograms, *Geophys. J. R. astr. Soc.*, **93**, 405-412.
- Magotra, N., N.Ahmed, and E.Chael (1987), Seismic event detection and source location using single station (three-component) data, *Bull. Seism. Soc. Am.*, **77**, 958-971.
- Montalbetti, J. F., and E. R. Kanasewich (1970), Enhancement of teleseismic body phases with a polarization filter, *Geophys. J. R. Astr. Soc.* **21**, 119-129.
- Nguyen, D. T., R. J. Brown, D. C. Lawton, (1989), Polarization filter for multi-component seismic data, in *CREWES Research Report 1989*, chap. 7, 93-101, <http://www.crewes.org/Reports/1989/1989-07.pdf>.
- Oye, V. and W.L. Ellsworth (2005), Orientation of Three-Component Geophones in the San Andreas Fault Observatory at Depth Pilot Hole, Parkfield, California, *Bull. Seism. Soc. Am.*, **95**, 751-758
- Samson, J. C. (1983), The spectral matrix, eigenvalues, and principal components in the analysis of multichannel geophysical data, *Ann. Geophys.* **1**, 115-119.
- Samson, J. C., and J. V. Olson (1980), Some comments on the descriptions of the polarization states of waves, *Geophys. J. R. Astr. Soc.* **61**, 115-130.
- Satriano, C., A. Lomax and A. Zollo (2008), Real-time evolutionary earthquake location for seismic early warning, *Bull. Seism. Soc. Am.*, **98**, 1482-1494
- Schimmel, M. and J. Gallart (2004), Degree of Polarization Filter for Frequency-Dependent Signal Enhancement Through Noise Suppression, *Bull. Seism. Soc. Am.*, **94**, 1016-1035.
- Sleeman, R., and T. van Eck (1999), Robust automatic P-phase picking: an on-line implementation in the analysis of broadband seismogram recordings, *Phys. of the Earth and Planet. Int.*, **113**, 265-275.
- Tarantola, A. (1987), *Inverse problem theory: Methods for data fitting and model parameter estimation*, Elsevier, Amsterdam, 613p.
- Tarantola, A. and Valette, B., (1982), Inverse problems = quest for information., *J. Geophys.*, **50**, 159-170.
- Vidale, J. E. (1986), Complex polarization analysis of particle motion, *Bull. Seism. Soc. Am.* **76**, 1393-1405.
- Withers, M., R. Aster, C. Young, J. Beiriger, M. Harris, S. Moore and J. Trujillo (1998), A comparison of select trigger algorithms for automated global seismic phase and event detection, *Bull. Seism. Soc. Am.*, **88**, 95-106.